Transfer Matrix Optical Modeling

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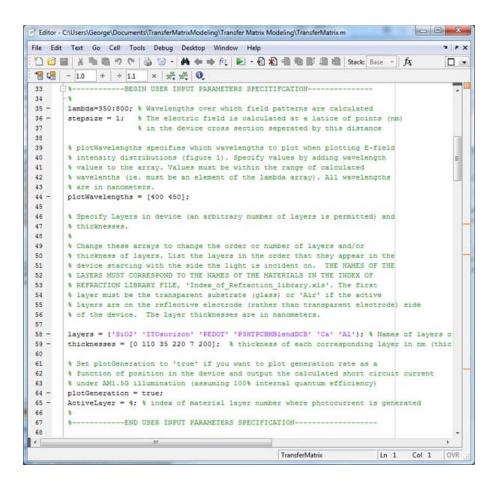
This document describes, briefly, how to use the Matlab script, TransferMatrix.m to calculate optical interference and absorption in multilayer stacks. This software uses the transfer matrix method, where transmission and reflection are calculated for each interface in the stack as well as attenuation in each layer. The theory behind this calculation is described in detail in the literature [1], 2] and will not be covered here. This model assumes normal incidence and does not take into account scattering.

The program consists of four files; the TransferMatrix.m file contains the main program as well as three helper functions. Using the program requires no knowledge of the code itself; however we have made every effort to thoroughly comment the code in case the user wishes to modify it. We will focus on how to use the program as designed to calculate optical fields in multilayers.

User definable parameters

All of the user definable parameters are defined at the top of the script:

lambda	array of wavelengths for which all values will be calculated. wavelength values must
	lie within the bounds of the wavelengths for which the optical constants (n and k) are
	defined in <i>Index_of_Refraction_library.xls</i> .
stepsize	numerical constant that defines the stepsize (in nanometers) between each point
	calculated in the spectrum.
plotWavelengths	array of wavelengths for which to plot interference patterns in the device. to add
	wavelengths, simply add elements to the vector.
layers	cell array of strings corresponding to the materials that compose each layer in the
	stack. these strings must correspond to the names used in the
	Index_of_Refraction_library.xls file (minus the '_n' or '_k' extension). the order of
	materials matters! light is incident on the stack "from the left"
thicknesses	vector describing the thicknesses of each layer (in nanometers). the thickness value at
	a given index in this vector corresponds to the thickness of the layer of the same index
	in layers.
plotGeneration	boolean switch. when true, TransferMatrix will include a plot of the generation rate as
	a function of thickness within the active layer of the device. if <i>plotGeneration</i> is set to
	true, activeLayer must be defined.
activeLayer	numerical constant that defines the index of the material responsible for photocurrent
	generation. this index corresponds to the index of the active material in the <i>layers</i> and
	thicknesses vectors. for instance, if layers = {'material1' 'material2' 'material3'} and
	material2 is the active layer, then activeLayer should be set to 2.



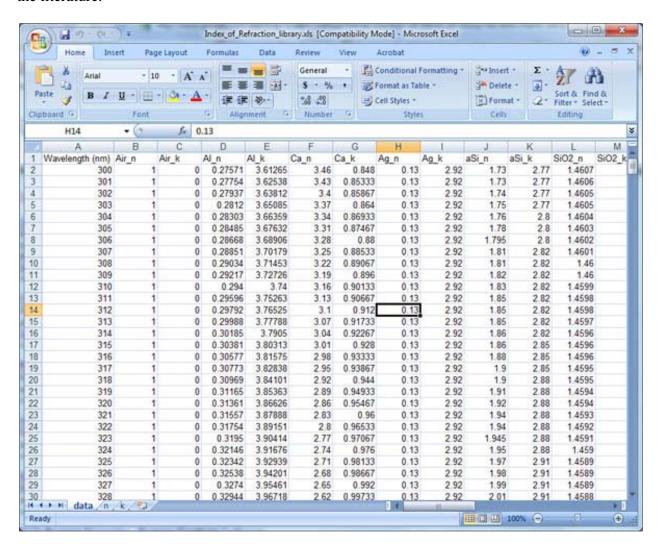
All user definable parameters are set within this section of code.

Index of refraction library file

The for each available material is defined the optical constant data in Index_of_Refraction_library.xls file. This file consists of wavelength-dependent optical constant data for each material. n and k are the real and imaginary parts of the complex index of refraction and are defined for each material at each wavelength. The names of the columns containing each set of data must follow the format, material n and material k, where material can be any designation for a material and _n and _k designate which column refers to n and k respectively. The first column must always be domain of wavelengths for which the material optical constants are defined.

We have provided optical constants for the materials we typically use. **Note: many materials' optical properties depend on processing conditions!** ITO deposited under different conditions can have drastically different optical constants and electrical conductivity (in our case, we purchase ITO coated glass substrates from Sorizon technologies and measured the optical constants using variable angle spectroscopic ellipsometry). Similarly, the optical constants of PEDOT:PSS and the P3HT:PCBM blend depend on doping density (in the case of PEDOT:PSS) and deposition technique, solvent, post-annealing temperature and time, and of course material quality (contamination and regioregularity). Therefore, while these results are typical, you may

wish to measure the optical constants of your materials or procure them from a supplier or from the literature.

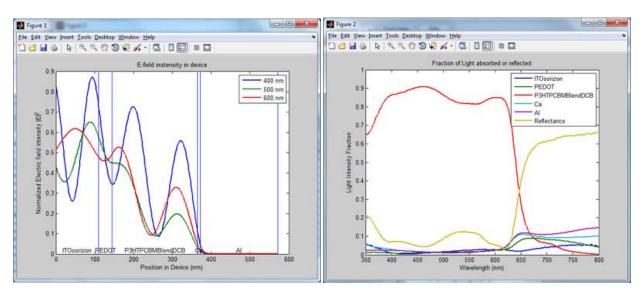


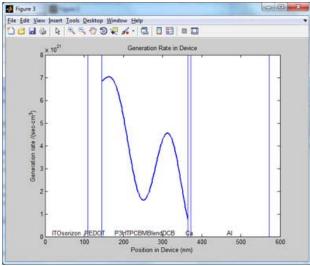
Example calculation

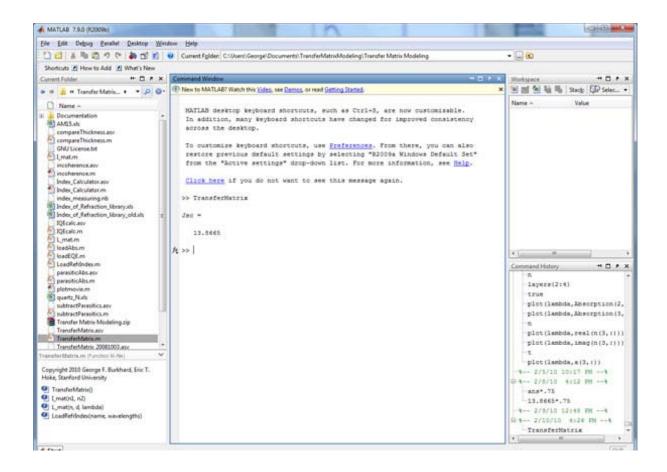
Suppose we want to calculate the optical properties for a typical poly-3-hexylthiophene:[6,6]-phenyl-C₆₁-butyric acid methyl ester (P3HT:PCBM) solar cell. A typical device structure consists of a glass substrate/ITO/PEDOT:PSS/P3HT:PCBM/Ca/Al (where PEDOT:PSS refers to poly(3,4-ethylenedioxythiophene) poly(styrenesulfonate)). The thickness of the glass substrate is not important as it is thick enough that interference effects have practically no effect. Typical thicknesses for the remaining layers are (in nm), 110/35/220/7/200. We are interested in the visible spectrum where the materials absorb (~350 nm - ~800 nm) and suppose we wish to see the interference patterns of 400, 500, and 600 nm light within the device. We would also like to see the position-dependent generation rate in the device. The user-defined parameters would then take the following values:

```
lambda=350:800;
stepsize = 1;
plotWavelengths = [400 500 600];
layers = {'SiO2' 'ITOsorizon' 'PEDOT' 'P3HTPCBMBlendDCB' 'Ca' 'Al'};
thicknesses = [0 110 35 220 7 200];
plotGeneration = true;
activeLayer = 4;
```

The script is then run either by pressing F5 in the editor or by typing, TransferMatrix at the Matlab command prompt (the current directory must be the directory containing the TransferMatrix.m file and associated .xls files). After a few seconds of computation, the results are plotted in four figure windows and the predicted short-circuit current (J_{sc}) is output in the command window (this assumes 100% *internal quantum efficiency* at all wavelengths).







By default, *TransferMatrix.m* creates variables, *absorption*, *reflection*, *parasitic_abs* and *lambda* in the base workspace when run. These arrays contain the absorption data for each material in the stack, the total reflection one would expect to measure from the device, the total parasitic absorption and the list of wavelengths for which these values correspond. This should be sufficient for most users, however, if you wish to output other local variables to the workspace (eg. E-field), you can add more *assignin('base'*, variable_name,local_variable) commands to the end of the main function.

TransferMatrix_VaryThickness.m

This additional Matlab script calculates the short circuit current that would be obtained if the device had an IQE of 100% as the thickness of one of the layers is varied over values specified by the user. The program generates a graph of the short circuit current (in mA/cm²) versus the thickness of the layer. It also creates the variables *Jsc* and *Thickness* in the base workspace containing the short circuit current data and the layer thicknesses which the currents correspond to. The methods and parameters are the same as for *TransferMatrix.m* except for the following additional parameters:

LayerVaried	numerical constant that defines the index of the material layer that will be varied in
	thickness. this index corresponds to the index of the active material in the <i>layers</i> and
	thicknesses vectors. for instance, if layers = {'material1' 'material2' 'material3'} and

	you want to vary the thickness of material2, then <i>LayerVaried</i> should be set to 2.
VaryThickness	numerical constant 1D array that defines the different thicknesses values for the layer
	which will be varied in thickness (LayerVaried). for instance if you would like to
	calculate the short circuit current for devices where one layer is 50, 60, 70 or 80nm
	then set <i>VaryThickness</i> = [50 60 70 80]; or <i>VaryThickness</i> = 50:10:80;

References

- [1] L. A. A. Pettersson, L. S. Roman, O. Inganas, J. Appl. Phys. 1999, 86, 487.
- [2] P. Peumans, A. Yakimov, S. Forrest, J. of Appl. Phys. 2003, 93, 3693.