Certifying Digital Rights' Expression Languages

by

Bahman Sistany

Ph.D.Thesis Proposal For the Ph.D. degree in Computer Science

School of Electrical Engineering and Computer Science Faculty of Engineering University of Ottawa

Ph.D.Thesis Advisor: Amy Felty

Abstract

This is the abstract.

${\bf Acknowledgements}$

I would like to thank all the little people who made this possible.

Dedication

This is dedicated to the one I love.

Table of Contents

List of Tables									vii			
Li	st of	Figure	es									viii
1 Introduction												1
2	\mathbf{Mid}	ldle										3
	2.1 Logic Based Semantics for ODRL								•		 •	3
	2.2	Pucell	la 2006									3
	2.3	what	will I do?						•		 •	4
		2.3.1	Coq .						•		 •	4
	2.4	Abstra	act Synta:	x					•		 •	4
		2.4.1	Odrl0						•		 •	5
	2.5	Coq V	ersion .				•		•			8
	2.6	Seman						•			10	
		2.6.1	Agreeme	ent Translation					•		 •	10
		2.6.2	Policy S	et Translation								10
			2.6.2.1	PrimitivePolicySet Translation				•				10
			2.6.2.2	${\bf Primitive Exclusive Policy Set\ Translation}$					•		 •	11
			2.6.2.3	AndPolicySet Translation								11
		2.6.3	3.3 Principal Translation									12
			2.6.3.1	Single Subject Translation			•		•			12
			2.6.3.2	List of Subjects Translation					•			12
		2.6.4 Prerequisite Translation										12
			2.6.4.1	True Prerequisite Translation								12
			2.6.4.2	Constraint Prerequisite Translation								13

		2.6.4.3	For Each Member Prerequisite Translation	13
		2.6.4.4	NotCons Prerequisite Translation	13
		2.6.4.5	AndPrqs Prerequisite Translation	13
		2.6.4.6	OrPrqs Prerequisite Translation	14
		2.6.4.7	XorPrqs Prerequisite Translation	14
	2.6.5	Constra	int Translation	14
		2.6.5.1	Principal Constraint Translation	14
		2.6.5.2	Count Constraint Translation	14
		2.6.5.3	CountByPrin Constraint Translation	15
	2.6.6	forEach	Member Translation	15
	2.6.7	"Not Co	nstraint" Translation	15
2.7	Semar	ntics in Co	oq	16
APPE	NDIC:	ES		22
Refere	nces			22

List of Tables

List of Figures

Chapter 1

Introduction

Digital rights management, DRM, refers to the digital management of rights associated with the access or usage of digital assets. There are various aspects of rights management however. According to the authors of the whitepaper "A digital rights management ecosystem model for the education community," digital rights management systems cover the following four areas: 1) defining rights 2) distributing/acquiring rights 3) enforcing rights and 4) tracking usage [1].

Rights Expression Languages, RELs, or more precisely when dealing with digital assets, Digital Rights Expression Languages DRELs deal with the "rights definition" aspect of the DRM ecosystem. A DREL, allows the expression and definition of digital asset usage rights such that other areas of the DRM ecosystem namely the enforcement mechanism and the usage tracking components can function correctly.

Currently the most popular RELs are the eXtensible rights Markup Language, XrML [bib], and the Open Digital Rights Language, ODRL [bib]. Both of these languages are XML based and are considered declarative languages. XrML has been selected to be the REL for MPEG-21 which is an ISO standard for multimedia applications. ODRL is also a standards based REL which has been accepted as part of the W3C community with the mandate of standardizing how rights and policies, related to the usage of digital content on the Open Web Platform, OWP, are expressed [wikipedia]. ODRL 2.0 supports expression of rights and also privacy rules for social media while ODRL 1.0 was only dealing with the mobile ecosystem – ODRL 1.0 was adopted by the Open Mobile Alliance, OMA in 2000.

As popular as both XrML and ODRL are, their adoption and usage is still somewhat limited in practice. Both Apple and Microsoft for example have defined their own lightweight RELs [problem with RELs paper] in Fair Play (Apple) and in PlayReady (Microsoft). The authors of [the problem with RELs] argue that both these RELs and other ones are simply too complex to be used effectively since they try to cover much of the DRM ecosystem.

Another issue with the current batch of RELs are due to their semantics being expressed in a natural language (e.g. English). By necessity natural languages are ambiguous and open to interpretation.

To formalize the semantics of RELS several approaches have been attempted by various authors. The main categories are logic based, operational semantics based interpreters and finally web ontology based (from the Knowledge Representation Field). In this thesis we will focus on the logic based approach to formalizing semantics and will study a specific logic based language that is a translation from a subset of ODRL.

Chapter 2

Middle

2.1 Logic Based Semantics for ODRL

Formal logic can represent the statements and facts we express in a natural language like English. Propositional logic is expressive enough to express simple facts as propositions and uses connectives to allow for the negation, conjunction and disjunction of the facts. However propositional logic is not expressive enough to express policies of the kind used in languages like ODRL and XrML. For example, a simple policy expressed in English like "All who pay 5 dollars can watch the movie Toy Story" cannot be expressed in propositional logic because the concept of variables doesn't exist in propositional logic.

A richer logic called "Predicate Logic" or "First Order Logic" (FOL) is more suitable and has the expressive power to represent policies written in English. Moreover, FOL can be used to capture the meaning of policies in an unambiguous way.

Halpern and Weissman [Using First Order Logic to Reason about Policies] propose a fragment of FOL to represent and reason about policies. The fragment of FOL they arrive at is called *Lithium* which is decidable and allows for efficiently answering interesting queries. Lithium restricts policies to be written based on the concept of "bipolarity" which disallows by construction policies that both permit and deny an action on an object.

2.2 Pucella 2006

Pucella and Weissman [2] specify a predicate logic based based language that represents a subset of ODRL.

2.3 what will I do?

2.3.1 Coq

âÁć Program correctness âÁć Formal verification of software âÁć Certified programs âÁć Proof assistant âÁć Interactive and mechanized theorem proving âÁć Examples of machine assisted proofs: CompCert, four-color theorem proof âAć Coq is based on a higher-order functional programming language âÅć Dependent Types âÜN Subset types âÜN Easier than writing explicit proofs âAć Write formal specification and proofs that programs comply to their specification (a-short-intro-to-coq) âÁć Automatically extract code from specifications as Ocaml or Haskell (a-short-intro) âÅć Properties, programs and proofs are all formalized in the same language called CIC (Calculus of inductive Constructions). (ashort-intro) â Áć Coq uses a sort called Prop for propositions â Áć Coq art: â Áć Well-formed propositions are assertions one can express about values such as mathematical objects or even programs e.g. 3 < 8 âUN Note that assertions may be true, false or simply conjectures âŬŃ An assertion is only true in general if a proof is provided âŬŃ However hand written proofs are difficult to verify âUN Coq provides an environment for developing proofs including a formal language to express proofs in, the language itself being built using proof theory making it possible to step by step verification of the proofs âUN Mechanized proof verification requires a "proof" that the verification algorithm is correct itself in applying all the formal rules correctly

2.4 Abstract Syntax

Authors of [2] use abstract syntax instead of XML to express statements in the ODRL language. The abstract syntax used is a more compact representation than XML based language ODRL policies are written in and furthermore it simplifies specifying the semantics as we shall see. As an example here is an agreement written in ODRL and the comparable agreement expressed in the abstract syntax [2].

Listing 2.1: agreement for Mary Smith in XML

```
</print>
<requirement>
  <prepay>
        <payment> <amount currency="AUD"> 5.00</amount> </payment>
        </prepay>
        </requirement>
        </permission>
        <party> <context> <name> Mary Smith </name> </context> 

</agreement>
```

The agreement 2.1 is shown below using the syntax from [2].

Listing 2.2: agreement for Mary Smith as BNF (as used in [2])

```
agreement
for Mary Smith
about Treasure Island
with prePay[5.00] -> and[cpu[Mary's Computer] => display,
count[2] => print].
```

In the following we will cover the *abstract syntax* of a subset of ODRL expressed as Coq's constructs such as *Inductive Types* and Definitions. We will call this subset *ODRL0* both because it is a variation of Pucella's ODRL language and also because it is missing some constructs from Pucella's ODRL.

2.4.1 Odrl0

In ODRL0, agreements and facts (i.e. environments) will only contain the number of times each policy has been used to justify an action. In ODRL0 agreements and facts will not contain:

- 1. Which payments have been made
- 2. Which acknowledgments have been made

This means Paid and Attributed predicates are not used in ODRL0. Also removed are related constructs prepay and attribution. We also had to remove two other constructs based on prepay and attribution out of ODRL0 in inSeq and anySeq. prepay, attribution, inSeq and anySeq make up what is called requirements in ODRL.

In ODRL a prerequisite is either true, a constraint, a requirement or a condition. true is the prerequisite that always holds. Constraints are facts that are outside of control of users. For example, there is nothing Alice can do to satisfy the constraint "user must be Bob". Requirements are facts that are in users' control. For example, Alice may satisfy the

requirement "The user must pay 5 dollars". Finally conditions are constraints that must not hold.

In ODRL0, a prerequisite is either true, a constraint, or not a constraint. So we have removed requirements from the picture and don't have explicit conditions. Conditions are replaced by a category called NotCons directly in the production for prerequisites (see 2.12). Note that we have also removed the condition not[policySet] from ODRL since the authors in [2] have shown the semantics of this component are not well-defined and including it leads to intractability results.

We will add the missing pieces as described above (except for not[policySet]) making up what we will call ODRL1 and perhaps ODRL2 (the latter only if needed). We will also describe ODRL0 in a BNF grammar that looks more like Pucella's ODRL grammar. BNF style grammars are less formal as they give some suggestions about the surface syntax of expressions [Pierce1] without getting into lexical analysis and parsing related aspects such as precedence order of operators. The Coq version in contrast is more formal and could be directly used for building compilers and interpreters. We will present both the BNF version and the Coq version for each construct of ODRL0 [Pierce1]. To get started let's see what the listing 2.2 would look like in ODRL0's Coq version.

Listing 2.3: Coq version of agreement for Mary Smith

The top level ODRL0 production is the *agreement*. An agreement expresses what actions a set of subjects may perform on an object and under what conditions. Syntactically an agreement is composed of a set of subjects/users called a *principal* or *prin*, an *asset* and a *policySet*.

```
Listing 2.4: agreement
```

Principals or prins are composed of subjects which are specified based on the application e.g. Alice, Bob, etc for the DRM application we will be using throughout.

```
Listing 2.5: prin {\tt prin} ::= {\tt subject_1}, \ldots, {\tt subject_m} }
```

```
Listing 2.6: subject
```

```
<subject> ::= N
```

Assets are also application specific but similar to subjects we will use specific ones for the DRM application (taken from [2]). ebook, $The\ Report$ and latestJingle are examples of specific subjects we will be using throughout. Syntactically an asset is represented as a natural number (N). Similarly for subjects.

Listing 2.7: asset

```
<asset> ::= N
```

Agreements include policy sets. Each policy set specifies a prerequisite and a policy. In general if the prerequisite holds the policy is taken into consideration. Otherwise the policy will not be looked at. Some policy sets are specified as exclusive. The Primitive Exclusive Policy Sets are exclusive to agreement's users in that only those users may perform the actions specified in the policy set. The implication is that all other users who are not specified in the agreement's principal (prin) are forbidden from performing the specified actions. Finally policy sets could be grouped together in a conjunction allowing a single agreement to be associated with many policy sets.

Listing 2.8: policySet

A policy specifies an action to be performed on an asset, depending of whether the policy's prerequisite holds or not. If the prerequisite holds the agreement's user is permitted to perform the action on the agreement's asset; otherwise permission is denied. Similar to policy sets, policies could also be grouped together in a conjunction. The policy also includes a unique identifier. The policy identifier is added to help the translation (from agreements to formulas) but is optional in ODRL proper.

Listing 2.9: policy

An Action (act) is represented as a natural number. Similar to assets and subjects, actions are application specific. Some example actions taken from [2] are Display and Print.

Listing 2.10: act

```
<act> ::= N
```

A Policy Id (policyId) is a unique identifier specified as (increasing) positive integers.

```
Listing 2.11: policyId
```

```
<policyId> ::= N
```

In ODRL0 a prerequisite is either true or it is a constraint. The true prerequisite always holds. A constraint is an intrinsic part of a policy and cannot be influenced by agreement's user. Minimum height requirements for popular attractions and rides are examples of we would consider a constraint. The constraint ForEachMember is interesting in its expressive power but has complicated semantics as we shall see in the 2.6 section. Roughly speaking, ForEachMember takes a prin (a list of subjects) and a list L of constraints. The ForEachConstraint holds if each subject in prin satisfies each constraint in L.NotCons is a negation of a constraint. The set of prerequisites are closed under conjunction (AndPrqs), disjunction (OrPrqs) and exclusive disjunction (XorPrqs).

Listing 2.12: preRequisite

Constraints are either *Principal*, *Count* or *CountByPrin*. Principal constraints basically require matching to specified prins. For example, the user being Alice is a Principal constraint. A count constraint refers to a set of policies P and specifies the number of times the user of an agreement has invoked the policies in P to justify her actions. If the count constraint is part of a policy then the set P is composed of the single policy. In the case that the count constraint is part of a policy set, the set P is the set of policies specified in the policy set.

Listing 2.13: constraint

2.5 Coq Version

Listing 2.14: Coq version of agreement

```
\begin{array}{l} \textbf{Inductive agreement}: \textbf{Set} := \\ \mid \textbf{Agreement}: \textbf{prin} \rightarrow \textbf{asset} \rightarrow \textbf{policySet} \rightarrow \textbf{agreement}. \end{array}
```

Listing 2.15: prin

```
Definition prin := nonemptylist subject.
```

Listing 2.16: asset

```
Definition asset := nat.
```

Listing 2.17: subject

```
Definition subject := nat.
```

Listing 2.18: policySet

```
Inductive policySet : Set :=
    | PrimitivePolicySet : preRequisite → policy → policySet
    | PrimitiveExclusivePolicySet : preRequisite → policy → policySet
    | AndPolicySet : nonemptylist policySet → policySet.
```

Listing 2.19: policy

Listing 2.20: act

```
{\bf Definition} \ {\bf act} := {\bf nat}.
```

Listing 2.21: policyId

```
Definition policyId := nat.
```

Listing 2.22: preRequisite

```
Inductive preRequisite : Set :=
    | TruePrq : preRequisite
    | Constraint : constraint → preRequisite
    | ForEachMember : prin → nonemptylist constraint → preRequisite
    | NotCons : constraint → preRequisite
    | AndPrqs : nonemptylist preRequisite → preRequisite
    | OrPrqs : nonemptylist preRequisite → preRequisite
    | XorPrqs : nonemptylist preRequisite → preRequisite.
```

Listing 2.23: constraint

```
Inductive constraint : Set :=
    | Principal : prin → constraint
    | Count : nat → constraint
    | CountByPrin : prin → nat → constraint.
```

2.6 Semantics

In this section, we describe the semantics of ODRL0 language by a translation from agreements to a subset of many-sorted first-order logic formulas with equality. The semantics will help answer queries of the form "may subject s perform action act to asset a?". If the answer is yes, we say permission is granted. Otherwise permission is denied.

At a high-level, an agreement is translated into a conjunction of formulas of the form $\forall x (prerequisites(x) \to P(x))$ where P(x) itself is a conjunction of formulas of the form $prerequisites(x) \to (\neg) Permitted(x, act, a)$, where "Permitted (x, act, a)" means the subject x is permitted to perform action act on asset a.

2.6.1 Agreement Translation

The translation of an agreement returns the translation for a policySet per $prin_u$, the agreement's user and a, the asset.

 $[agreement \ for \ prin_u \ about \ a \ with \ ps] \triangleq [policySet]^{prin_u,a}$

2.6.2 Policy Set Translation

The translation for a policySet ($[policySet]^{prin_u,a}$) is described by translation formulas for each type of policySet. A policySet is either a PrimitivePolicySet, a PrimitiveExclusivePolicySet or a AndPolicySet.

2.6.2.1 PrimitivePolicySet Translation

Translation of a PrimitivePolicySet ($preRequisite \rightarrow policy$) yields a formula that includes a test on whether the subject is in the set of agreements' users, the translation of the policy and the translation of the prerequisite. Basically if the subject in question is a user of the agreement and the policySet prerequisites hold, then the policy holds. Translation of the policy for a PrimitivePolicySet is called a $positive\ translation$. A positive translation is one where the actions described by the policies are permitted.

Listing 2.25: Policy Set Translation: PrimitivePolicySet

```
[preRequisite \rightarrow policy]^{e,prin_u,a} \triangleq \forall x \ (([prin_u]_x \land [preRequisite]_x^{e,getId(p),prin_u,a}) \rightarrow [policy]_x^{positive,e,prin_u,a})
```

Listing 2.26: Positive Policy Translation: Single policy

```
[preRequisite \Rightarrow_{policyId} act]_{x}^{positive,e,prin_{u},a} \triangleq ([preRequisite]_{x}^{e,policyId,prin_{u}}) \Rightarrow Permitted(x, [act], a)
```

If the policy is a *AndPolicy*, the translation yields a conjunction of positive translations of each policy in turn.

Listing 2.27: Positive Policy Translation: List of policies

```
 \llbracket and[policy_1,...,policy_m] \rrbracket^{positive,e,prin_u,a} \triangleq \llbracket policy_1 \rrbracket^{positive,e,prin_u,a} \wedge ... \wedge \llbracket policy_m \rrbracket^{positive,e,prin_u,a}
```

2.6.2.2 PrimitiveExclusivePolicySet Translation

 $Primitive Exclusive Policy Set \ (pre Requisite \mapsto policy)$ yields the conjunction of two implications. The first implication, is the same as one found in the translation of Primitive Policy Set. The second implication however restricts access (to make the policy set exclusive) to only those subjects that are in the agreement's user. Translation of the policy in the second implication is called a $negative \ translation$. A negative translation is one where the actions described by the policies are not permitted.

Listing 2.28: Policy Set Translation: PrimitiveExclusivePolicySet

Listing 2.29: Negative Policy Translation: Single policy

```
 [preRequisite \Rightarrow_{policyId} act]_x^{negative,e,prin_u,a} \triangleq ([preRequisite]_x^{e,policyId,prin_u}) \Rightarrow \neg (Permitted(x, [act], a))
```

If the policy is a *AndPolicy*, the translation yields a conjunction of negative translations of each policy in turn.

Listing 2.30: Negative Policy Translation: List of policies

```
[\![and[policy_1,...,policy_m]\!]]^{negative,e,a} \triangleq [\![policy_1]\!]^{negative,e,a} \land ... \land [\![policy_m]\!]^{negative,e,a}
```

2.6.2.3 AndPolicySet Translation

And Policy Set translates to conjunctions of the corresponding policy set translations.

```
 [[and[policySet_1,...,policySet_m]]]^{e,prin_u,a} \triangleq [[policySet_1]]^{e,prin_u,a} \wedge ... \wedge [[policySet_m]]^{e,prin_u,a}
```

2.6.3 Principal Translation

Translation for a $prin([prin]_x)$ is a formula that is true if and only if the subject x is in the prin set. A prin is either a single subject or a list of subjects $(\{subject_1, ..., subject_m\}$ so the translation covers both cases.

If the prin is a single subject, the translation is a formula that is true if and only if the subject x is the same as the single subject subject.

2.6.3.1 Single Subject Translation

Listing 2.32: Prin Translation: Single subject

 $[subject]_x \triangleq x = subject$

2.6.3.2 List of Subjects Translation

Translation of a list of subjects is the disjunction of the translations for each subject.

Listing 2.33: Prin Translation: List of subjects

 $[\![\{subject_1,...,subject_m\}]\!]_x \ \triangleq \ [\![subject_1]\!]_x \ \lor \ ... \ \lor \ [\![subject_m]\!]_x$

2.6.4 Prerequisite Translation

Translation for a prerequisite is a formula $[prerequisite]_x^{[id_1,...,id_m],prin,a}$, where the set of ids refer to identifiers for policies that are implied by the prerequisites, prin is the agreement's user(s) (and to which the prerequisites apply), a is the asset and x is a variable of type subject. The translation for a prerequisite is described by translation formulas for each type of prerequisite. A prerequisite is either always true, a Constraint, a ForEachMember, a NotCons, a AndPrqs, a OrPrqs or a XorPrqs.

2.6.4.1 True Prerequisite Translation

The translation for a TruePrq yields a formula that is always true.

Listing 2.34: Prerequisite Translation: Always True Prerequisite

 $[prerequisite :: true] \triangleq True$

2.6.4.2 Constraint Prerequisite Translation

The translation for a *Constraint* is handled by a specialized constraint translation function (coverage of which starts at 2.41.

Listing 2.35: Prerequisite Translation: Constraint

$$[prerequisite :: constraint]_{x}^{[id_{1},...,id_{m}],prin_{u}} \triangleq [constraint]_{x}^{[id_{1},...,id_{m}],prin_{u}}$$

2.6.4.3 For Each Member Prerequisite Translation

The translation for a ForEachMember is also is handled by a specialized translation function (covered at 2.56.

Listing 2.36: Prerequisite Translation: ForEachMember

2.6.4.4 NotCons Prerequisite Translation

The translation for a NotCons yields a formula that is simply the negation of the translation for a constraint.

Listing 2.37: Prerequisite Translation: Not Constraint

```
[\![not\ prerequisite::constraint]\!]_x^{[id_1,...,id_m],prin_u} \triangleq \neg [\![constraint]\!]_x^{[id_1,...,id_m],prin_u}
```

2.6.4.5 And Prqs Prerequisite Translation

The translation for a AndPrqs yields a formula that is the conjunction of the translation for each preRequisite.

Listing 2.38: Prerequisite Translation: Conjunction

```
 [\![and\ [preRequisite_1,...,preRequisite_k]]\!]^{[id_1,...,id_m],prin_u} \triangleq [\![preRequisite_1]\!]^{[id_1,...,id_m],prin_u} \land ... \land [\![preRequisite_k]\!]^{[id_1,...,id_m],prin_u}
```

2.6.4.6 OrPrqs Prerequisite Translation

The translation for a OrPrqs yields a formula that is the inclusive disjunction of the translation for each preRequisite.

Listing 2.39: Prerequisite Translation: Inclusive Disjunction

2.6.4.7 XorPrqs Prerequisite Translation

The translation for a XorPrqs yields a formula that is the exclusive disjunction of the translation for each preRequisite.

Listing 2.40: Prerequisite Translation: Exclusive Disjunction

2.6.5 Constraint Translation

Translation for a constraint is a formula $[constraint]_x^{[id_1,...,id_m],prin_u,a}$, where the set of ids refer to identifiers for policies that are implied by the constraint, $prin_u$ is the agreement's user(s) (and to which the constraint applies), a is the asset and x is a variable of type subject. The translation for a constraint is described by translation formulas for each type of constraint. A constraint is either a Principal, a Count, or a CountByPrin.

2.6.5.1 Principal Constraint Translation

The translation for a *Principal* is handled by a specialized translation function (covered at 2.51.

Listing 2.41: Constraint Translation: Principal

```
\llbracket constraint :: prin \rrbracket_{x}^{[subject_{1}, \dots, subject_{m}]} \triangleq \llbracket prin \rrbracket_{x}^{[subject_{1}, \dots, subject_{m}]}
```

2.6.5.2 Count Constraint Translation

The translation for a *Count* is handled by a specialized translation function (covered at 2.58.

Listing 2.42: Constraint Translation: Count

```
\llbracket constraint :: count[N] \rrbracket_x^{[id_1, \dots, id_m], prin_u} \triangleq \llbracket count[N] \rrbracket_x^{[id_1, \dots, id_m], prin_u}
```

2.6.5.3 CountByPrin Constraint Translation

The translation for a CountByPrin is handled by the same specialized translation function as that for Count. The difference is that CountByPrin overrides the subjects in $prin_u$ by a different set of subjects (covered at 2.58.

Listing 2.43: Constraint Translation: Count by Principal

```
 | [constraint :: prin(count[N])]_x^{[subject_1, ..., subject_m], [id_1, ..., id_n]} \triangleq [prin(count[N])]_x^{[subject_1, ..., subject_m], [id_1, ..., id_n]}
```

2.6.6 for Each Member Translation

Listing 2.44: For Each Member Translation: Count by Principal

2.6.7 "Not Constraint" Translation

The translation for "Not Constraint" was listed in listing 2.37 earlier but we repeat it here to go along the Coq version.

Listing 2.45: Not Constraint Translation

```
 | [not \ constraint]_x^{[id_1,...,id_m],prin_u} \triangleq \neg [constraint]_x^{[id_1,...,id_m],prin_u}
```

2.6.8 Count Translation

2.6.8.1 Count Translation For Subject/ID Pair

The translation for Count or CountByPrin for a pair of subject and policy identifier is a formula that is true if the number of times the $subject_1$ has invoked a policy with policy identifier id_1 is smaller than N.

Listing 2.46: Count Translation: subject and policyId pair

```
\llbracket count[N] \rrbracket_x^{subject_1,id_1} \triangleq getCount(subject_1,id_1) < N
```

2.6.8.2 Count Translation For Subject/ID Pairs

The translation for Count or CountByPrin for subject and policy identifier pairs is a formula that is true if the total number of times that a subject has invoked a policy with policy identifier id_i is smaller than N.

Listing 2.47: Count Translation: subject and policyId pairs

2.7 Semantics in Coq

A predicate in Coq is any function that returns a term of type Prop. Here is how we have specified the Permitted predicate in Coq: ParameterPermitted : subject -> act -> asset -> Prop. So Permitted predicate takes a subject, an act (action) and an asset and returns a Prop. Note that the notation (\neg) indicates that Permitted may be negated.

Whether a permission is granted or denied depends on the agreements in question but also on the facts recorded in the environment. For ODRL0 those facts revolve around the number of times a policy has been used to justify an action (see 2.4.1 for more details on odrl0). We encode this information in an *environment* which is a conjunction of equalities of the form count(s, policyId) = n.

The Coq version of the count equality is a new inductive type called *count_equality*. An environment is defined to be a non-empty list of count_equality objects.

Listing 2.48: Environments and Counts

```
Inductive count_equality : Set :=
```

```
|\  \, {\tt CountEquality: subject} \rightarrow \  \, {\tt policyId} \rightarrow \  \, {\tt nat} \rightarrow \  \, {\tt count\_equality}. |\  \, {\tt Inductive environment: Set:=} \\ |\  \, {\tt SingleEnv: count\_equality} \rightarrow \  \, {\tt environment} \\ |\  \, {\tt ConsEnv: count\_equality} \rightarrow \  \, {\tt environment} \rightarrow \  \, {\tt environment}.
```

Translation of the top level *agreement* element proceeds by case analysis on the structure of the agreement. Note that each translation function takes an environment parameter.

Listing 2.49: Translation of agreement

```
Definition trans_agreement (e:environment)(ag:agreement) : Prop := match ag with | Agreement prin_u a ps \Rightarrow trans_ps e ps prin_u a end.
```

Translation of a policy Set takes as input $prin_u$, the agreement's user, and a, the asset, and proceeds by case analysis of different policy Set constructors and recursing into translation functions for the composing elements. A policy Set is either a Primitive Policy Set, Primitive Exclusive Policy Set or a And Policy Set.

The Coq version of the policy set translation function follows (listing 2.50).

Listing 2.50: Translation of Policy Set

```
Fixpoint trans_ps
 (e:environment)(ps:policySet)(prin_u:prin)(a:asset){struct ps} : Prop :=
let trans_ps_list := (fix trans_ps_list (ps_list:nonemptylist policySet)(prin_u:prin)
    (a:asset){struct ps_list}:=
 match ps_list with
  | Single ps1 ⇒ trans_ps e ps1 prin_u a
  | NewList ps ps_list' ⇒ ((trans_ps e ps prin_u a) /\ (trans_ps_list ps_list' prin_u a
    ))
 end) in
  match ps with
  | PrimitivePolicySet prq p \Rightarrow \forall x, (((trans_prin x prin_u) / )
                          (trans_preRequisite e x prq (getId p) prin_u)) →
                          (trans_policy_positive e x p prin_u a))
   | PrimitiveExclusivePolicySet prq p \Rightarrow \forall x, (((trans_prin x prin_u) / (trans_prin x prin_u)))
                                  (trans_preRequisite e x prq (getId p) prin_u)) →
                                 (trans_policy_positive e x p prin_u a)) /\
                                 ((not (trans_prin x prin_u)) \rightarrow (trans_policy_negative e)
    x p a)))
   | AndPolicySet ps_list ⇒ trans_ps_list ps_list prin_u a
   end.
```

Translation of a prin is a formula takes as input x, a variable of type subject and proceeds based on whether we have a single subject or a list of subjects.

Translation of a single $prin_u$ yields a formula that is true if and only if the subject x is the same as the single subject.

Listing 2.51: Translation of a Prin

```
\begin{split} & \texttt{Fixpoint trans\_prin} \\ & (\texttt{x:subject})(\texttt{p: prin}) \colon \texttt{Prop} := \\ & \texttt{match p with} \\ & | \texttt{Single s} \Rightarrow (\texttt{x=s}) \\ & | \texttt{NewList s rest} \Rightarrow ((\texttt{x=s}) \setminus / \texttt{trans\_prin x rest}) \\ & \texttt{end.} \end{split}
```

A positive translation for a policy p takes as input e, the environment, x, the subject, $prin_u$, the agreement's user, and a, the asset and proceeds based on whether we have a PrimitivePolicy or a AndPolicy. If the policy is a PrimitivePolicy an implication is returned which indicates x is permitted to do act to a, if the preRequisite holds.

Listing 2.52: Translation of a positive policy

```
Fixpoint trans_policy_positive
 (e:environment)(x:subject)(p:policy)(prin_u:prin)(a:asset){struct p} : Prop :=
let trans_p_list := (fix trans_p_list (p_list:nonemptylist policy)(prin_u:prin)(a:
    asset){struct p_list}:=
            match p_list with
              | Single p1 ⇒ trans_policy_positive e x p1 prin_u a
              \mid NewList p p_list' \Rightarrow
                 ((trans_policy_positive e x p prin_u a) /\
                  (trans_p_list p_list' prin_u a))
             end) in
 match p with
  | PrimitivePolicy prq policyId action \Rightarrow ((trans_preRequisite e x prq (Single
   policyId) prin_u) →
                                 (Permitted x action a))
  | AndPolicy p_list ⇒ trans_p_list p_list prin_u a
 end.
```

A negative translation for a policy p takes as input e, the environment, x, the subject, $prin_u$, the agreement's user, and a, the asset and proceeds based on whether we have a PrimitivePolicy or a AndPolicy. If the policy is a PrimitivePolicy an implication is returned which indicates x is forbidden to do act to a regardless of whether preRequisite holds.

Listing 2.53: Translation of a negative policy

The translation of a prerequisite takes as input e, the environment, x, the subject, $prin_u$, the agreement's user, and IDs, the set of identifiers (of policies implied by the prerequisite) and proceeds by case analysis on the structure of the prerequisite. A prerequisite is either a TruePrq, a Constraint, a ForEachMember, a NotCons, a AndPrqs, a OrPrqs or a XorPrqs.

The Coq version of the translate function for a *preRequisite* is given in 2.54. Note that in this listing the translations for *AndPrqs*, *OrPrqs* and *XorPrqs* have not yet been done.

Listing 2.54: Translation of a PreRequisite

The translation of a constraint takes as input e, the environment, x, the subject and IDs, the set of identifiers (of policies implied by the constraint) and proceeds by case analysis on the structure of the constraint. A constraint is either a Principal, a Count or a CountByPrin.

The Coq version of the translate function for a *constraint* is given in 2.55.

Listing 2.55: Translation of a Constraint

```
Fixpoint trans_constraint
  (e:environment)(x:subject)(const:constraint)(IDs:nonemptylist policyId)
  (prin_u:prin){struct const} : Prop :=
  match const with
   | Principal prn \Rightarrow trans_prin x prn

  | Count n \Rightarrow trans_count e n IDs prin_u

  | CountByPrin prn n \Rightarrow trans_count e n IDs prn

end.
```

The translation for forEachMember yields a formula that is true, if each subject mentioned in forEachMember is met by each constraint mentioned in forEachMember. Note that the agreement's user $prin_u$ may be overriden by a forEachConstraint constraint.

Listing 2.56: Translation of forEachMember

```
Fixpoint trans_forEachMember
      (e:environment)(x:subject)(principals: nonemptylist subject)(const_list:
   nonemptylist constraint)
      (IDs:nonemptylist policyId){struct const_list} : Prop :=
let trans_forEachMember_Aux
 := (fix trans_forEachMember_Aux
      (prins_and_constraints: nonemptylist (Twos subject constraint))
      (IDs:nonemptylist policyId){struct prins_and_constraints} : Prop :=
    match prins_and_constraints with
     | Single pair1 ⇒ trans_constraint e x (right pair1) IDs (Single (left pair1))
     | NewList pair1 rest_pairs ⇒
        (trans_constraint e x (right pair1) IDs (Single (left pair1))) /\
        (trans_forEachMember_Aux rest_pairs IDs)
    end) in
    let prins_and_constraints := process_two_lists principals const_list in
    {\tt trans\_forEachMember\_Aux\ prins\_and\_constraints\ IDs.}
```

Listing 2.57: Translation of not cons

```
Definition trans_notCons
  (e:environment)(x:subject)(const:constraint)(IDs:nonemptylist policyId)(prin_u:prin) :
     Prop :=
```

~ (trans_constraint e x const IDs prin_u).

Listing 2.58: Translation of count

References

- [1] Robby Robson Geoff Collier, Harry Piccariello. A digital rights management ecosystem model for the education community. *DRM Whitepapers: Content Guard*, 2004.
- [2] Riccardo Pucella and Vicky Weissman. A formal foundation for ODRL. CoRR, abs/cs/0601085, 2006.