



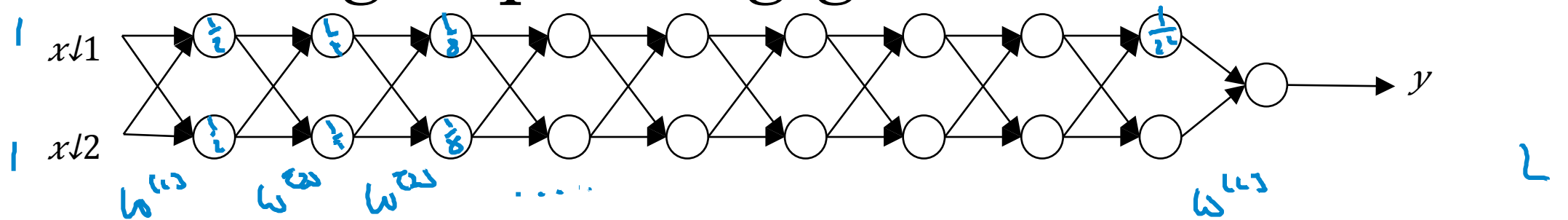
deeplearning.ai

Setting up your  
optimization problem

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Vanishing/exploding  
gradients

# Vanishing/exploding gradients



Handwritten notes:  $g(z) = z$  and  $b^{(L)} = 0$ .

Handwritten equation:  $\hat{y} = w^{(L)} \left( w^{(L-1)} \left( w^{(L-2)} \dots \right) \right)$

Handwritten equation:  $a^{(L)} = w^{(L)} x$

Handwritten notes:  $1.5^L$  and  $0.5^L$

Handwritten note:  $w^{(1)} > I$

Handwritten note:  $w^{(2)} < I$  with matrix  $\begin{bmatrix} 0.9 & 0 \\ 0 & 0.9 \end{bmatrix}$

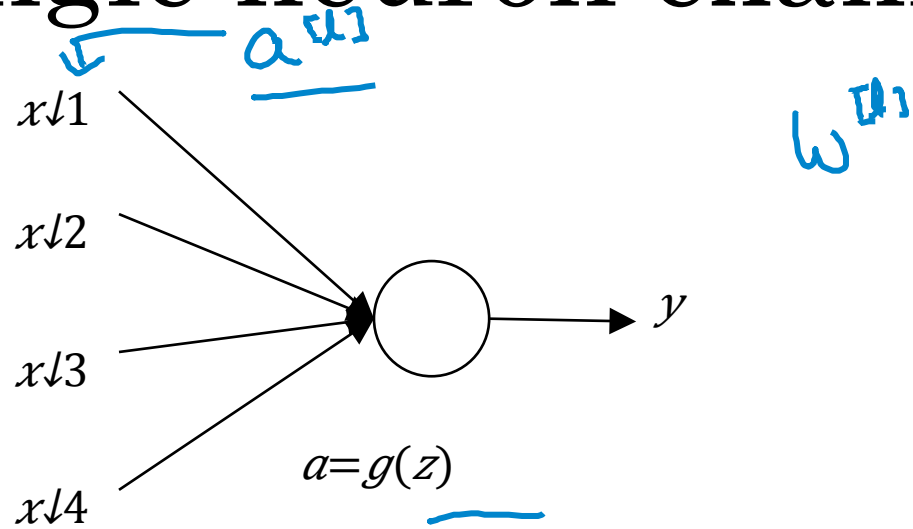
Handwritten equation:  $w^{(L)} = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}$

Handwritten equations:  $z^{(1)} = w^{(1)} x$ ,  $a^{(1)} = g(z^{(1)}) = z^{(1)}$ , and  $a^{(2)} = g(z^{(2)}) = g(w^{(2)} a^{(1)})$

Handwritten equation:  $\hat{y} = w^{(L)} \left[ \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}^{L-1} x \right]$

Handwritten notes:  $1.5^{L-1} x$  and  $0.5^{L-1} x$

# Single neuron example



$$z = w_1 x_1 + w_2 x_2 + \dots + w_n x_n$$

large  $n \rightarrow$  Smaller  $w_i$

$$\text{Var}(w_i) = \frac{1}{n} \frac{2}{n}$$

$$\underline{w^{[1]}} = \text{np.random.randn}(\text{shape}) * \text{np.sqrt}\left(\frac{2}{n^{[1-1]}}\right)$$

ReLU  $g^{[1]}(z) = \text{ReLU}(z)$

Other variants:

$$\text{tanh} \quad \frac{1}{n^{[1-1]}}$$

Xavier initialization  $\uparrow$

$$\sqrt{\frac{2}{n^{[1-1]} + n^{[1]}}}$$

$\uparrow$