Math 151 – Python Lab 7

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0.1 MATH 151 Lab 7

Section Number: 568

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```
[1]: from sympy import *
from sympy.plotting import (plot, plot_parametric)
```

0.1.1 Question 1

[2]: # piece wise function

→{points}.')

1a

The critical values for f(x) = Piecewise((8 - x**2, x < 0), (x + 5*exp(-(x/2 - 1)**2), True)) are x = [0, 2.41784619385985, 4.78643377270907]. The points are [(0, 8 - x**2), (2.41784619385985, x + 5*exp(-(x/2 - 1)**2)), (4.78643377270907, x + 5*exp(-(x/2 - 1)**2))].

print(f'The critical values for $f(x) = \{p\}$ are $x = \{critical\}$. The points are

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1b
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[3]: # find the absolute extrema of the function on the interval [-5, 5]
maxin_candidates = [-5, 5] + critical
yvals = [p.subs(x, i) for i in maxin_candidates]
maxy = max(yvals)
miny = min(yvals)
maxx = maxin_candidates[yvals.index(maxy)]
minx = maxin_candidates[yvals.index(miny)]
print(f'The absolute extrema of f(x) = {p} on the interval [-5, 5] are y = \( \triangle \) {maxy} and y = {miny}. The points are ({maxx}, {maxy}) and ({minx}, {miny}).
```

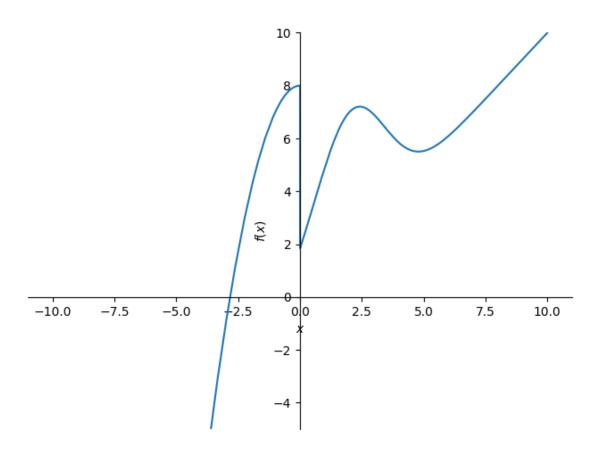
The absolute extrema of f(x) = Piecewise((8 - x**2, x < 0), (x + 5*exp(-(x/2 - 1)**2), True)) on the interval [-5, 5] are y = 7.20429639824017 and y = -17. The points are (2.41784619385985, 7.20429639824017) and (-5, -17).

1c

The absolute extrema of f(x) = Piecewise((8 - x**2, x < 0), (x + 5*exp(-(x/2 - 1)**2), True)) on the interval [-10, 10] are y = 5*exp(-16) + 10 and y = -92. The points are (10, 5*exp(-16) + 10) and (-10, -92).

1d

```
[5]: # plot the function on the interval [-10, 10]
main_plot = plot(p, (x, -10, 10), ylim=(-5, 10))
print(f'The plot of f(x) = {p} on the interval [-10, 10] is shown above.')
```



The plot of f(x) = Piecewise((8 - x**2, x < 0), (x + 5*exp(-(x/2 - 1)**2), True)) on the interval [-10, 10] is shown above.

0.1.2 Question 2

2a

```
[6]: # v(r) = k (r_o - r) * r ** 2
# find the value of r in the interval [1/2 r_o, r_o]
# where v has an absolute maximum
k, r, r_o = symbols('k r r_o')
v = k * (r_o - r) * r ** 2
v_prime = diff(v, r)
r_crit = solve(v_prime, r)[1]
print(f'The absolute maximum of v(r) = {v} is at r = {r_crit}.')
```

The absolute maximum of $v(r) = k*r**2*(-r + r_o)$ is at $r = 2*r_o/3$.

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2b

v_max = v.subs(r, r_crit)

point = (r_crit, v_max)
```

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print(f'The absolute max of v(r) = {v} is {v_max} at r = {r_crit}. The point is_ \hookrightarrow {point}.')
```

The absolute max of $v(r) = k*r**2*(-r + r_o)$ is $4*k*r_o**3/27$ at $r = 2*r_o/3$. The point is $(2*r_o/3, 4*k*r_o**3/27)$.

2c

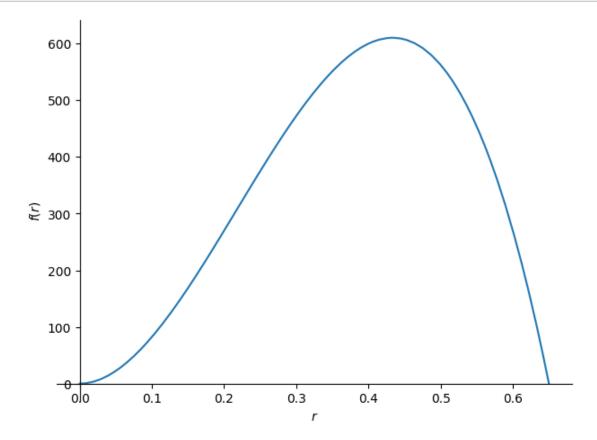
The absolute max of $v(r) = k*r**2*(-r + r_o)$ is 610.27777777778 at $r = 2*r_o/3$. The point is (0.433333333333333, 610.2777777778).

2d

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[9]: # sketch the graph of v with the conditions from part c on the interval [0, r_o] v_plot = plot(v.subs(subs[1:]), (r, 0, 0.65))

print(f'The plot of v(r) = {v.subs(subs[1:])} on the interval [0, r_o] is shown

above.')
```



The plot of v(r) = 15000*r**2*(0.65 - r) on the interval $[0, r_o]$ is shown above.

0.1.3 Question 3

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3a
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```
[10]: x = Symbol('x')

f = atan(x)

g = acot(x)

f_prime = diff(f, x)

g_prime = diff(g, x)

f_g_prime = f_prime + g_prime

print(f"The derivative of [f(x) + g(x)] is f'(x) + g'(x) if we apply the sum_{\square}
\Rightarrow rule. f(x) = \{f\} \text{ and } g(x) = \{g\}. f'(x) = \{f_prime\} \text{ and } g'(x) = \{g_prime\}._{\square}
\Rightarrow Therefore, f'(x) + g'(x) = \{f_g_prime\}._{\square}
```

The derivative of [f(x) + g(x)] is f'(x) + g'(x) if we apply the sum rule. f(x) = atan(x) and g(x) = acot(x). f'(x) = 1/(x**2 + 1) and g'(x) = -1/(x**2 + 1). Therefore, f'(x) + g'(x) = 0.

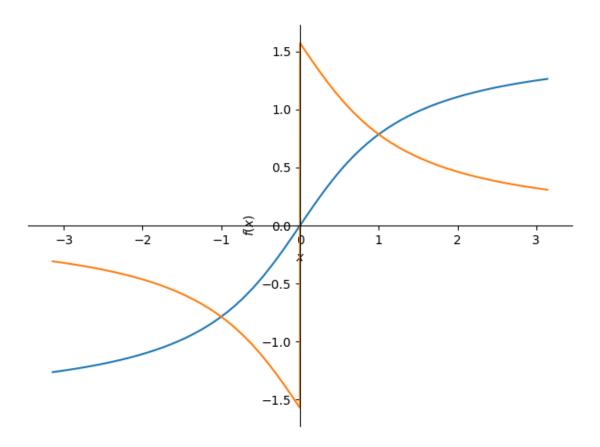
3b

[11]: print(f'Since the derivative of f(x) + g(x) is 0 we can conclude that f(x) + g(x) is a constant function or we cannot take the derivative of the function.

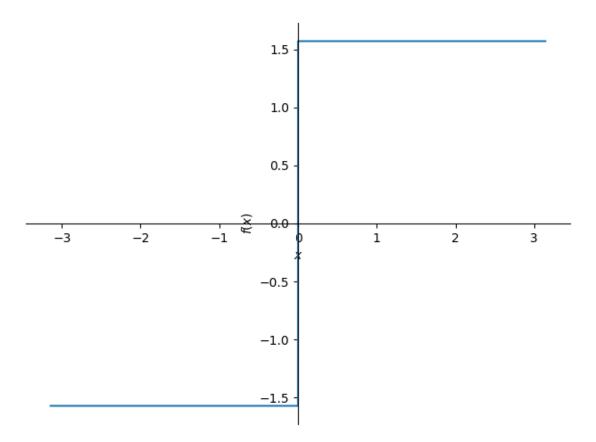
Since the derivative of f(x) + g(x) is 0 we can conclude that f(x) + g(x) is a constant function or we cannot take the derivative of the function.

```
3c
```

```
[12]: f_plot = plot(f, (x, -pi, pi), show=False)
g_plot = plot(g, (x, -pi, pi), show=False)
f_plot.extend(g_plot)
f_plot.show()
print((atan(x)+acot(x)).simplify())
print(f'The graph shows f(x) = {f} in blue and g(x) = {g} in orange.')
f_g_plot = plot(atan(x)+acot(x), (x, -pi, pi))
print(f'The graph above shows f(x) + g(x) = {f + g} in blue.')
print(f'This graph above shows that the left side of the graph is a constant
negative value and the right side is a constant positive value.')
```



acot(x) + atan(x)The graph shows f(x) = atan(x) in blue and g(x) = acot(x) in orange.



The graph above shows f(x) + g(x) = acot(x) + atan(x) in blue. This graph above shows that the left side of the graph is a constant negative value and the right side is a constant positive value.

3d

[13]: print(f'It makes sense that the graph of f(x) + g(x) would look like this since the graph of $f(x) = \{f\}$ is a reflection of the graph of $g(x) = \{g\}$ over the f(x) + g(x) is the sum of the two graphs.')

It makes sense that the graph of f(x) + g(x) would look like this since the graph of f(x) = atan(x) is a reflection of the graph of g(x) = acot(x) over the x-axis. The graph of f(x) + g(x) is the sum of the two graphs.