A Parallel Application of the Fourier Transformation

Justin Spidell – Brett Sumser

October 2021

Abstract

A Fourier transform is a mathematical transform decomposing functions based on space and time into functions based on spatial or temporal frequency. The Fourier transform is denoted by adding a circumflex to the symbol of a function:

$$f \to \hat{f}$$

The Fourier transform is defined as:

$$\hat{f}(\xi) = \int_{-\infty}^{\infty} f(x) e^{-2\pi i x \xi} dx \tag{1}$$

Whereas the inverse Fourier transform is denoted as:

$$f(x) = \int_{-\infty}^{\infty} \hat{f}(\xi) e^{2\pi i x \xi} d\xi \tag{2}$$

Introduction

The Fourier Transform is an important mathematical concept. It has applications in digital signal processing, convolution in neural networks, image recognition and even speech processing. The main idea behind the Fourier Transform is that it is a ”mathematical operation that changes the domain (x-axis) of a signal from time to frequency,” [4]. The particular use case for the Fourier Transform that initially started this project was that of digital signal processing, specifically the conversion of analog signals to digital for guitar effects processing.

Parallelization

There are a few different directions to explore when developing a more parallized implementation of the Fourier Transform. According to Anthony Blake in his thesis paper titled "Computing the Fast Fourier Transform on SIMD Microprocessors", use of the FFT algorithm is extremely widespread in multiple disciplines. He goes on to state that "use of the FFT is even more pervasive, and it is counted among the 10 algorithms that have had the greatest influence on the development and practice of science and engineering in the 20th century," [1]. The widespread use of the FFT algorithm provides great evidence for the need to optimize for different applications, and to understand the methods that can be used to achieve this. Two methods of Parallelization that stand out in particular are SIMD, and multithreading.

This is a test citation. [2] This is a test citation. [3]

SIMD

Multithreading

References

[1] Anthony Blake. Computing the fast fourier transform on simd microprocessors, 2012.

[2] Donald E. Knuth. Literate programming. *The Computer Journal*, 27(2):97–111, 1984.

[3] Bo Liu. Parallel fast fourier transform, N/A.

[4] Cory Maklin. Fast fourier transform, 2019.