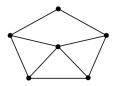
## Math 390: Practice Problems for Quiz 2

## Problems from the book

4 <sup>th</sup> Edition	$5^{\text{th}} \text{ Edition}$
Section 17: 17.1, 17.3	Section 5.1: 5.1, 5.3
Section 21: 21.1, 21.2(i)	Section 5.2: 5.9, 5.11(i)
Section 29: 29.4	Section 6.3: 6.21

## **Additional Problems**

1. For each of the following graphs, compute the chromatic number  $\chi(G)$  of the graph, and show a coloring that uses the minimum number of colors.



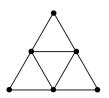




2. For each of the following graphs, compute the chromatic index  $\chi'(G)$  of the graph, and show an edge-coloring that uses the minimum number of colors.

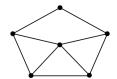






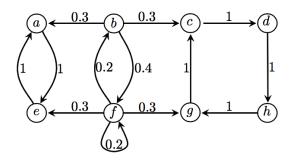
3. For each of the following graphs, compute the chromatic polynomial  $P_G(k)$ .



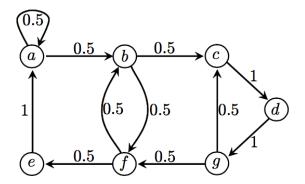




4. Consider the following Markov chains:

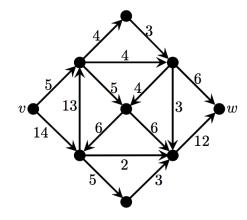


- (a) Which states in the Markov chain are persistent? Which states are transient?
- (b) For each state of the Markov chain, determine whether the state is periodic. If it is periodic, what is its period?
- (c) Is the Markov chain ergodic?
- 5. Consider the following Markov chains:



- (a) Which states in the Markov chain are persistent? Which states are transient?
- (b) For each state of the Markov chain, determine whether the state is periodic. If it is periodic, what is its period?
- (c) Is the Markov chain ergodic?
- 6. There are two competing cellphone companies in a city, Company A and Company B. In 2015, 40% of the people in the city use Company A, and 60% of the people use Company B. Each year 40% of the people who who use Company A switch to using Company B, and 30% of the people who use Company B switch to using Company A. (Assume that everyone in the city has a cellphone with either Company A or Company B.)
  - (a) Model this situation with a Markov chain. Find the transition matrix and associated digraph that describes the number of people using each company.
  - (b) What percent of people will use Company A in 2016?
  - (c) Assuming the trend continues, what fraction of people will use Company A in the long run?

## 7. Consider the following network:



- (a) Find a maximum flow in the above network.
- (b) Fine a minimum cut in the above network.