Certifying Digital Rights' Expression Languages

by

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Abstract

This is the abstract.

Acknowledgements

I would like to thank all the little people who made this possible.

Dedication

This is dedicated to the one I love.

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Chapter 1

Introduction

Digital rights management, *DRM*, refers to the digital management of rights associated with the access or usage of digital assets. There are various aspects of rights management however. According to the authors of the whitepaper "A digital rights management ecosystem model for the education community," digital rights management systems cover the following four areas: 1) defining rights 2) distributing/acquiring rights 3) enforcing rights and 4) tracking usage [1].

Rights Expression Languages, *RELs*, or more precisely when dealing with digital assets, Digital Rights Expression Languages *DRELs* deal with the "rights definition" aspect of the DRM ecosystem. A DREL, allows the expression and definition of digital asset usage rights such that other areas of the DRM ecosystem namely the enforcement mechanism and the usage tracking components can function correctly.

Currently the most popular RELs are the eXtensible rights Markup Language, *XrML* [bib], and the Open Digital Rights Language, *ODRL* [bib]. Both of these languages are XML based and are considered declarative languages. XrML has been selected to be the REL for *MPEG-21* which is an ISO standard for multimedia applications. ODRL is also a standards based REL which has been accepted as part of the W3C community with the mandate of standardizing how rights and policies, related to the usage of digital content on the Open Web Platform, *OWP*, are expressed [wikipedia]. ODRL 2.0 supports expression of rights and also privacy rules for social media while ODRL 1.0 was only dealing with the mobile ecosystem – ODRL 1.0 was adopted by the Open Mobile Alliance, *OMA* in 2000.

As popular as both XrML and ODRL are, their adoption and usage is still somewhat limited in practice. Both Apple and Microsoft for example have defined their own lightweight RELs [problem with RELs paper] in *Fair Play* (Apple) and in *PlayReady* (Microsoft). The authors of [the problem with RELs] argue that both these RELs and other ones are simply too complex to be used effectively since they try to cover much of the DRM ecosystem.

Another issue with the current batch of RELs are due to their semantics being expressed in a natural language (e.g. English). By necessity natural languages are ambiguous and open to interpretation.

To formalize the semantics of RELS several approaches have been attempted by various authors. The main categories are logic based, operational semantics based interpreters and finally web ontology based (from the Knowledge Representation Field). In this thesis we will focus on the logic based approach to formalizing semantics and will study a specific logic based language that is a translation from a subset of ODRL.

Chapter 2

Middle

2.1 Logic Based Semantics for ODRL

Formal logic can represent the statements and facts we express in a natural language like English. Propositional logic is expressive enough to express simple facts as propositions and uses connectives to allow for the negation, conjunction and disjunction of the facts. However propositional logic is not expressive enough to express policies of the kind used in languages like ODRL and XrML. For example, a simple policy expressed in English like "All who pay 5 dollars can watch the movie Toy Story" cannot be expressed in propositional logic because the concept of variables doesn't exist in propositional logic.

A richer logic called "Predicate Logic" or "First Order Logic" (*FOL*) is more suitable and has the expressive power to represent policies written in English. Moreover, FOL can be used to capture the meaning of policies in an unambiguous way.

Halpern and Weissman [Using First Order Logic to Reason about Policies] propose a fragment of FOL to represent and reason about policies. The fragment of FOL they arrive at is called *Lithium* which is decidable and allows for efficiently answering interesting queries. Lithium restricts policies to be written based on the concept of "bipolarity" which disallows by construction policies that both permit and deny an action on an object.

2.2 Pucella 2006

Pucella and Weissman [2] specify a predicate logic based based language that represents a subset of ODRL.

2.3 what will I do?

2.3.1 Coq

âĂć Program correctness âĂć Formal verification of software âĂć Certified programs âĂć Proof assistant âĂć Interactive and mechanized theorem proving âĂć Examples of machine assisted proofs: CompCert, four-color theorem proof âĂć Coq is based on a higher-order functional programming language âĂć Dependent Types âŮŃ Subset types âŮŃ Easier than writing explicit proofs âĂć Write formal specification and proofs that programs comply to their specification (a-short-intro-to-coq) âĂć Automatically extract code from specifications as Ocaml or Haskell (a-short-intro) âĂć Properties, programs and proofs are all formalized in the same language called CIC (Calculus of inductive Constructions). (a-short-intro) âĂć Coq uses a sort called Prop for propositions âĂć Coq art: âĂć Well-formed propositions are assertions one can express about values such as mathematical objects or even programs e.g. $3 < 8$ âŮŃ Note that assertions may be true, false or simply conjectures âŮŃ An assertion is only true in general if a proof is provided âŮŃ However hand written proofs are difficult to verify âŮŃ Coq provides an environment for developing proofs including a formal language to express proofs in, the language itself being built using proof theory making it possible to step by step verification of the proofs âŮŃ Mechanized proof verification requires a "proof" that the verification algorithm is correct itself in applying all the formal rules correctly

2.4 Abstract Syntax

Authors of [2] use abstract syntax instead of XML to express statements in the ODRL language. The abstract syntax used is a more compact representation than XML based language ODRL policies are written in and furthermore it simplifies specifying the semantics as we shall see. As an example here is an agreement written in ODRL and the comparable agreement expressed in the abstract syntax [2].

Listing 2.1: agreement for Mary Smith in XML

```
<agreement>
 <asset> <context> <uid> Treasure Island </uid> </context> </
    asset>
 <permission>
   <display>
    <constraint>
     <cpu> <context> <uid> Mary's computer </uid> </context> <
        /cpu>
    </constraint>
   </display>
   <print>
    <constraint> <count> 2 </count> </constraint>
```

```
   </print>
  <requirement>
   <prepay>
    <payment> <amount currency="AUD"> 5.00</amount> </payment>
   </prepay>
  </requirement>
 </permission>
 <party> <context> <name> Mary Smith </name> </context> </
    party>
</agreement>
```

The agreement 2.1 is shown below using the syntax from [2].

Listing 2.2: agreement for Mary Smith as BNF (as used in [2])

```
agreement
 for Mary Smith
 about Treasure Island
 with prePay[5.00] -> and[cpu[Mary's Computer] => display,
                          count[2] => print].
```

In the following we will cover the *abstract syntax* of a subset of ODRL expressed as Coq's constructs such as *Inductive Types* and Definitions. We will call this subset *ODRL0* both because it is a variation of Pucella's ODRL language and also because it is missing some constructs from Pucella's ODRL.

2.4.1 Odrl0

In ODRL0, agreements and facts (i.e. environments) will only contain the number of times each policy has been used to justify an action. In ODRL0 agreements and facts will not contain:

1. Which payments have been made
2. Which acknowledgments have been made

This means *Paid* and *Attributed* predicates are not used in ODRL0. Also removed are related constructs *prepay* and *attribution*. We also had to remove two other constructs based on *prepay* and *attribution* out of ODRL0 in *inSeq* and *anySeq*. *prepay*, *attribution*, *inSeq* and *anySeq* make up what is called *requirements* in ODRL.

In ODRL a *prerequisite* is either *true*, a *constraint*, a *requirement* or a *condition*. *true* is the prerequisite that always holds. Constraints are facts that are outside of control of users. For example, there is nothing *Alice* can do to satisfy the constraint "user must be Bob". Requirements are facts that are in users' control. For example, *Alice* may satisfy the

requirement "The user must pay 5 dollars". Finally conditions are constraints that must not hold.

In ODRL0, a prerequisite is either *true*, a *constraint*, or not a *constraint*. So we have removed requirements from the picture and don't have explicit conditions. Conditions are replaced by a category called *NotCons* directly in the production for prerequisites (see 2.12). Note that we have also removed the condition *not*[*policySet*] from ODRL since the authors in [2] have shown the semantics of this component are not well-defined and including it leads to intractability results.

We will add the missing pieces as described above (except for *not*[*policySet*]) making up what we will call *ODRL1* and perhaps *ODRL2* (the latter only if needed). We will also describe ODRL0 in a *BNF* grammar that looks more like Pucella's ODRL grammar. BNF style grammars are less formal as they give some suggestions about the surface syntax of expressions [Pierce1] without getting into lexical analysis and parsing related aspects such as precedence order of operators. The Coq version in contrast is more formal and could be directly used for building compilers and interpreters. We will present both the BNF version and the Coq version for each construct of ODRL0 [Pierce1]. To get started let's see what the listing 2.2 would look like in ODRL0's Coq version.

Listing 2.3: Coq version of agreement for Mary Smith

```
Agreement (Single MarySmith) Treasure Island
 (PrimitivePolicySet (Constraint (PrePay 5.00))
  (AndPolicy
   (NewList (PrimitivePolicy (Constraint
                       (Principal
                        (Single MarysComputer))) id1 Display)
   (Single (PrimitivePolicy (Constraint (Count 2)) id2 Print))))).
```

The top level ODRL0 production is the *agreement*. An agreement expresses what actions a set of subjects may perform on an object and under what conditions. Syntactically an agreement is composed of a set of subjects/users called a *principal* or *prin*, an *asset* and a *policySet*.

Listing 2.4: agreement

```
<agreement> ::= 'agreement' 'for' <prin> 'about' <asset> 'with' <policySet
    >
```

Principals or prins are composed of *subjects* which are specified based on the application e.g. Alice, Bob, etc for the DRM application we will be using throughout.

Listing 2.5: prin

```
<prin> ::=  { <subject_1>, ..., <subject_m> }
```

Listing 2.6: subject

```
<subject> ::= N
```

Assets are also application specific but similar to subjects we will use specific ones for the DRM application (taken from [2]). *ebook*, *The Report* and *latestJingle* are examples of specific subjects we will be using throughout. Syntactically an asset is represented as a natural number (N). Similarly for subjects.

Listing 2.7: asset

```
<asset> ::= N
```

Agreements include policy sets. Each policy set specifies a *prerequisite* and a *policy*. In general if the prerequisite holds the policy is taken into consideration. Otherwise the policy will not be looked at. Some policy sets are specified as *exclusive*. The *Primitive Exclusive Policy Sets* are exclusive to agreement's users in that only those users may perform the actions specified in the policy set. The implication is that all other users who are not specified in the agreement's principal (prin) are forbidden from performing the specified actions. Finally policy sets could be grouped together in a *conjunction* allowing a single agreement to be associated with many policy sets.

Listing 2.8: policySet

```
<policySet> ::=
   <preRequisite> → <policy>                    ; primitive policy set
   <preRequisite> ↦ <policy>                    ; primitive exclusive policy set
   'and'[ <policySet_1>, ..., <policySet_m> ]
   ; conjunction
```

A policy specifies an action to be performed on an asset, depending of whether the policy's prerequisite holds or not. If the prerequisite holds the agreement's user is permitted to perform the action on the agreement's asset; otherwise permission is denied. Similar to policy sets, policies could also be grouped together in a conjunction. The policy also includes a unique identifier. The policy identifier is added to help the translation (from agreements to formulas) but is optional in ODRL proper.

Listing 2.9: policy

```
<policy> ::=
   <preRequisite> ⇒_<policyId> <act>            ; primitive policy
   'and'[ <policy_1>, ..., <policy_m> ]         ; conjunction
```

An *Action* (*act*) is represented as a natural number. Similar to assets and subjects, actions are application specific. Some example actions taken from [2] are *Display* and *Print*.

Listing 2.10: act

```
<act> ::= N
```

A *Policy Id* (*policyId*) is a unique identifier specified as (increasing) positive integers.

Listing 2.11: policyId

```
<policyId> ::= N
```

In ODRL0 a *prerequisite* is either true or it is a *constraint*. The *true* prerequisite always holds. A constraint is an intrinsic part of a policy and cannot be influenced by agreement's user. Minimum height requirements for popular attractions and rides are examples of we would consider a constraint. The constraint *ForEachMember* is interesting in its expressive power but has complicated semantics as we shall see in the 2.6 section. Roughly speaking, ForEachMember takes a prin (a list of subjects) and a list L of constraints. The ForEachConstraint holds if each subject in prin satisfies each constraint in L.*NotCons* is a negation of a constraint. The set of prerequisites are closed under conjunction (*AndPrqs*), disjunction (*OrPrqs*) and exclusive disjunction (*XorPrqs*).

Listing 2.12: preRequisite

```
<preRequisite> ::=
   'True'                                   ; always true
   <constraint>                             ; constraint
   'ForEachMember' [<prin> ; <constraint_1>, ..., <constraint_m> ]
   ; constraint distribution
   'not' [ <constraint> ]                   ; suspending constraint
   'and'[ <preRequisite_1>, ..., <preRequisite_m> ]
   ; conjunction
   'or'[ <preRequisite_1>, ..., <preRequisite_m> ]
   ; disjunction
   'xor'[ <preRequisite_1>, ..., <preRequisite_m> ]
   ; exclusive disjunction
```

Constraints are either *Principal*, *Count* or *CountByPrin*. Principal constraints basically require matching to specified prins. For example, the user being Alice is a Principal constraint. A count constraint refers to a set of policies P and specifies the number of times the user of an agreement has invoked the policies in P to justify her actions. If the count constraint is part of a policy then the set P is composed of the single policy. In the case that the count constraint is part of a policy set, the set P is the set of policies specified in the policy set.

Listing 2.13: constraint

```
<constraint> ::=
   <prin>                                   ; principal
   'Count' [N]                              ; number of executions
   <prin> ('Count' [N])                     ; number of executions by prin
```

2.5 Coq Version

Listing 2.14: Coq version of agreement

```
Inductive agreement : Set :=
  | Agreement : prin → asset → policySet → agreement.
```

Listing 2.15: prin

```
Definition prin := nonemptylist subject.
```

Listing 2.16: asset

```
Definition asset := nat.
```

Listing 2.17: subject

```
Definition subject := nat.
```

Listing 2.18: policySet

```
Inductive policySet : Set :=
  | PrimitivePolicySet : preRequisite → policy → policySet
  | PrimitiveExclusivePolicySet : preRequisite → policy  → policySet
  | AndPolicySet : nonemptylist policySet → policySet.
```

Listing 2.19: policy

```
Inductive policy : Set :=
  | PrimitivePolicy : preRequisite → policyId → act → policy
  | AndPolicy : nonemptylist policy → policy.
```

Listing 2.20: act

```
Definition act := nat.
```

Listing 2.21: policyId

```
Definition policyId := nat.
```

Listing 2.22: preRequisite

```
Inductive preRequisite : Set :=
  | TruePrq : preRequisite
  | Constraint : constraint → preRequisite
  | ForEachMember : prin  → nonemptylist constraint → preRequisite
  | NotCons : constraint → preRequisite
  | AndPrqs : nonemptylist preRequisite → preRequisite
  | OrPrqs : nonemptylist preRequisite → preRequisite
  | XorPrqs : nonemptylist preRequisite → preRequisite.
```

Listing 2.23: constraint

```
Inductive constraint : Set :=
  | Principal : prin  → constraint
  | Count : nat → constraint
  | CountByPrin : prin → nat → constraint.
```

2.6 Semantics

In this section, we describe the semantics of ODRL0 language by a translation from agreements to a subset of many-sorted first-order logic formulas with equality. The semantics will help answer queries of the form "may subject s perform action act to asset a?". If the answer is yes, we say permission is granted. Otherwise permission is denied.

At a high-level, an agreement is translated into a conjunction of formulas of the form $\forall x(prerequisites(x) \rightarrow P(x))$ where $P(x)$ itself is a conjunction of formulas of the form $prerequisites(x) \rightarrow (\neg)Permitted(x, act, a)$, where "Permitted (x, act, a)" means the subject x is permitted to perform action act on asset a.

2.6.1 Agreement Translation

The translation of an *agreement* returns the translation for a *policySet* per $prin_u$, the agreement's user and a, the asset.

Listing 2.24: Agreement Translation

$$[\![agreement\ for\ prin_u\ about\ a\ with\ ps]\!] \triangleq [\![policySet]\!]^{prin_u,a}$$

2.6.2 Policy Set Translation

The translation for a *policySet* ($[\![policySet]\!]^{prin_u,a}$) is described by translation formulas for each type of *policySet*. A *policySet* is either a *PrimitivePolicySet*, a *PrimitiveExclusivePolicySet* or a *AndPolicySet*.

2.6.2.1 PrimitivePolicySet Translation

Translation of a *PrimitivePolicySet* (*preRequisite* $\rightarrow$ *policy*) yields a formula that includes a test on whether the subject is in the set of agreements' users, the translation of the policy and the translation of the *prerequisite*. Basically if the subject in question is a user of the agreement and the policySet prerequisites hold, then the policy holds. Translation of the policy for a *PrimitivePolicySet* is called a *positive translation*. A positive translation is one where the actions described by the policies are permitted.

Listing 2.25: Policy Set Translation : PrimitivePolicySet

$$[\![preRequisite \rightarrow policy]\!]^{e,prin_u,a} \triangleq \forall x\ ((([\![prin_u]\!]_x \wedge [\![preRequisite]\!]_x^{e,getId(p),prin_u,a}) \rightarrow [\![policy]\!]_x^{positive,e,prin_u,a})$$

Listing 2.26: Positive Policy Translation : Single policy

$$[\![preRequisite \Rightarrow_{policyId} act]\!]_x^{positive,e,prin_u,a} \triangleq ([\![preRequisite]\!]_x^{e,policyId,prin_u}) \Rightarrow Permitted(x, [\![act]\!], a)$$

If the policy is a *AndPolicy*, the translation yields a conjunction of positive translations of each policy in turn.

Listing 2.27: Positive Policy Translation : List of policies

$$[\![and[policy_1, ..., policy_m]]\!]^{positive,e,prin_u,a} \triangleq [\![policy_1]\!]^{positive,e,prin_u,a} \wedge ... \wedge [\![policy_m]\!]^{positive,e,prin_u,a}$$

2.6.2.2 PrimitiveExclusivePolicySet Translation

PrimitiveExclusivePolicySet ($preRequisite \mapsto policy$) yields the conjunction of two implications. The first implication, is the same as one found in the translation of *PrimitivePolicySet*. The second implication however restricts access (to make the policy set exclusive) to only those subjects that are in the agreement's user. Translation of the policy in the second implication is called a *negative translation*. A negative translation is one where the actions described by the policies are not permitted.

Listing 2.28: Policy Set Translation : PrimitiveExclusivePolicySet

$$[\![preRequisite \mapsto policy]\!]^{e,prin_u,a} \triangleq \forall x \ ([\![prin_u]\!]_x \wedge [\![preRequisite]\!]_x^{e,getId(p),prin_u,a}) \rightarrow [\![policy]\!]_x^{positive,e,prin_u,a}) \wedge \forall x \ (\neg [\![prin_u]\!]_x \rightarrow [\![policy]\!]_x^{negative,e,a})$$

Listing 2.29: Negative Policy Translation : Single policy

$$[\![preRequisite \Rightarrow_{policyId} act]\!]_x^{negative,e,prin_u,a} \triangleq ([\![preRequisite]\!]_x^{e,policyId,prin_u}) \Rightarrow \neg(Permitted(x, [\![act]\!], a))$$

If the policy is a *AndPolicy*, the translation yields a conjunction of negative translations of each policy in turn.

Listing 2.30: Negative Policy Translation : List of policies

$$[\![and[policy_1, ..., policy_m]]\!]^{negative,e,a} \triangleq [\![policy_1]\!]^{negative,e,a} \wedge ... \wedge [\![policy_m]\!]^{negative,e,a}$$

2.6.2.3 AndPolicySet Translation

AndPolicySet translates to conjunctions of the corresponding policy set translations.

Listing 2.31: Policy Set Translation : AndPolicySet

$$[\![and[policySet_1, ..., policySet_m]]\!]^{e,prin_u,a} \triangleq [\![policySet_1]\!]^{e,prin_u,a} \wedge ... \wedge [\![policySet_m]\!]^{e,prin_u,a}$$

2.6.3 Principal Translation

Translation for a *prin* ($[\![prin]\!]_x$) is a formula that is true if and only if the subject x is in the prin set. A *prin* is either a single subject or a list of subjects ($\{subject_1, ..., subject_m\}$ so the translation covers both cases.

If the *prin* is a single subject, the translation is a formula that is true if and only if the subject x is the same as the single subject *subject*.

2.6.3.1 Single Subject Translation

Listing 2.32: Prin Translation : Single subject

$$[\![subject]\!]_x \triangleq x = subject$$

2.6.3.2 List of Subjects Translation

Translation of a list of subjects is the disjunction of the translations for each subject.

Listing 2.33: Prin Translation : List of subjects

$$[\![\{subject_1, ..., subject_m\}]\!]_x \triangleq [\![subject_1]\!]_x \lor ... \lor [\![subject_m]\!]_x$$

2.6.4 Prerequisite Translation

Translation for a prerequisite is a formula $[\![prerequisite]\!]_x^{[id_1,...,id_m],prin,a}$, where the set of *id*s refer to identifiers for policies that are implied by the prerequisites, *prin* is the agreement's user(s) (and to which the prerequisites apply), a is the asset and x is a variable of type *subject*. The translation for a *prerequisite* is described by translation formulas for each type of *prerequisite*. A *prerequisite* is either always *true*, a *Constraint*, a *ForEachMember*, a *NotCons*, a *AndPrqs*, a *OrPrqs* or a *XorPrqs*.

2.6.4.1 True Prerequisite Translation

The translation for a *TruePrq* yields a formula that is always *true*.

Listing 2.34: Prerequisite Translation : Always True Prerequisite

$$[\![prerequisite :: true]\!] \triangleq \texttt{True}$$

2.6.4.2 Constraint Prerequisite Translation

The translation for a *Constraint* is handled by a specialized constraint translation function (coverage of which starts at 2.41.

Listing 2.35: Prerequisite Translation : Constraint

$$[\![prerequisite :: constraint]\!]_x^{[id_1,...,id_m],prin_u} \triangleq [\![constraint]\!]_x^{[id_1,...,id_m],prin_u}$$

2.6.4.3 ForEachMember Prerequisite Translation

The translation for a *ForEachMember* is also is handled by a specialized translation function (covered at 2.44.

Listing 2.36: Prerequisite Translation : ForEachMember

$$[\![prerequisite :: forEachMember]\!]_x^{[subject_1,...,subject_k],[constraint_1,...,constraint_m],[id_1,...,id_n]} \triangleq [\![forEachMember]\!]_x^{[subject_1,...,subject_k],[constraint_1,...,constraint_m],[id_1,...,id_n]}$$

2.6.4.4 NotCons Prerequisite Translation

The translation for a *NotCons* yields a formula that is simply the negation of the translation for a constraint.

Listing 2.37: Prerequisite Translation : Not Constraint

$$[\![not\ \ prerequisite :: constraint]\!]_x^{[id_1,...,id_m],prin_u} \triangleq \neg [\![constraint]\!]_x^{[id_1,...,id_m],prin_u}$$

2.6.4.5 AndPrqs Prerequisite Translation

The translation for a *AndPrqs* yields a formula that is the conjunction of the translation for each *preRequisite*.

Listing 2.38: Prerequisite Translation : Conjunction

$$[\![and\ \ [preRequisite_1, ..., preRequisite_k]]\!]^{[id_1,...,id_m],prin_u} \triangleq [\![preRequisite_1]\!]^{[id_1,...,id_m],prin_u} \wedge ... \wedge [\![preRequisite_k]\!]^{[id_1,...,id_m],prin_u}$$

2.6.4.6 OrPrqs Prerequisite Translation

The translation for a *OrPrqs* yields a formula that is the inclusive disjunction of the translation for each *preRequisite*.

Listing 2.39: Prerequisite Translation : Inclusive Disjunction

$$[\![or\ \ [preRequisite_1, ..., preRequisite_k]]\!]^{[id_1,...,id_m],prin_u} \triangleq [\![preRequisite_1]\!]^{[id_1,...,id_m],prin_u} \vee \\ ... \vee [\![preRequisite_k]\!]^{[id_1,...,id_m],prin_u}$$

2.6.4.7 XorPrqs Prerequisite Translation

The translation for a *XorPrqs* yields a formula that is the exclusive disjunction of the translation for each *preRequisite*.

Listing 2.40: Prerequisite Translation : Exclusive Disjunction

$$[\![Xor\ \ [preRequisite_1, ..., preRequisite_k]]\!]^{[id_1,...,id_m],prin_u} \triangleq [\![preRequisite_1]\!]^{[id_1,...,id_m],prin_u} \oplus \\ ... \oplus [\![preRequisite_k]\!]^{[id_1,...,id_m],prin_u}$$

2.6.5 Constraint Translation

Translation for a constraint is a formula $[\![constraint]\!]_x^{[id_1,...,id_m],prin_u,a}$, where the set of *id*s refer to identifiers for policies that are implied by the constraint, $prin_u$ is the agreement's user(s) (and to which the constraint applies), a is the asset and x is a variable of type *subject*. The translation for a *constraint* is described by translation formulas for each type of *constraint*. A *constraint* is either a *Principal*, a *Count*, or a *CountByPrin*.

2.6.5.1 Principal Constraint Translation

The translation for a *Principal* is handled by a specialized translation function (covered at 2.52.

Listing 2.41: Constraint Translation : Principal

$$[\![constraint :: prin]\!]_x^{[subject_1,...,subject_m]} \triangleq [\![prin]\!]_x^{[subject_1,...,subject_m]}$$

2.6.5.2 Count Constraint Translation

The translation for a *Count* is handled by a specialized translation function (covered at ??.

Listing 2.42: Constraint Translation : Count

$$[\![constraint :: count[N]]\!]_x^{[id_1,...,id_m],prin_u} \triangleq [\![count[N]]\!]_x^{[id_1,...,id_m],prin_u}$$

2.6.5.3 CountByPrin Constraint Translation

The translation for a *CountByPrin* is handled by the same specialized translation function as that for *Count*. The difference is that *CountByPrin* overrides the subjects in $prin_u$ by a different set of subjects (covered at **??**.

Listing 2.43: Constraint Translation : Count by Principal

$$[\![constraint :: prin(count[N])]\!]_x^{[subject_1,...,subject_m],[id_1,...,id_n]} \triangleq [\![prin(count[N])]\!]_x^{[subject_1,...,subject_m],[id_1,...,id_n]}$$

2.6.6 forEachMember Translation

Listing 2.44: ForEachMember Translation : Count by Principal

$$\begin{aligned}&[\![forEachMember]\!]_x^{[subject_1,...,subject_k],[constraint_1,...,constraint_m],[id_1,...,id_n]} \triangleq \\ &\quad [\![constraint]\!]_x^{(subject_1,constraint_1),[id_1,...,id_n]} \wedge \ ... \ \wedge [\![constraint]\!]_x^{(subject_1,constraint_m),[id_1,...,id_n]} \\ &\quad \wedge \ ... \ \wedge [\![constraint]\!]_x^{(subject_2,constraint_1),[id_1,...,id_n]} \wedge \ ... \ \wedge \\ &\quad [\![constraint]\!]_x^{(subject_2,constraint_m),[id_1,...,id_n]} \wedge \ ... \ \wedge [\![constraint]\!]_x^{(subject_k,constraint_1),[id_1,...,id_n]} \\ &\quad \wedge \ ... \ \wedge [\![constraint]\!]_x^{(subject_k,constraint_m),[id_1,...,id_n]}\end{aligned}$$

2.6.7 "Not Constraint" Translation

The translation for "Not Constraint" was listed in listing 2.37 earlier but we repeat it here to go along the Coq version.

Listing 2.45: Not Constraint Translation

$$[\![not\ \ constraint]\!]_x^{[id_1,...,id_m],prin_u} \triangleq \neg [\![constraint]\!]_x^{[id_1,...,id_m],prin_u}$$

2.6.8 Count Translation

2.6.8.1 Count Translation For Subject/ID Pair

The translation for *Count* or *CountByPrin* for a pair of subject and policy identifier is a formula that is true if the number of times the $subject_1$ has invoked a policy with policy identifier id_1 is smaller than N.

Listing 2.46: Count Translation : subject and policyId pair

$$[\![count[N]]\!]_x^{subject_1,id_1} \triangleq getCount(subject_1, id_1) < N$$

2.6.8.2 Count Translation For Subject/ID Pairs

The translation for *Count* or *CountByPrin* for subject and policy identifier pairs is a formula that is true if the total number of times that a subject has invoked a policy with policy identifier id_i is smaller than N.

Listing 2.47: Count Translation : subject and policyId pairs

$$[\![count[N]]\!]_x^{[id_1,...,id_m],prn} \triangleq$$

$$(getCount(getSubject(prn)_1, id_1) \ +...+ \ getCount(getSubject(prn)_1, id_m) \ +...+ \\ getCount(getSubject(prn)_k, id_1) \ +...+ \ getCount(getSubject(prn)_k, id_m)) \ < \ N$$

2.7 Semantics in Coq

The translation functions plus the auxiliary types and infrastructure, implementing the semantics have been encoded in Coq. Translation functions all return the *sort Prop*.

Talk about Props here...

Whether a permission is granted or denied depends on the agreements in question but also on the facts recorded in the environment. For ODRL0 those facts revolve around the number of times a policy has been used to justify an action (see 2.4.1 for more details on odrl0). We encode this information in an *environment* which is a conjunction of equalities of the form *count(s, policyId) = n*.

The Coq version of the count equality is a new inductive type called *count_ equality*. An environment is defined to be a non-empty list of count_equality objects.

Listing 2.48: Environments and Counts

```
Inductive count_equality : Set :=
  | CountEquality : subject → policyId → nat → count_equality.

Inductive environment : Set :=
  | SingleEnv : count_equality → environment
  | ConsEnv : count_equality → environment → environment.
```

The non-empty list data structure is defined as a new *polymorphic* inductive type in its own section. The non-empty list definition is listed at listing 2.49.

Listing 2.49: nonemptylist type

```
Section nonemptylist.

Variable X : Set.

Inductive nonemptylist : Set :=
  | Single : X → nonemptylist
  | NewList : X → nonemptylist → nonemptylist.

End nonemptylist.
```

Translation of the top level *agreement* element proceeds by case analysis on the structure of the agreement. However an agreement can only be built one way; by calling the constructor *Agreement*. The translation proceeds by calling the translation function for the corresponding *policySet* namely the parameter to *Agreement* called *ps*.

Listing 2.50: Translation of agreement

```
Definition trans_agreement (e:environment)(ag:agreement) : Prop :=
 match ag with
   | Agreement prin_u a ps ⇒ trans_ps e ps prin_u a
 end.
```

Translation of a *policySet* (called *trans_ps* in listing ??), takes as input e, the environment, ps, the policy set, $prin_u$, the agreement's user, and a, the asset, and proceeds by case analysis of different policySet constructors and recursing into translation functions for the composing elements. A policySet is either a *PrimitivePolicySet*, *PrimitiveExclusivePolicySet* or a *AndPolicySet*.

Note that to implement the translation for an *AndPolicySet* a local function $trans_ps_list$ has been defined where for a single *policySet*, $trans_ps$ is called, and for a list of *policySet*s, the conjunction of $trans_ps$s are returned.

Listing 2.51: Translation of Policy Set

```
Fixpoint trans_ps
 (e:environment)(ps:policySet)(prin_u:prin)(a:asset){struct ps} : Prop :=

let trans_ps_list := (fix trans_ps_list (ps_list:nonemptylist policySet)(prin_u:prin)
    (a:asset){struct ps_list}:=
 match ps_list with
  | Single ps1 ⇒ trans_ps e ps1 prin_u a
  | NewList ps ps_list' ⇒ ((trans_ps e ps prin_u a) /\ (trans_ps_list ps_list' prin_u a
   ))
 end) in
  match ps with
  | PrimitivePolicySet prq p ⇒ ∀ x, (((trans_prin x prin_u) /\
                        (trans_preRequisite e x prq (getId p) prin_u)) →
                        (trans_policy_positive e x p prin_u a))

  | PrimitiveExclusivePolicySet prq p ⇒ ∀ x, ((((trans_prin x prin_u) /\
                                  (trans_preRequisite e x prq (getId p) prin_u)) →
                                 (trans_policy_positive e x p prin_u a)) /\
                                ((not (trans_prin x prin_u)) → (trans_policy_negative e
    x p a)))

  | AndPolicySet ps_list ⇒ trans_ps_list ps_list prin_u a
  end.
```

Translation of a *prin* (called *trans_prin* in listing 2.52) takes as input x, the *subject* in question, p, the principal or the *prin*, and proceeds based on whether p is a single subject or a list of subjects. If p is a single subject, s, the *Prop* $x = s$ is returned. Otherwise the disjunction of the translation of the first subject in p (s) and the *rest* of the subjects is returned.

Listing 2.52: Translation of a Prin

```
Fixpoint trans_prin
 (x:subject)(p: prin): Prop :=

 match p with
  | Single s ⇒ (x=s)
  | NewList s rest ⇒ ((x=s) \/ trans_prin x rest)
 end.
```

A positive translation for a policy (called *trans_policy_positive* in listing 2.53) takes as input e, the *environment*, x, the *subject*, p, the *policy* to translate, $prin_u$, the agreement's user, and a, the asset and proceeds based on whether we have a *PrimitivePolicy* or a *AndPolicy*. If the policy is a *PrimitivePolicy* an implication is returned which indicates x is *permitted* to do *action* to a, if the *preRequisite* holds.

Permitted is a predicate specified as *ParameterPermitted* : *subject*− > *act*− > *asset*− > *Prop*. So *Permitted* predicate takes a *subject*, an *act* (an action) and an *asset* and returns a *Prop*.

Note that to implement the translation for an *AndPolicy* a local function *trans_p_list* has been defined where for a single *policy*, *trans_policy_positive* is returned, and for a list of *policy*s, the conjunction of *trans_policy_positive*s are returned.

Listing 2.53: Translation of a positive policy

```
Fixpoint trans_policy_positive
 (e:environment)(x:subject)(p:policy)(prin_u:prin)(a:asset){struct p} : Prop :=

let trans_p_list := (fix trans_p_list (p_list:nonemptylist policy)(prin_u:prin)(a:
    asset){struct p_list}:=
             match p_list with
              | Single p1 ⇒ trans_policy_positive e x p1 prin_u a
              | NewList p p_list' ⇒
                 ((trans_policy_positive e x p prin_u a) /\
                  (trans_p_list p_list' prin_u a))
             end) in


 match p with
  | PrimitivePolicy prq policyId action ⇒ ((trans_preRequisite e x prq (Single
   policyId) prin_u) →
                                  (Permitted x action a))
  | AndPolicy p_list ⇒ trans_p_list p_list prin_u a
 end.
```

A negative translation for a policy (called *trans_policy_negative* in listing 2.54) takes as input e, the *environment*, x, the *subject*, p, the *policy* to translate, and a the asset and proceeds based on whether we have a *PrimitivePolicy* or a *AndPolicy*. If the policy is a *PrimitivePolicy* an implication is returned which indicates x is forbidden to do *action* to a regardless of whether *preRequisite* holds. Note that the notation $(\neg)$ indicates that *Permitted* may be negated. As the case for the positive translation, to implement the translation for an *AndPolicy* a local function *trans_p_list* has been defined where for a single *policy*, *trans_policy_negative* is returned, and for a list of *policy*s, the conjunction of *trans_policy_negative*s are returned.

Listing 2.54: Translation of a negative policy

```
Fixpoint trans_policy_negative
 (e:environment)(x:subject)(p:policy)(a:asset){struct p} : Prop :=
let trans_p_list := (fix trans_p_list (p_list:nonemptylist policy)(a:asset){
    struct p_list}:=
            match p_list with
              | Single p1 ⇒ trans_policy_negative e x p1 a
              | NewList p p_list' ⇒ ((trans_policy_negative e x p a) /\
                                    (trans_p_list p_list' a))
            end) in


 match p with
  | PrimitivePolicy prq policyId action ⇒ not (Permitted x action a)
  | AndPolicy p_list ⇒ trans_p_list p_list a
 end.
```

The translation of a *prerequisite* (called *trans_preRequisite* in listing 2.55) takes as input e, the *environment*, x, the *subject*, *prq*, the *preRequisite* to translate, IDs, the set of identifiers (of policies implied by the *prq*), $prin_u$, the agreement's user, and proceeds by case analysis on the structure of the *prerequisite*. A *prerequisite* is either a $TruePrq$, a $Constraint$, a $ForEachMember$, a $NotCons$, a $AndPrqs$, a $OrPrqs$ or a $XorPrqs$.

In listing 2.55 the translation for $TruePrq$ is the Prop $True$, the translations for $Constraint$, $ForEachMember$ and $NotCons$ simply call respective translation functions for corresponding types *constraint* and $forEachMember$ (namely *trans_constraint*, $trans\_forEachMe$ and *trans_notCons*). Note that the translation for $AndPrqs$, $OrPrqs$ and $XorPrqs$ have not yet been implemented but based on the their many-sorted-logic formulas' specifications (2.12) they will be conjunctions, disjunctions and exclusive disjunctions of translations for each *prerequisite*.

Listing 2.55: Translation of a PreRequisite

```
Definition trans_preRequisite
 (e:environment)(x:subject)(prq:preRequisite)(IDs:nonemptylist policyId)(prin_u:prin) :
    Prop :=

 match prq with
  | TruePrq ⇒ True
  | Constraint const ⇒ trans_constraint e x const IDs prin_u
  | ForEachMember prn const_list ⇒ trans_forEachMember e x prn const_list IDs
  | NotCons const ⇒ trans_notCons e x const IDs prin_u
  | AndPrqs prqs ⇒ True
  | OrPrqs prqs ⇒ True
  | XorPrqs prqs ⇒ True
 end.
```

The translation of a *constraint* (called *trans_constraint* in listing 2.56) takes as input e the *environment*, x the *subject*, *const*, the *constraint* to translate, IDs, the set of identifiers (of policies implied by the parent *preRequisite*) and $prin_u$, the agreement's user and proceeds by case analysis on the structure of the *constraint*. A *constraint* is either a $Principal$, a $Count$ or a $CountByPrin$.

In listing 2.56 the translation for $Principal$ returns the translation function (namely *trans_prin*) for the *prn* (the *prin* that accompanies the *const* constraint). The translation for $Count$ and $CountByPrin$ return the translation function *trans_count*. For $Count$ the *prin* used is the agreement's user, whereas the *prin* used is the one passed to $CountByPrin$ namely *prn*.

Listing 2.56: Translation of a Constraint

```
Fixpoint trans_constraint
 (e:environment)(x:subject)(const:constraint)(IDs:nonemptylist policyId)
 (prin_u:prin){struct const} : Prop :=
 match const with
  | Principal prn ⇒ trans_prin x prn

  | Count n ⇒ trans_count e n IDs prin_u

  | CountByPrin prn n ⇒ trans_count e n IDs prn

 end.
```

The translation of a $forEachMember$ (called $trans\_forEachMember$ in listing 2.57) takes as input e the *environment*, x the *subject*, *principals*, the set of subjects that override the agreement's user(s), *const_list* the set of constraints and IDs, the set of identifiers (of policies implied by the parent *preRequisite*).

To implement the translation for a $forEachMember$ we start by calling an auxiliary function *process_two_lists* that effectively returns a new list composed of pairs of members of the first list and the second list (the cross-product of the two input lists). In the case of a $forEachMember$ translation, the call is "*process_two_lists principals const_list*" which returns a list of pairs of subject and constraint namely *prins_and_constraints*. *prins_and_constraints* is then passed to a locally defined function $trans\_forEachMember\_Aux$ where for a single pair of subject and constraint *trans_constraint* is called and for a list of pairs of subject and constraints, the conjunction of *trans_constraint*s (for the first pair) and $trans_forEachMember_Aux$s (for the rest of the pairs) are returned.

Listing 2.57: Translation of forEachMember

```
Fixpoint trans_forEachMember
      (e:environment)(x:subject)(principals: nonemptylist subject)(const_list:
    nonemptylist constraint)
      (IDs:nonemptylist policyId){struct const_list} : Prop :=

let trans_forEachMember_Aux
 := (fix trans_forEachMember_Aux
      (prins_and_constraints : nonemptylist (Twos subject constraint))
      (IDs:nonemptylist policyId){struct prins_and_constraints} : Prop :=

    match prins_and_constraints with
     | Single pair1 ⇒ trans_constraint e x (right pair1) IDs (Single (left pair1))
     | NewList pair1 rest_pairs ⇒
        (trans_constraint e x (right pair1) IDs (Single (left pair1))) /\
        (trans_forEachMember_Aux rest_pairs IDs)
    end) in

    let prins_and_constraints := process_two_lists principals const_list in
    trans_forEachMember_Aux prins_and_constraints IDs.
```

The translation of a *NotCons* (called *trans_notCons* in listing 2.58) takes as input e the *environment*, x the *subject*, *const*, the *constraint* to translate, IDs, the set of identifiers (of policies implied by the parent *preRequisite*) and $prin_u$, the agreement's user and proceeds to return the negation of *trans_constraint* (see listing 2.56).

Listing 2.58: Translation of not cons

```
Definition trans_notCons
 (e:environment)(x:subject)(const:constraint)(IDs:nonemptylist policyId)(prin_u:prin) :
    Prop :=
 ~ (trans_constraint e x const IDs prin_u).
```

The translation of a *Count* or a *CountByPrin* (called *trans_count* in listing 2.59) takes as input e the *environment*, n the total number of times the subjects mentioned in $prin_u$ (last parameter) may invoke the policies identified by IDs (third parameter).

To implement the translation for a *Count* or a *CountByPrin* we start by calling an auxiliary function *process_two_lists* that effectively returns a new list composed of pairs of members of the first list and the second list (the cross-product of the two input lists). In the case of *trans_count*, the call is "*process_two_lists* IDs $prin_u$" which returns a list of pairs of *policyId* and *subject* namely *ids_and_subjects*. *ids_and_subjects* is then passed to a locally defined function *trans_ count_ aux*.

trans_count_aux returns the current count for a single pair of *policyId* and *subject* (the call to *getCount* which looks up the environment e and returns the current count per

each *subject* and *policyId*) and for a list of pairs of *policyId* and *subject*s, the addition of *get_count* (for the first pair) and *trans_count_aux*s (for the rest of the pairs) is returned.

A local variable $running_total$ has the value returned by *trans_count_aux*. Finally the proposition $running_total < n$ is returned as the translation for a *Count* or a *CountByPrin*.

Note that the only difference between translations for a *Count* and a *CountByPrin* is the additional *prn* parameter for *CountByPrin* which allows for getting counts for subjects not necessarily the same as $prin_u$, the agreement's user(s).

Listing 2.59: Translation of count

```
Fixpoint trans_count
  (e:environment)(n:nat)(IDs:nonemptylist policyId)
  (prin_u:prin) : Prop :=

  let trans_count_aux
   := (fix trans_count_aux
       (ids_and_subjects : nonemptylist (Twos policyId subject)) : nat :=
    match ids_and_subjects with
      | Single pair1 ⇒ getCount e (right pair1) (left pair1)
      | NewList pair1 rest_pairs ⇒
        (getCount e (right pair1)(left pair1)) +
        (trans_count_aux rest_pairs)
     end) in

  let ids_and_subjects := process_two_lists IDs prin_u in
  let running_total := trans_count_aux ids_and_subjects in
  running_total < n.
```

References

[1] Robby Robson Geoff Collier, Harry Piccariello. A digital rights management ecosystem model for the education community. *DRM Whitepapers: Content Guard*, 2004.

[2] Riccardo Pucella and Vicky Weissman. A formal foundation for ODRL. *CoRR*, abs/cs/0601085, 2006.