

⑥ the ~~reconstruct~~ reconstruction formula is given by

$$s(t) = \sum_{n=-\infty}^{+\infty} s[n] \operatorname{sinc}(2\omega t - n)$$

where  $\operatorname{sinc}(z) \triangleq \begin{cases} \frac{\sin \pi z}{\pi z} & z \neq 0 \\ 1 & z = 0 \end{cases}$

Since  $h^I(z), h^Q(z), x^I(t), x^Q(t), y^I(t), y^Q(t)$  are band limited baseband signals, and so are  $h(z), x(t)$  and  $y(t)$ . Using the sampling theorem we therefore have

$$h(z) = \sum_{n=-\infty}^{\infty} h[n] \operatorname{sinc}(2\omega \frac{z}{2} - n)$$

$$x(t) = \sum_{n=-\infty}^{\infty} x[n] \operatorname{sinc}(2\omega t - n)$$

$$y(t) = \sum_{n=-\infty}^{\infty} y[n] \operatorname{sinc}(2\omega t - n)$$

$$h[n] \triangleq h(z = \frac{n}{2\omega}), \quad x[n] \triangleq x(t = \frac{n}{2\omega}), \quad y[n] \triangleq y(t = \frac{n}{2\omega}). \quad \text{--- ⑦}$$

Therefore in ⑦ we have

$$y[n] = y(t = \frac{n}{2\omega}) = \frac{1}{2} \int h(z) x(\frac{n}{2\omega} - z) dz. \quad \text{--- ⑧}$$

using the sampling theorem expansions from ⑧ in ⑤ we have