Remann Sums => approx. area under curve. => For some function of x, y=fG)  $W = \Delta X = 22 - 2$ h = y = f(x)xi E {x,...xu} n= stal# bony. · Divide x into bins, Ax= 2x-2, · Pick some x; Yw x, xx: x, < x; < x, < x, < x, =x · Height xwidth hi ax for each xi approx. I area under curve for [x; tsz] where hi is height at xi Now, total area under curve is approximated by:  $F(x) \stackrel{\sim}{=} \stackrel{\sim}{=} f(x_i) \stackrel{\sim}{\leq} x$  i=1  $f(x_i) \stackrel{\sim}{\leq} x \stackrel{\sim}{=} x$   $f(x_i) \cdot sx \stackrel{\sim}{=} hi \cdot w$ The integral is the limit over as \$x get smaller & smaller  $F(x) = \lim_{\Delta x \to 0} \sum_{x \to 0} F(x) dx = \int_{x \to 0}^{x} f(x) dx \qquad \text{[triblimite material]}$ -> Definite Integral · the area under curve spanning interval (a, 6] from x=a to  $\int_{0}^{6} f(x) dx = F(x) \Big|_{0}^{6} = F(6) - F(a) = \int_{0}^{6} f(x) dx - \int_{0}^{6} f(x) dx$ 

PBF & CBF: f(x) & F(x)

· For probability distributions, total over is by definition = 1.

• 
$$f(x) = \text{height at} x$$
  
•  $x \in X = \{x_1, ..., x_n\}$ 

Continuous : 
$$\int_{-\infty}^{\infty} f(x) dx = 1$$

· Total publishing that X=x is (lower-tail)

Discrete => 
$$F(x) = P(x \le x) = \sum_{x_i \le x} f(x_i)$$

Continuous => 
$$F(x) = P(x \le x) = \int_{-\infty}^{x} f(t) dt$$
 (t'y a variable finternation)

Discrete distributions

· Fotal mose that 
$$a \le X \le 6$$

$$\Pr(\chi_n < \chi \le \chi_n) = \sum_{\chi_i = \chi_n + 1} \chi_i = \chi_n + 1$$

. Note that Xi ranges from Kat to X & & X X

· To get when al w/a molive we F(x) - F(x, )  $=P(\chi_n \leq \chi \leq \chi_i)$ 

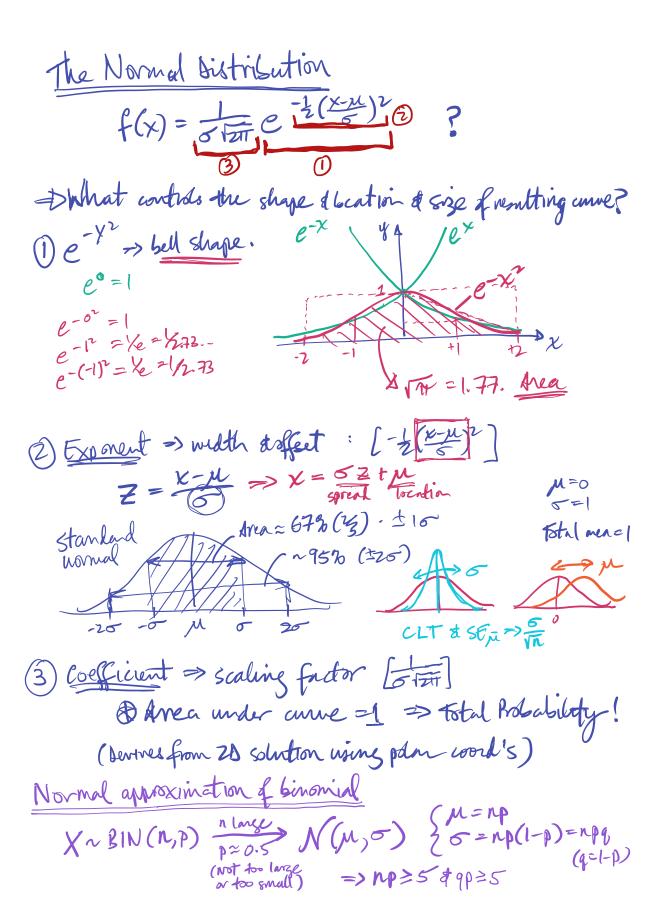
Continuous Dustin Lutions

· Total pub xxx = x6

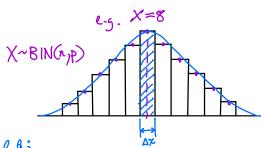
$$P_r(a < x \leq b) = \int_{a}^{b} f(x) dx = F \Big|_{\infty}^{b} - F \Big|_{\infty}^{c} = F(x_b) - F(x_r)$$

$$= P(\chi_{a} \leq \chi \leq \chi_{b})$$

Aren =  $P(x_0 \le x \le x_b)$  p = p  $y_0 = x_0$ 



· To approximate a discrete distribution with a continuous one, we need to compute the area under a curve across a range of values (since the area under a single point is 0):



Binomial distribution for  $\begin{cases} n=16 \\ p=0.5 \end{cases}$  M = Exp(x) = np = 8 $\sigma = np(1-p) = 16.0.5^2 = 4 = 3 sd. = 2$ 

In order to compute Pr[X=8] using the normal approx, we need to get the area under a normal curve across an interval that spans X=8, and is adjacent to X=7 & X=9. The width of JX=1, so we need to get Pr[8-0.5 < X < 8+0.5] = Pr[7.5 < X < 8.5].

More generally, we need to follow these rules:

## Binomial (discrete). P(X=X) P(X=X) P(X=X) P(X=X) P(X=X) P(X=X) P(X=X)

Normal (continuous)  $P(x-0.5 \le X < X+0.5)$   $P(X \le x+0.5) \times \text{inclusive}$   $P(X \ge X-0.5) \times \text{exclusive}$   $P(X > X-0.5) \times \text{inclusive}$   $P(X > X+0.5) \times \text{inclusive}$