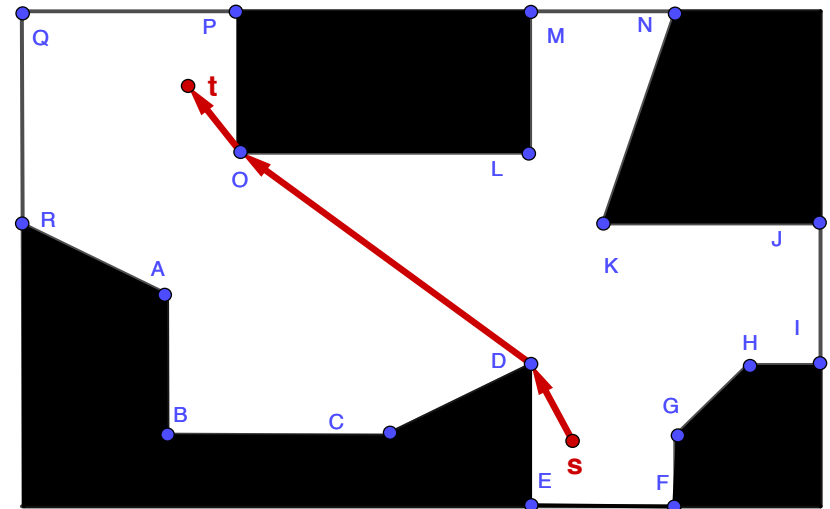


Euclidean Pathfinding with Compressed Path Databases IJCAI 2020

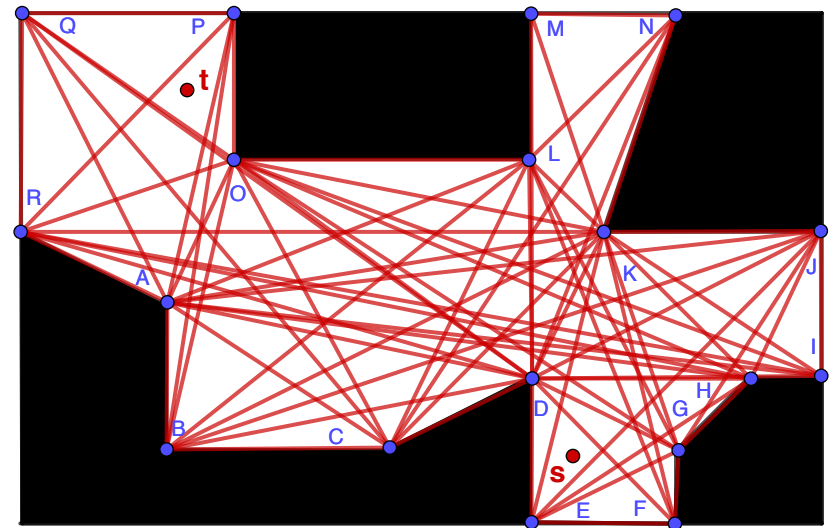
Bojie Shen, Muhammad Aamir Cheema, Daniel D. Harabor,
Peter J. Stuckey

Monash University

- Euclidean plane:
 - Polygonal obstacles
 - A set of vertices
 - A set of closed edges
- Pathfinding:
 - Given a start s and target t
 - Optimal non-obstructed path.



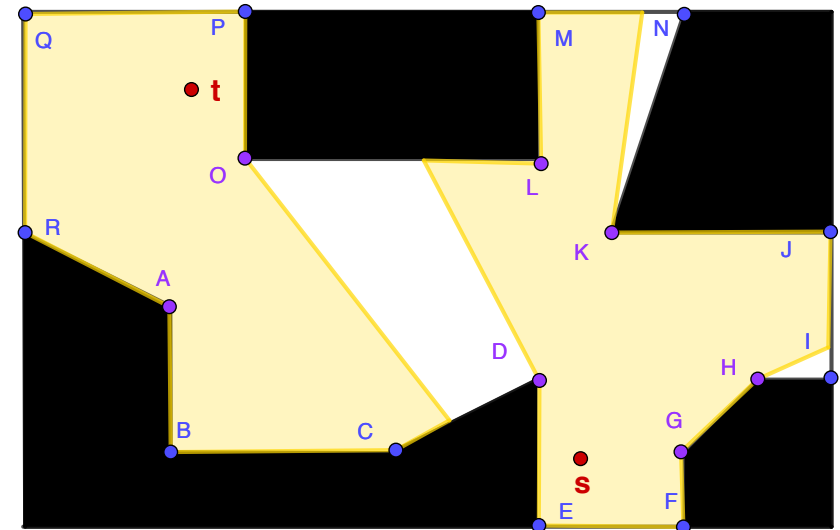
- Visibility graph [1]:
 - Connecting co-visible vertices



Visibility Graph Families

Pathfinding

- Visibility graph [1]
- Sparse visibility graph [2]
- **Pathfinding:**
 - Full insertion
 - Heuristic search

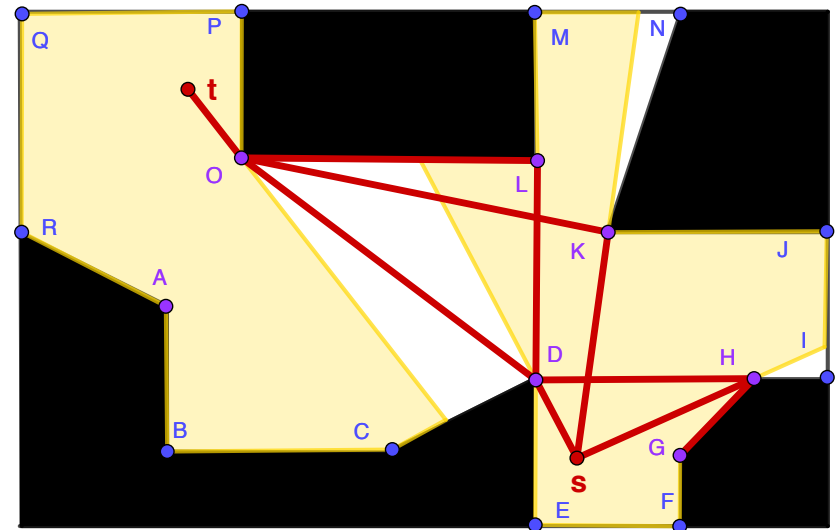


Shaded yellow areas correspond to the area visible from s and t

Visibility Graph Families

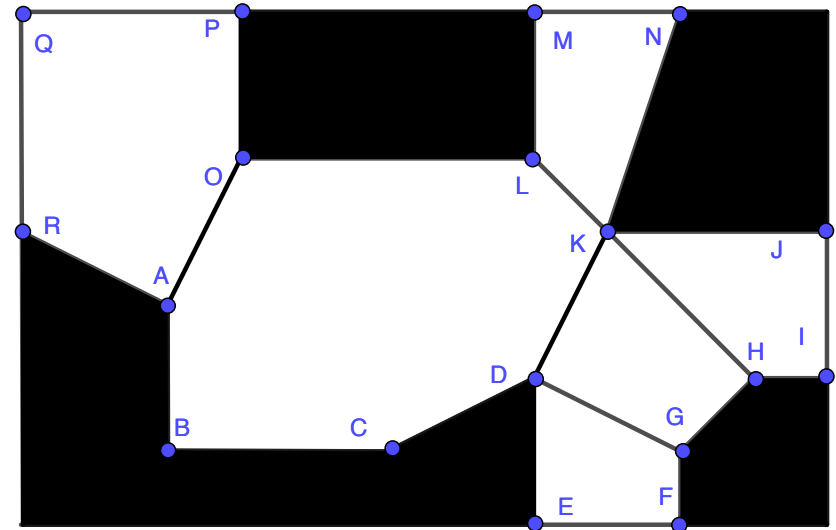
Pathfinding

- Visibility graph [1]
- Sparse visibility graph [2]
- **Pathfinding:**
 - Full insertion
 - **Heuristic search**

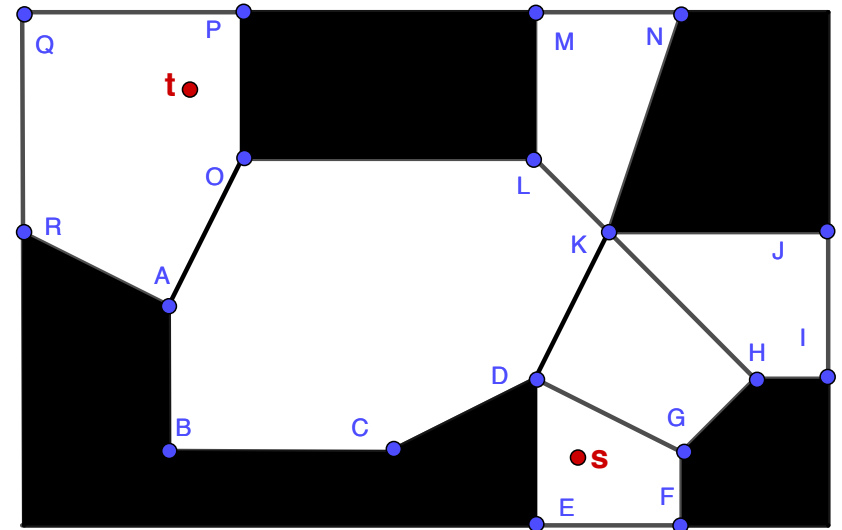


Shaded yellow areas correspond to the area visible from s and t

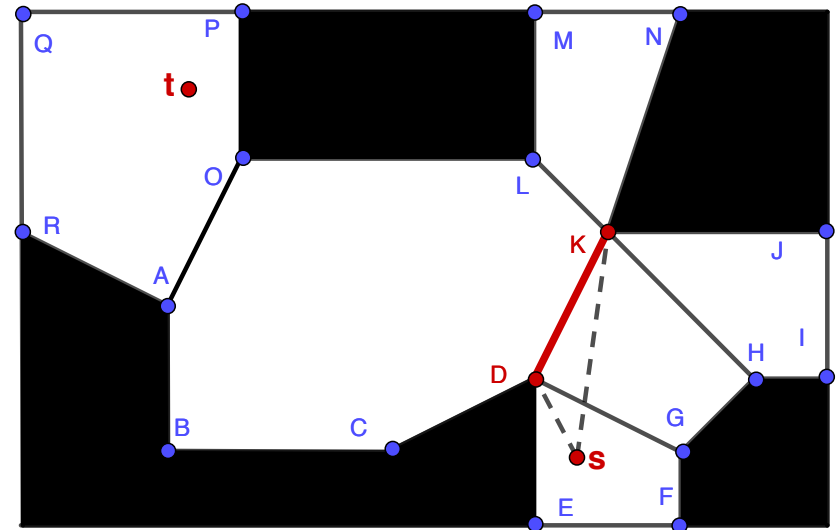
- Navigation Mesh



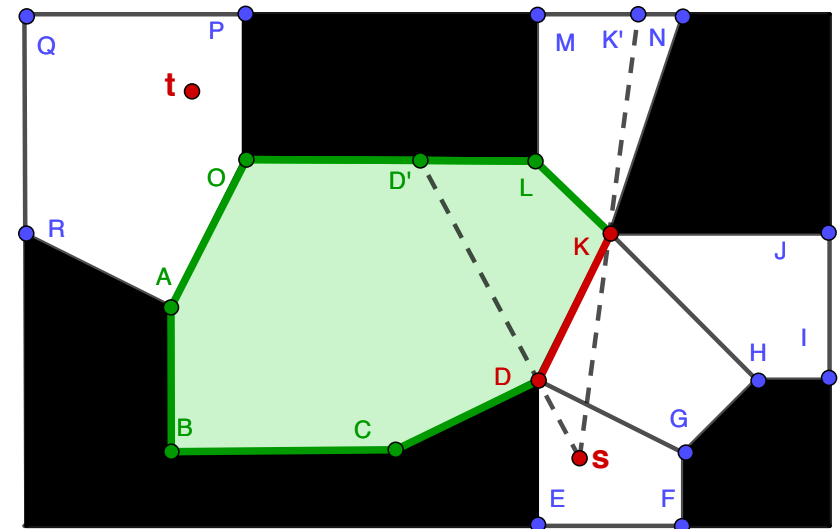
- Navigation Mesh
- Polyanya [3]
 - Search Nodes
 - Successors
 - Evaluation Function



- Navigation Mesh
- Polyanya [3]
 - Search Nodes:
 - Interval & Root
 - i.e. ([D,K] , s)

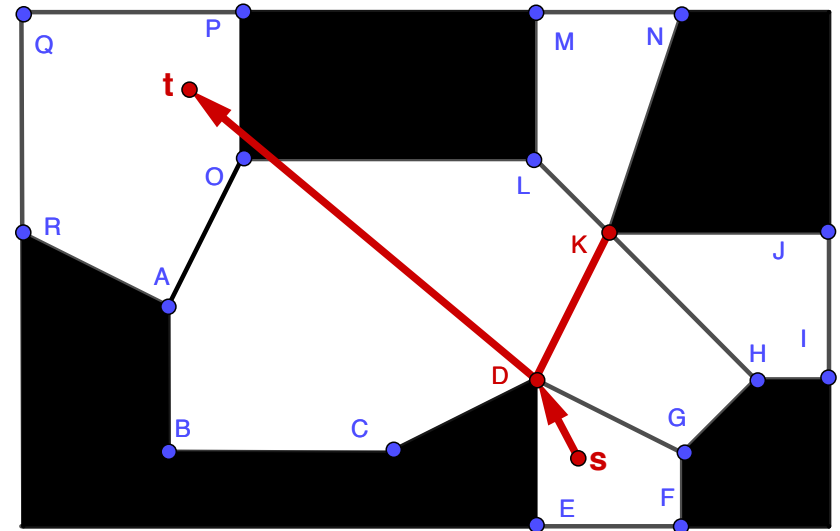


- Navigation Mesh
- Polyanya [3]
 - Search Nodes:
 - Interval & Root
 - Successors:
 - Observable Successors
 - i.e. ([L,K] , s)
 - Non-observable Successors
 - i.e. ([A,O] , D)

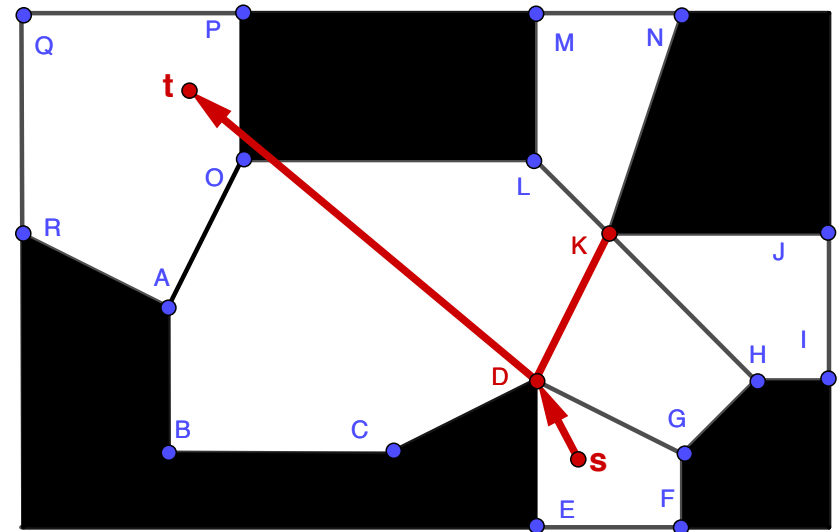


Node expansion in Polyanya. When the current node $([D,K],s)$ is expanded, it generates the observable successors $([D',L],s)$ and $([L,K],s)$; and non-observable successors $([D',O],D)$, $([O,A],D)$, $([A,B],D)$, $([B,C],D)$, and $([C,D],D)$.

- Navigation Mesh
- Polyanya [3]
 - Search Nodes:
 - Interval & Root
 - Successors:
 - Observable Successors
 - Non-observable Successors
 - Evaluation Function:
 - $f(n) = g(n) + h(n)$
 - i.e. $h(n) = d(s, D) + d(D, t)$



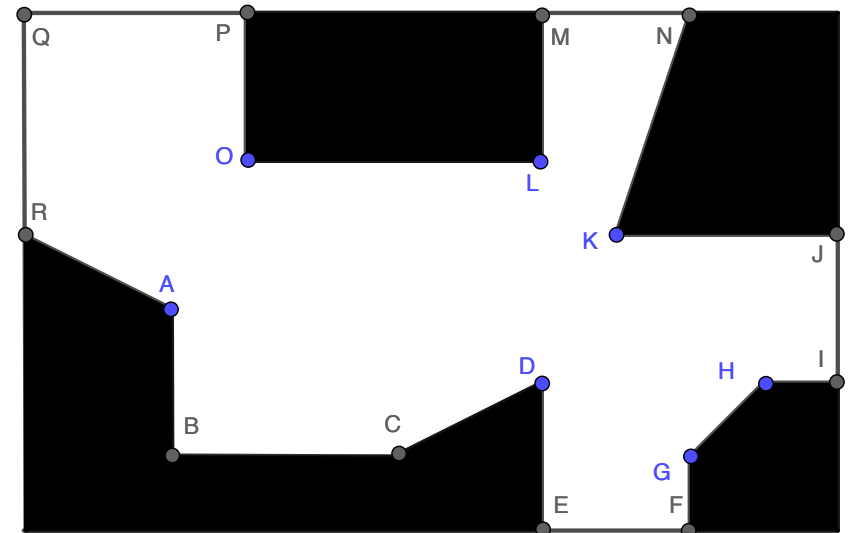
- Navigation Mesh
- Polyanya [3]
 - Search Nodes:
 - Interval & Root
 - Successors:
 - Observable Successors
 - Non-observable Successors
 - Evaluation Function:
 - $f(n) = g(n) + h(n)$
 - Pathfinding:
 - Depends on the number of polygons expanded and the number of edges on each polygon



- Euclidean-based CPD:

- First Move Table:
 - Convex vertices

Ordering	A	D	G	H	K	L	O
A	A	D	D	H	K	L	O
D	A	D	G	H	K	L	O
G	D	D	G	H	K	L	O

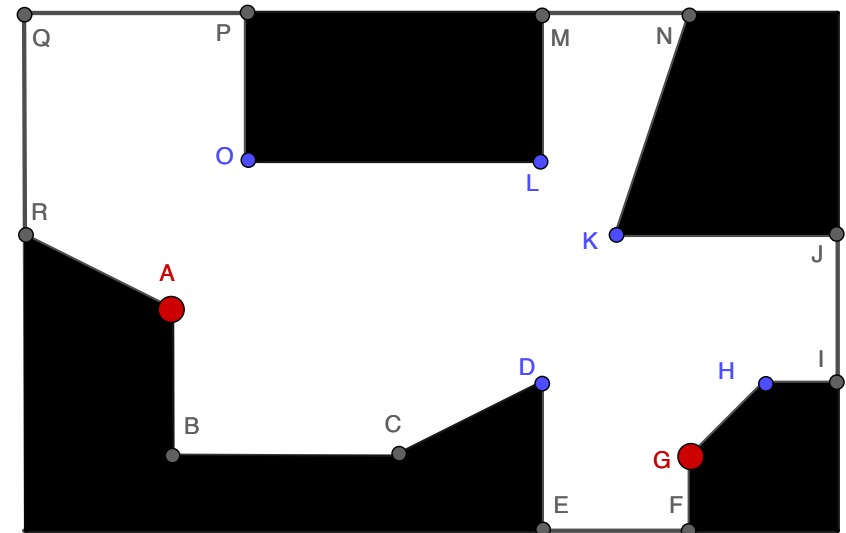


- Euclidean-based CPD:

- First Move Table:

- Convex vertices

Ordering	A	D	G	H	K	L	O
A	A	D	D	H	K	L	O
D	A	D	G	H	K	L	O
G	D	D	G	H	K	L	O

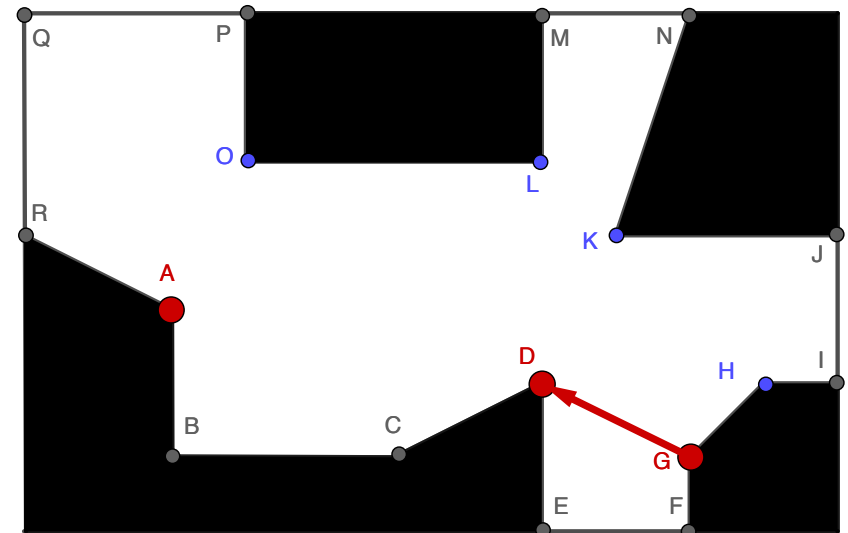


- Euclidean-based CPD:

- First Move Table:

- Convex vertices

Ordering	A	D	G	H	K	L	O
A	A	D	D	H	K	L	O
D	A	D	G	H	K	L	O
G	D	D	G	H	K	L	O

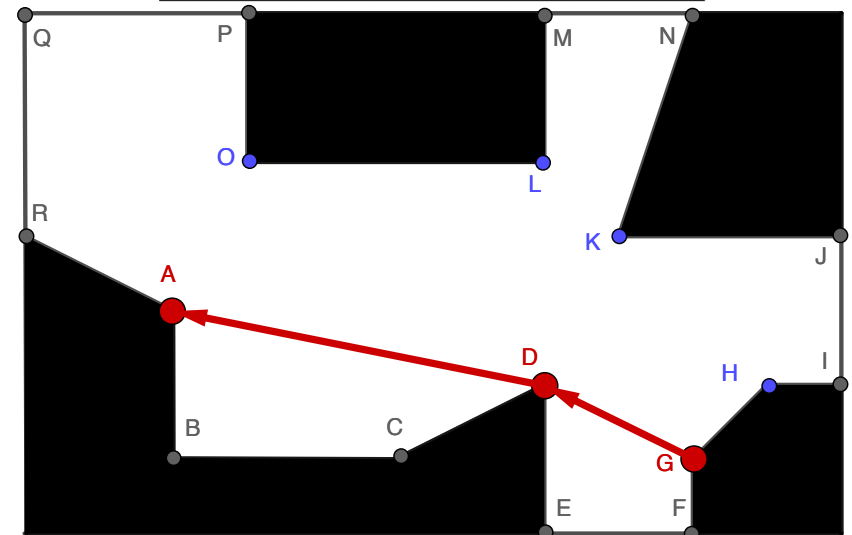


- Euclidean-based CPD:

- First Move Table:

- Convex vertices

Ordering	A	D	G	H	K	L	O
A	A	D	D	H	K	L	O
D	A	D	G	H	K	L	O
G	D	D	G	H	K	L	O



Our Approach

Compressed Path Databases (CPD) [4]

■ Euclidean-based CPD:

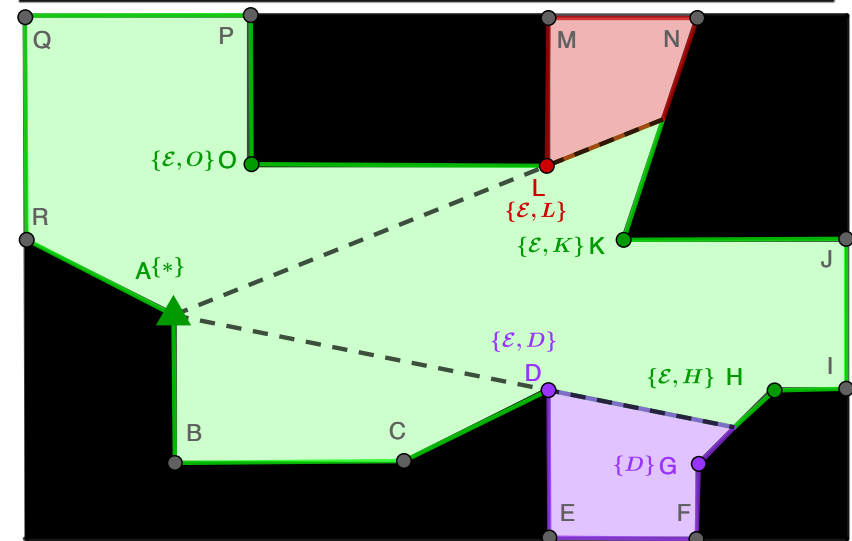
– First Move Table:

- Convex vertices

– Symbols:

- [A – R]: indicates the optimal first move

Ordering	A	D	G	H	K	L	O
A	*	$\{\mathcal{E}, D\}$	D	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
D	$\{\mathcal{E}, A\}$	*	$\{\mathcal{E}, G\}$	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
G	D	$\{\mathcal{E}, D\}$	*	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$



Green area corresponds to the area visible from the source node A. The first move on the optimal path from A to any node in the purple (resp. red) area is D (resp. L).

Our Approach

Compressed Path Databases (CPD) [4]

■ Euclidean-based CPD:

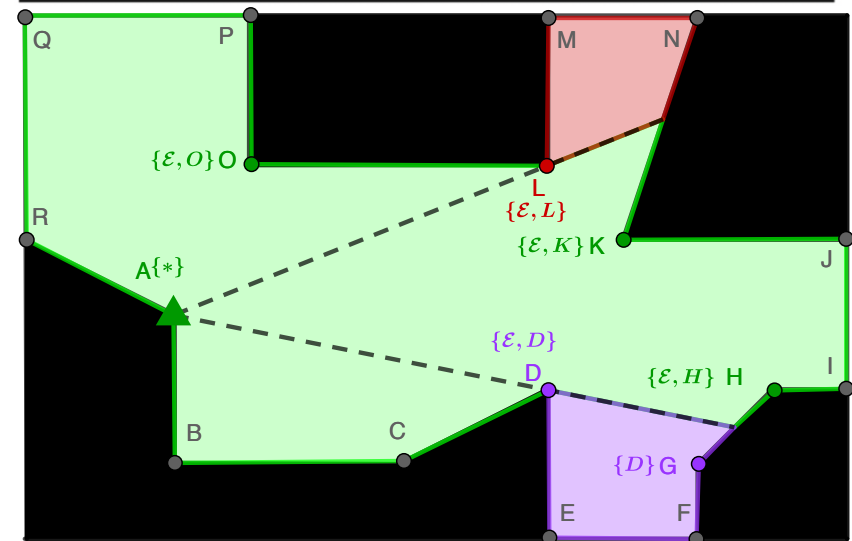
– First Move Table:

- Convex vertices

– Symbols:

- [A – R]: indicates the optimal first move
- \mathcal{E} : indicates two vertices are directly visible

Ordering	A	D	G	H	K	L	O
A	*	\mathcal{E}, D	D	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
D	$\{\mathcal{E}, A\}$	*	$\{\mathcal{E}, G\}$	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
G	D	$\{\mathcal{E}, D\}$	*	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$



Green area corresponds to the area visible from the source node A. The first move on the optimal path from A to any node in the purple (resp. red) area is D (resp. L).

Our Approach

Compressed Path Databases (CPD) [4]

■ Euclidean-based CPD:

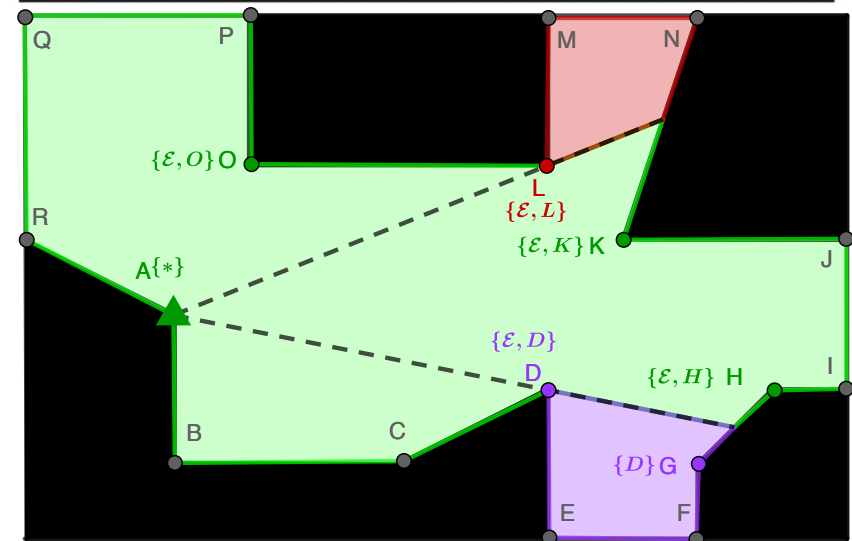
– First Move Table:

- Convex vertices

– Symbols:

- [A – R]: indicates the optimal first move
- \mathcal{E} : indicates two vertices are directly visible
- $\{\mathcal{E}, D\}$: redundant symbol [5]

Ordering	A	D	G	H	K	L	O
A	*	$\{\mathcal{E}, D\}$	D	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
D	$\{\mathcal{E}, A\}$	*	$\{\mathcal{E}, G\}$	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
G	D	$\{\mathcal{E}, D\}$	*	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$



Green area corresponds to the area visible from the source node A. The first move on the optimal path from A to any node in the purple (resp. red) area is D (resp. L).

Our Approach

Compressed Path Databases (CPD) [4]

■ Euclidean-based CPD:

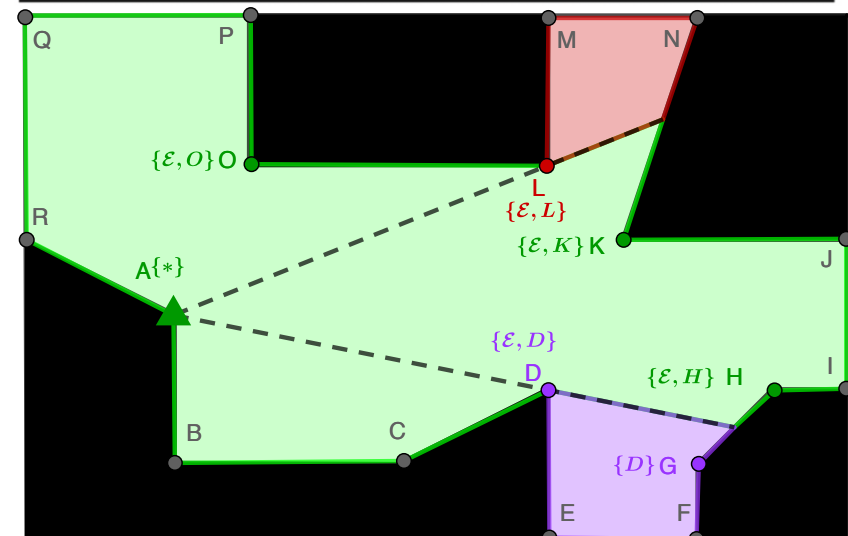
– First Move Table:

- Convex vertices

– Symbols:

- [A – R]: indicates the optimal first move
- \mathcal{E} : indicate two vertices are directly visible
- $\{\mathcal{E}, D\}$: redundant symbol [5]
- *: wildcard symbol [5]

Ordering	A	D	G	H	K	L	O
A	*	$\{\mathcal{E}, D\}$	D	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
D	$\{\mathcal{E}, A\}$	*	$\{\mathcal{E}, G\}$	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
G	D	$\{\mathcal{E}, D\}$	*	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$



Green area corresponds to the area visible from the source node A. The first move on the optimal path from A to any node in the purple (resp. red) area is D (resp. L).

Our Approach

Compressed Path Databases (CPD) [4]

■ Euclidean-based CPD:

– First Move Table:

- Convex vertices

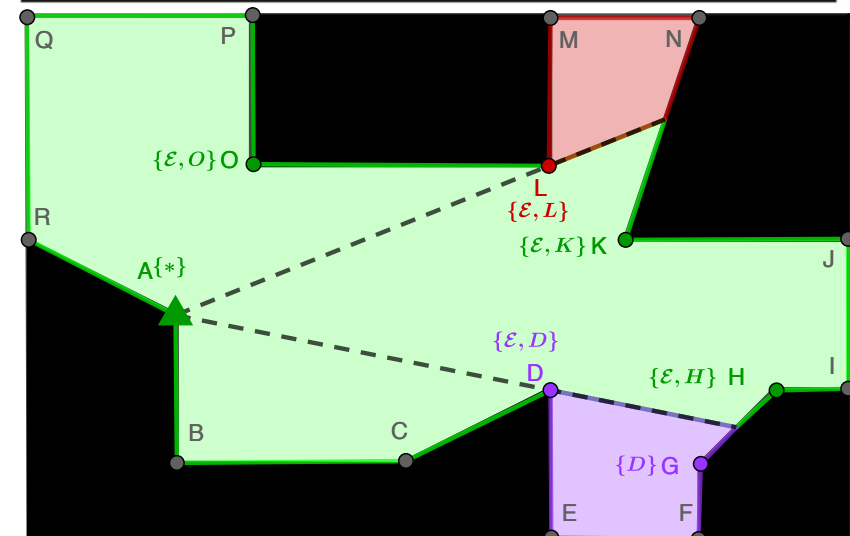
– Symbols:

- [A – R]: indicates the optimal first move
- \mathcal{E} : indicate two vertices are directly visible
- $\{\mathcal{E}, D\}$: redundant symbol [5]
- $*$: wildcard symbol [5]

– Compression:

- Depth first search ordering [4]
- Run length encoding [4]
 - (i.e. Row A: 1D; 4 \mathcal{E})

Ordering	A	D	G	H	K	L	O
A	*	$\{\mathcal{E}, D\}$	D	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
D	$\{\mathcal{E}, A\}$	*	$\{\mathcal{E}, G\}$	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$
G	D	$\{\mathcal{E}, D\}$	*	$\{\mathcal{E}, H\}$	$\{\mathcal{E}, K\}$	$\{\mathcal{E}, L\}$	$\{\mathcal{E}, O\}$



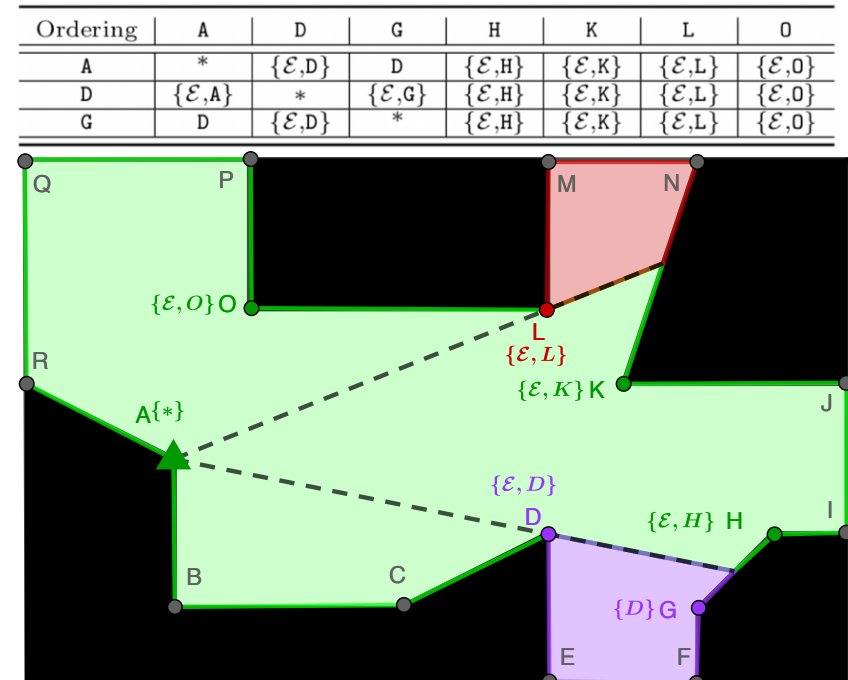
Green area corresponds to the area visible from the source node A. The first move on the optimal path from A to any node in the purple (resp. red) area is D (resp. L).

Our Approach

Compressed Path Databases (CPD) [4]

■ Euclidean-based CPD:

- First Move Table:
 - Convex vertices
- Symbols:
 - [A – R]: indicates the optimal first move
 - \mathcal{E} : indicate two vertices are directly visible
 - $\{\mathcal{E}, D\}$: redundant symbol [5]
 - $*$: wildcard Symbol [5]
- Compression:
 - Depth first search ordering [4]
 - Run length encoding [4]
- First Move Extraction:
 - A simple binary search

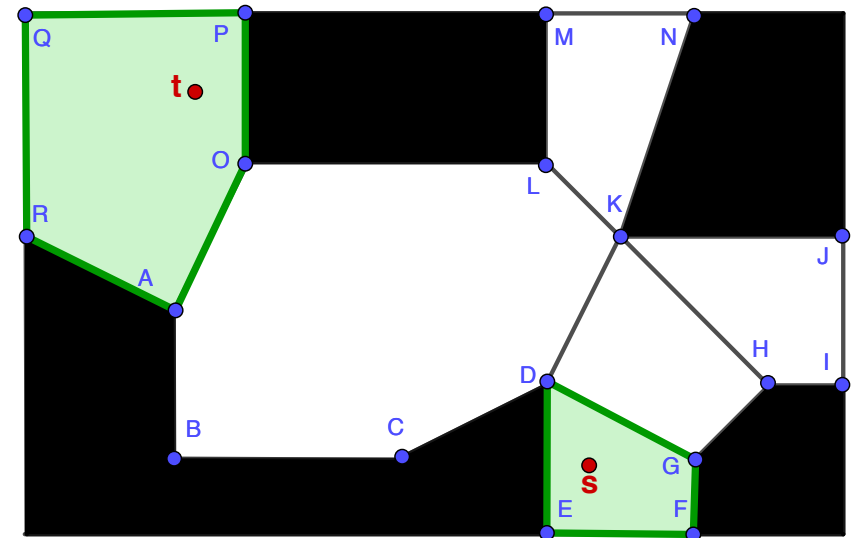


Green area corresponds to the area visible from the source node A. The first move on the optimal path from A to any node in the purple (resp. red) area is D (resp. L).

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)

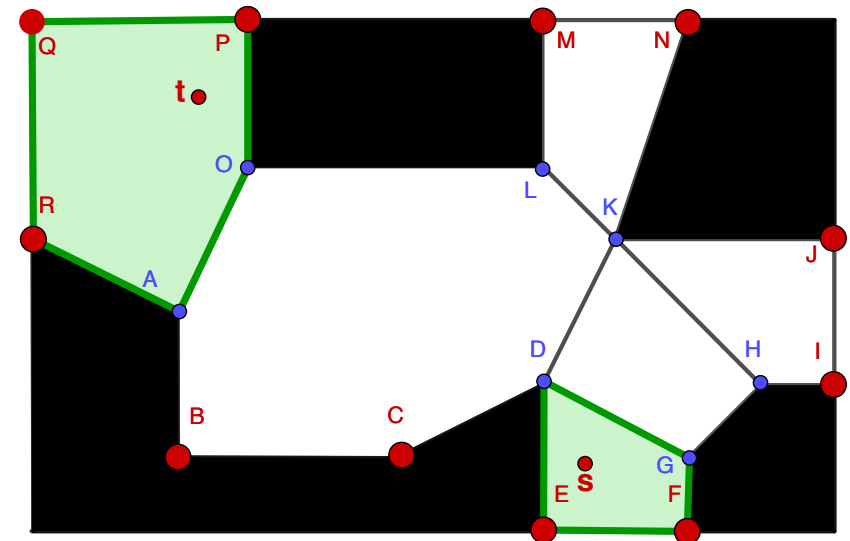


Shaded green area shows the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices

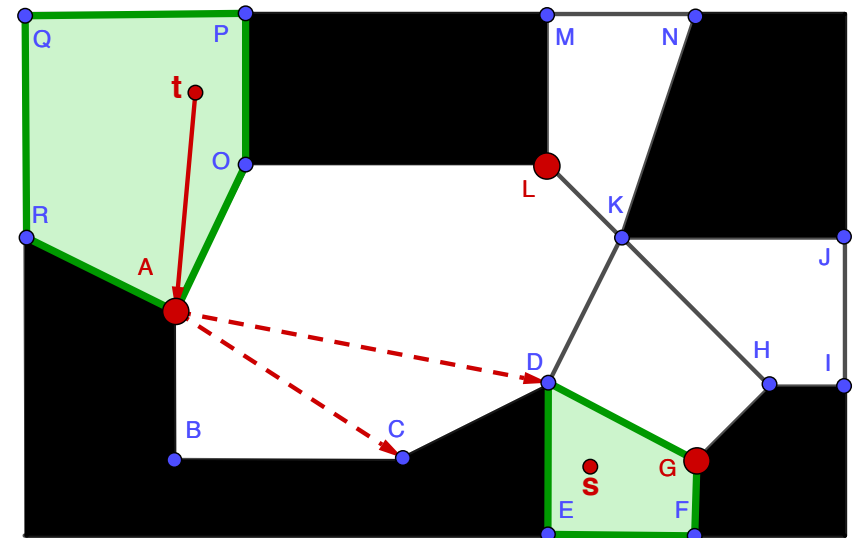


Avoid accessing the non-convex visible vertices

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices

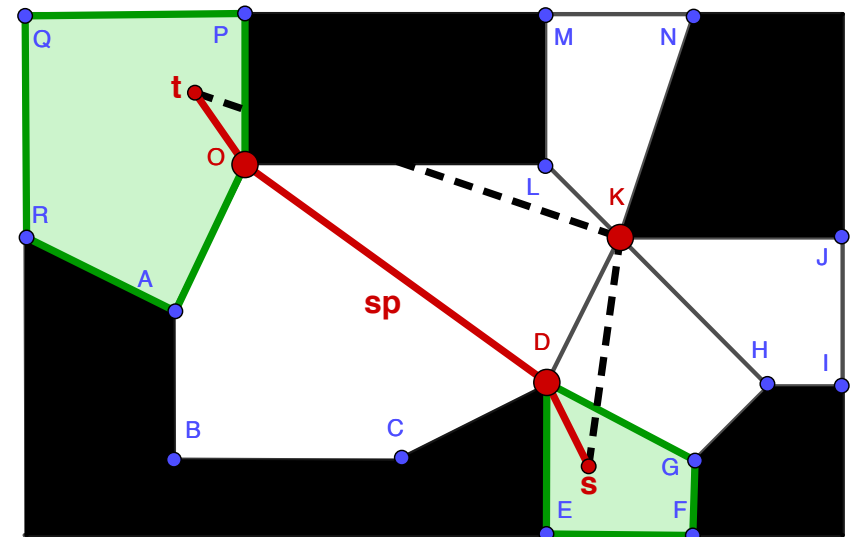


Avoid accessing the visible vertices can not possibly turn

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance Pruning
$$d(s, K) + h(K, t) > |sp|$$



Avoid accessing the visible vertices that can be pruned based on the current solution

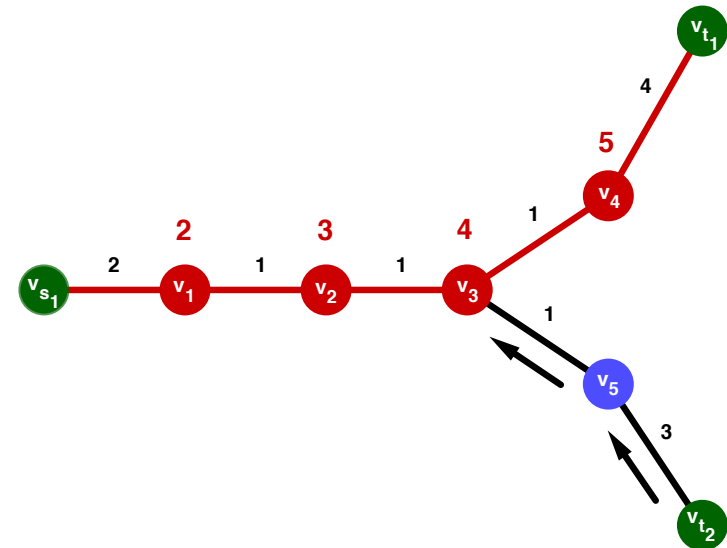
-

28

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching

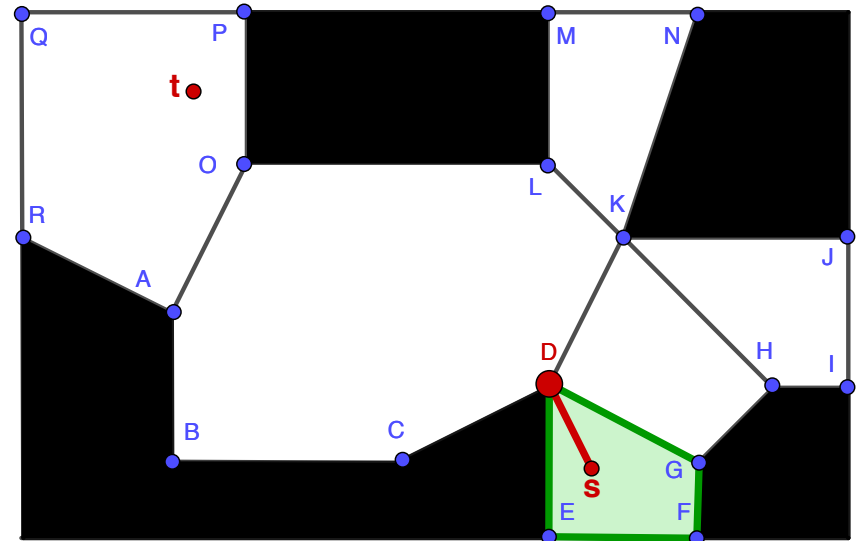


EPS cache distance on each node when extract paths from V_{t1} to V_{s1} . The path extraction from V_{t2} to V_{s1} terminate when reach a cached node (i.e. V_3)

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

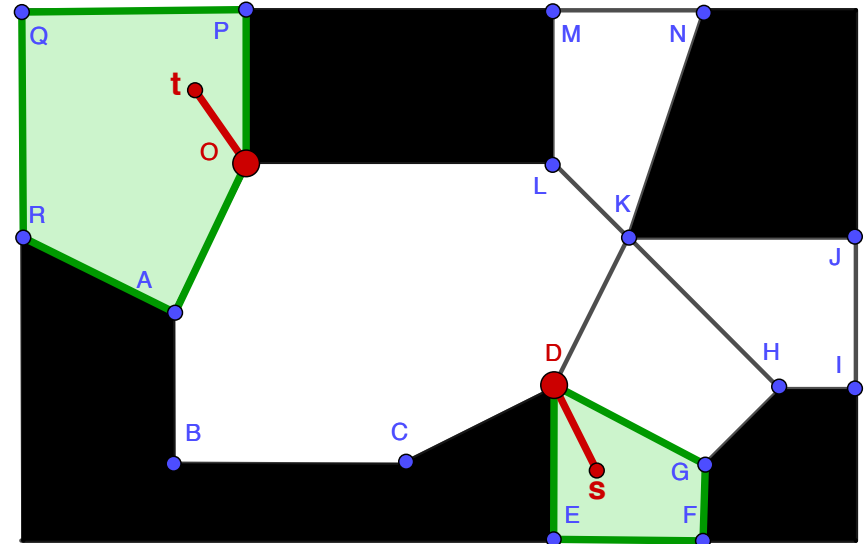


The shaded green area shows the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

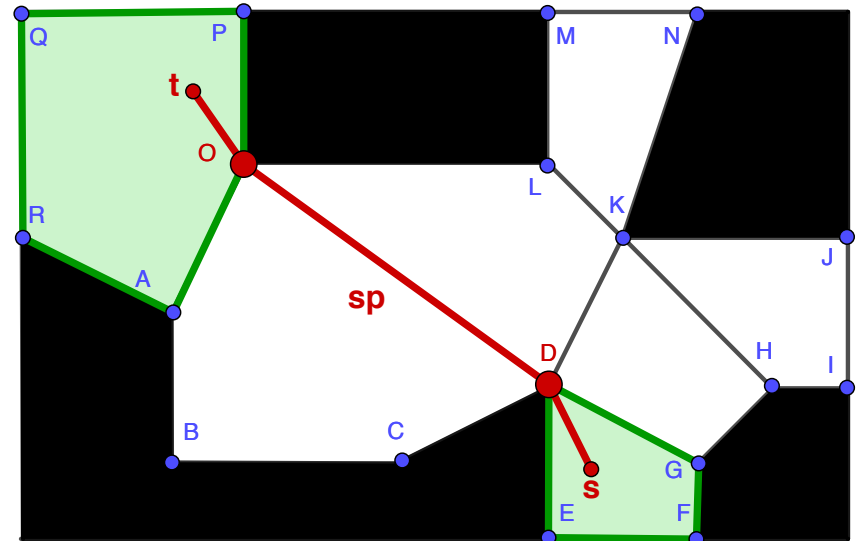


The shaded green areas show the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

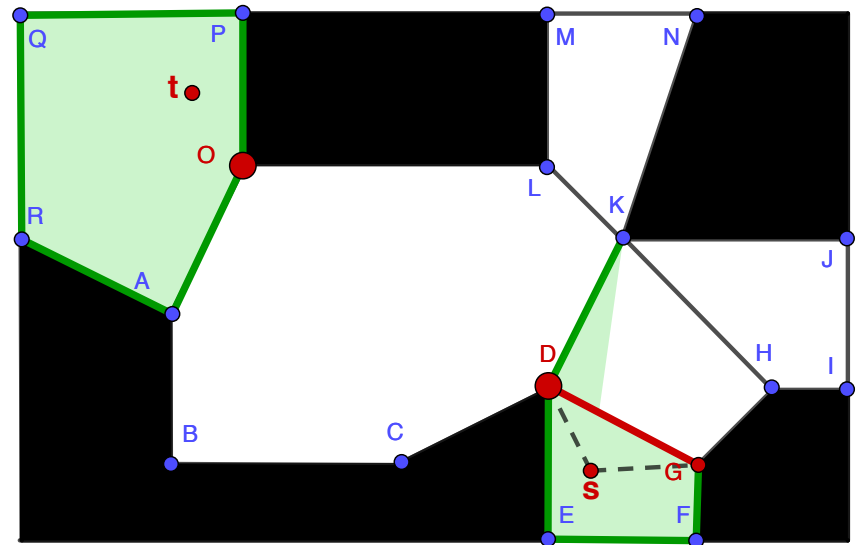


The shaded green areas show the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

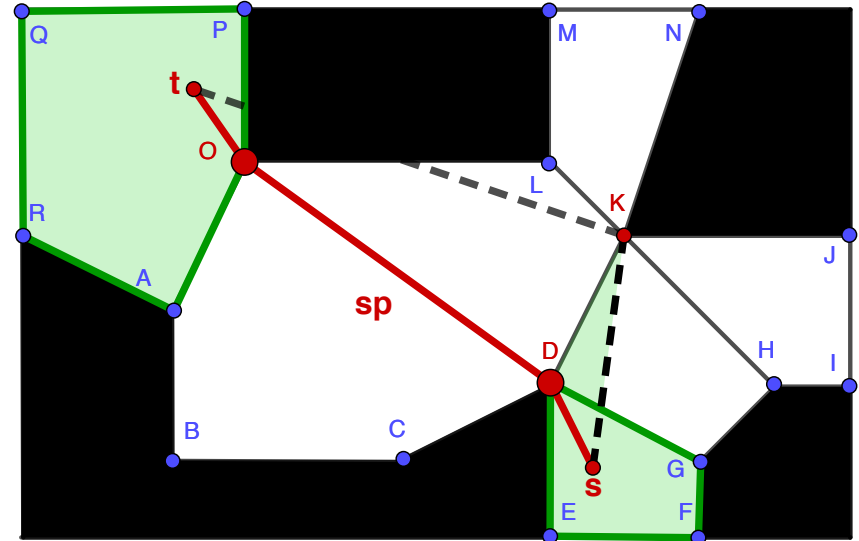


The shaded green areas show the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

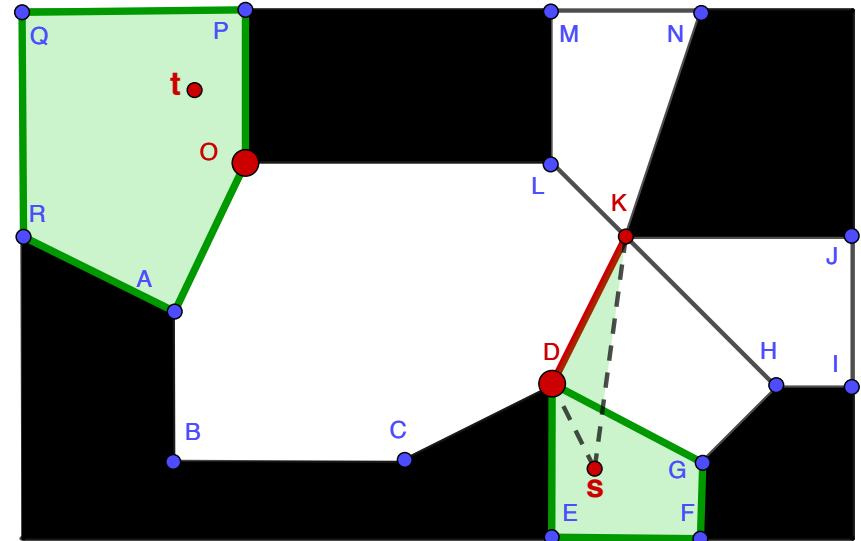


The shaded green areas show the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

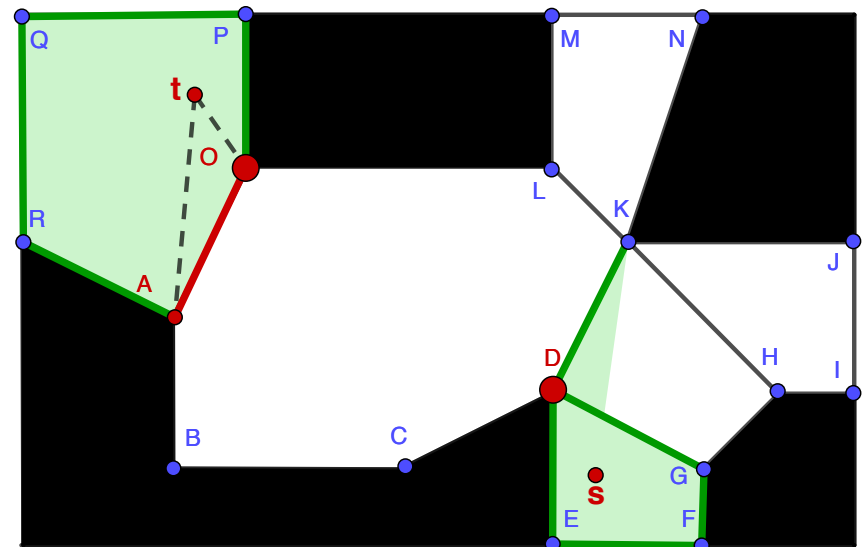


The shaded green areas show the space incrementally explored by search_s and search_t

Our Approach

End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example

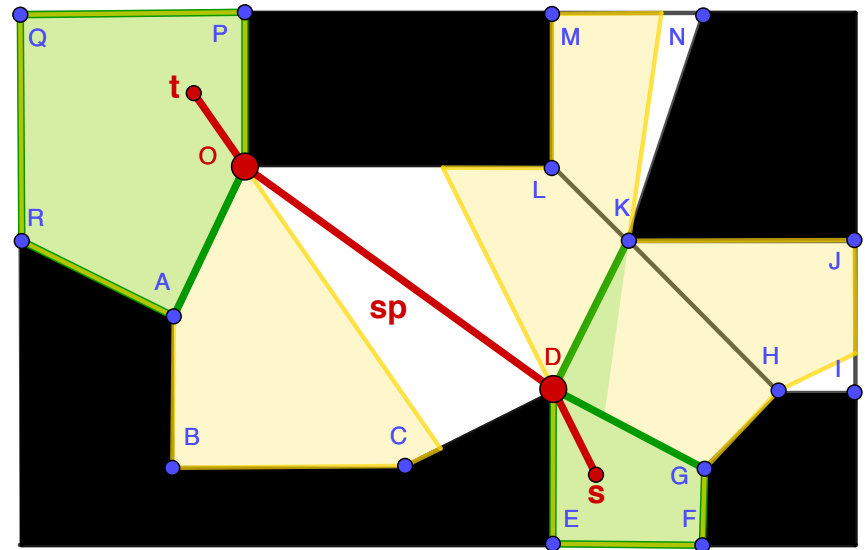


Shaded green areas show the space incrementally explored by search_s and search_t

Our Approach

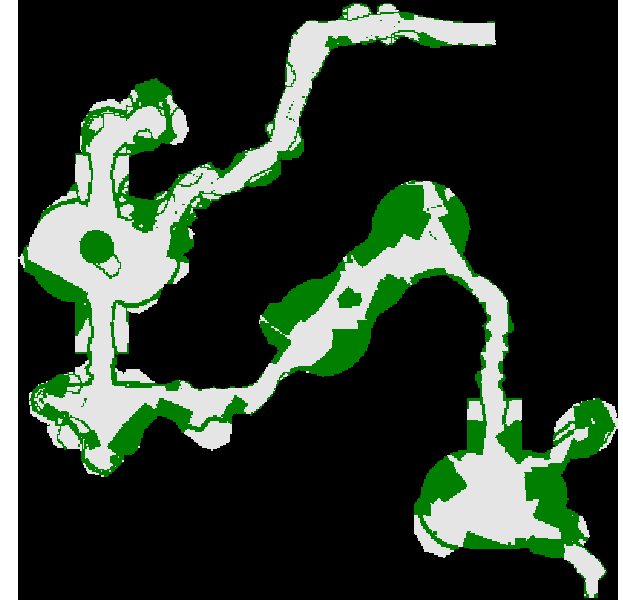
End Point Search (EPS)

- Euclidean-based CPD
- End Point Search (EPS)
 - Incremental Insertion
 - Search_s & Search_t
 - V_s & V_t
 - Shortest Path (sp)
 - Vertex Pruning
 - Dead-end Vertices
 - Non-turn Vertices
 - Distance-based Pruning
 - Path Pruning
 - Non-taut Paths
 - Cost Caching
 - Running Example



Shaded yellow areas correspond to the area visible from s and t. Shaded green areas show the space incrementally explored by Polyanya when search_s and search_t are both exhausted

- Euclidean-based CPD
- End Point Search (EPS)
- Experimental Results
 - Benchmarks:
 - Game Maps from [Sturtevant's Repository](#)



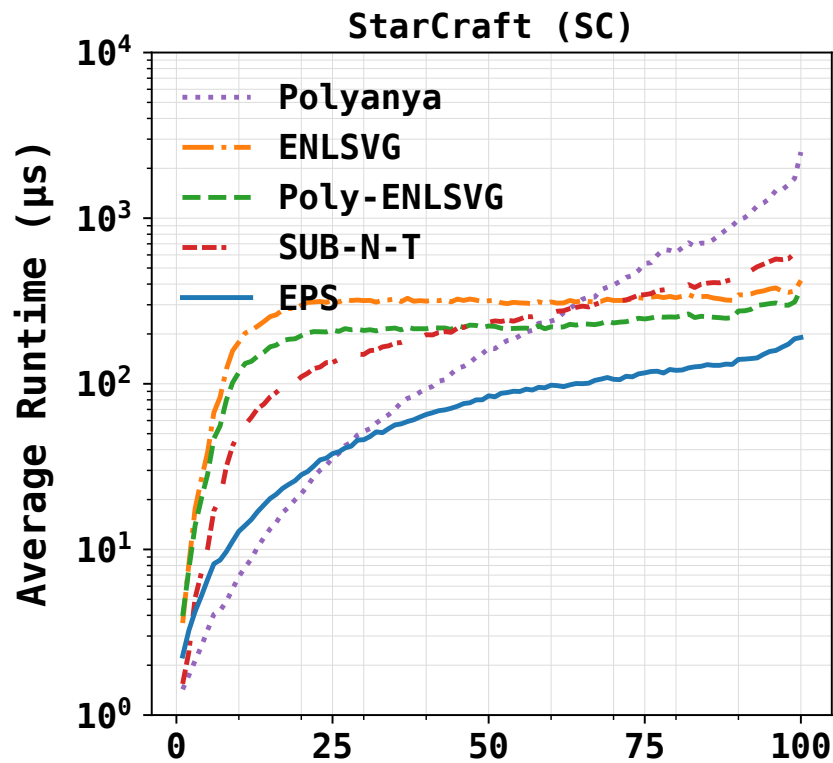
Euclidean-based CPD Statistics

	#Map	#Queries	Build Time		Raw Memory		CPD Memory	
			Avg	Max	Avg	Max	Avg	Max
SC	75	198k	0.7	8	190	2202	2	14

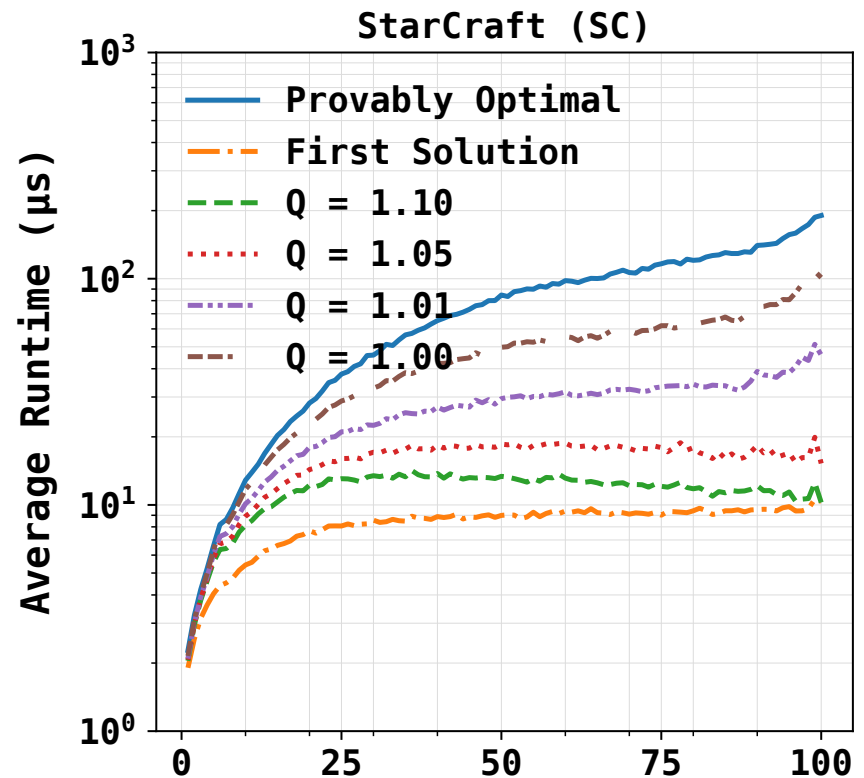
Our Approach

Experimental Results

■ Optimal Search



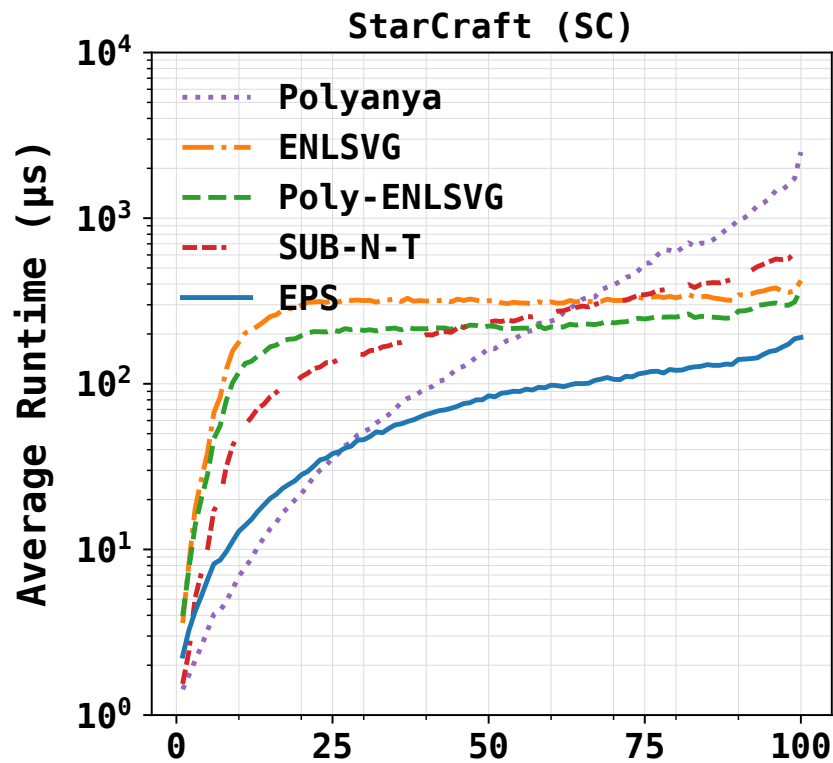
■ Any-time Search



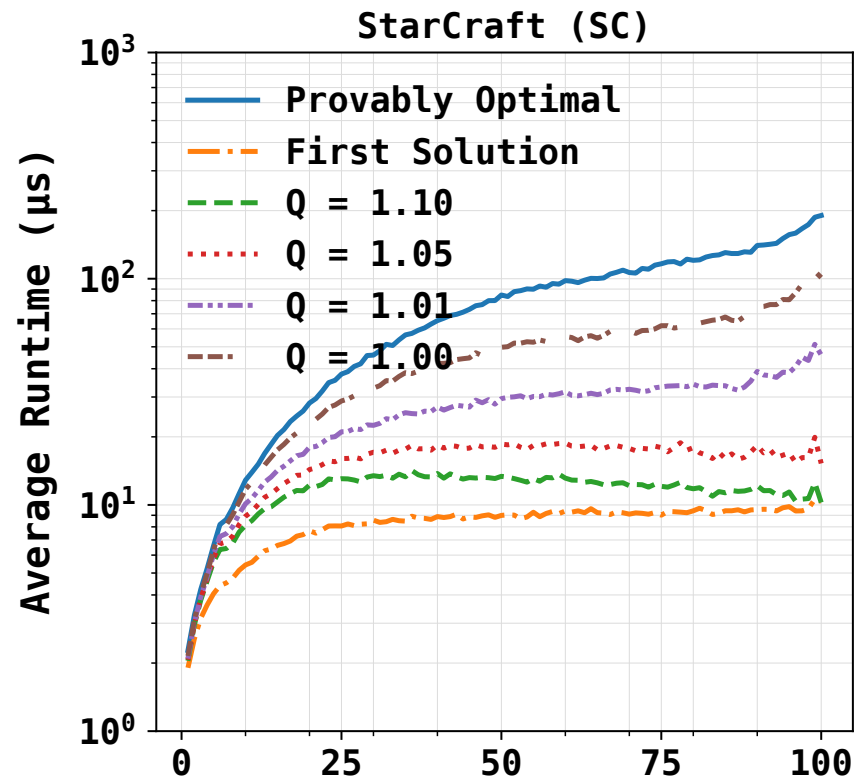
Our Approach

Experimental Results

■ Optimal Search



■ Any-time Search



- [1] T. Lozano-Perez, M. A. Wesley, An algorithm for planning collision-free paths among polyhedral obstacles, *Commun. ACM* 22 (10) (1979) 560-570.
- [2] S. Oh, H. W. Leong, Edge n-level sparse visibility graphs: Fast optimal any-angle pathfinding using hierarchical taut paths, in: *Proceedings of the Tenth International Symposium on Combinatorial Search, SOCS 2017, 16-17 June 2017, Pittsburgh, Pennsylvania, USA, AAAI Press, 2017*, pp. 64-72.
- [3] M. Cui, D. D. Harabor, A. Grastien, Compromise-free pathfinding on a navigation mesh, in: *Proceedings of the Twenty-Sixth International Joint Conference on Artificial Intelligence, IJCAI 2017, Melbourne, Australia, August 19-25, 2017, ijcai.org, 2017*, pp. 496–502.
- [4] B. Strasser, D. Harabor, A. Botea, Fast first-move queries through run-length encoding, in: *Proceedings of the Seventh Annual Symposium on Combinatorial Search, SOCS 2014, Prague, Czech Republic, 15-17 August 2014, AAAI Press, 2014*.
- [5] M. Chiari, S. Zhao, A. Botea, A. E. Gerevini, D. Harabor, A. Saetti, M. Salvetti, P. J. Stuckey, Cutting the size of compressed path databases with wildcards and redundant symbols, in: *Proceedings of the Twenty-Ninth International Conference on Automated Planning and Scheduling, ICAPS 2018, Berkeley, CA, USA, July 11-15, 2019, AAAI Press, 2019*, pp. 106–113.

Thank you for listening