2-Party Secure Computation: A Survey of BetterYao Ben Terner

${f 1}$ Introduction

This survey will give an overview of the BetterYao implementation of secure computation against malicious adversaries, as described by [1] and [2] and implemented in [3]. This survey assumes familiarity with circuit garbling techniques, which are explained in another survey for reference.

1.1 Notation

We will discuss the protocol for securely evaluation a function $f(x,y) = (f_1(x,y), f_2(x,y))$ by two players P_1 and P_2 , where P_1 's input is x, P_1 's output is f_1 , P_2 's input is f_2 , and f_2 's output is f_2 . In our protocols, one of the players will take the role of *generator* and one will take the role of *evaluator*, or *Gen* and *Eval*, respectively. Without loss of generality, we can assume that f_2 will be f_2 will be f_2 will be f_2 .

For each wire w_i in the circuit, Gen randomly picks two keys, $K_{i,0}$, $K_{i,1}$, and a permutation bit π_i . Each key is the length of the security parameter k. The *label* for each wire w_i consists of the pair $(K_{i,b}, b \oplus \pi_i)$ and is denoted $W_{i,b}$.

2 An Honest-But-Curious Protocol

We first describe a protocol for secure two-party computation by Yao that is secure in the honest-but-curious setting, and then explain potential attacks by malicious players and the mechanisms by which we enforce proper behavior or dampen the capabilities of attacks.

Gen will construct a circuit, gate by gate, according to Yao's protocol [4] and send each gate to Eval, as well as proper input keys for each of Gen's inputs. Eval and Gen will use OTs in order for Eval to retrieve the proper keys for her own inputs. Gen also sends the random permutation bit π for each of the circuit output wires so that Eval can identify their semantic values.

So that Eval cannot trivially read the values of Gen's output wires, Gen constructs the circuit to produce his output masked with one-time pad c. Gen keeps the value of c private and uses it to decrypt his output after receiving it from Eval, although keys for c must be also provided to Eval.

3 Attacks

3.1 Malicious Eval

The two-party protocol we describe is not fair in the sense that if Eval does not want to, she does not have to send Gen his outputs, but in this case Gen knows that Eval has cheated. Eval can behave maliciously against Gen in two other ways during this protocol: she can attempt to learn Gen's outputs or she can report false outputs to Gen. We will refer to these as attacks against Gen's Output Outp

3.2 Malicious Gen

3.2.1 Generator's Input Consistency

Because we achieve security in the malicious protocol using Cut and Choose, Gen and Eval execute the Yao protocol on many circuits. Gen could attack Eval by providing inconsistent inputs to Eval in the evaluation

circuits. Lindell and Pinkas [5] showed that for some functions, this could leak some information about Eval's inputs.

3.2.2 Selective Failure

Gen could infer information about Eval's inputs by providing a incorrect keys to Eval during OT that will force circuit decryption to fail. For example, a malicious Gen could assign keys (K_0, K_1) to one of Eval's input wires when garbling a circuit but use (K_0, K_1^*) in the OT, where $K_1 \neq K_1^*$. If Eval's input is 1, decryption of the first gate will fail and Eval will have to abort, indicating to Gen that her input was 1. If Eval's input is 0, then Gen discovers her input by the knowledge that decryption of the circuit did not fail.

4 Security in the Malicious Setting

4.1 Cut and Choose

Before explaining defenses to specific concerns about *Gen* and *Eval* acting maliciously, we first discuss the *Cut and Choose* technique for circuit evaluation in the malicious setting. Intuitively, *Gen* will construct many circuits (the number determined by some security parameter) and send them to Eval, or at least commit to them. *Gen* and *Eval* will collaboratively choose some of the circuits at random to become "check circuits," with the rest being "evaluation circuits." *Gen* will reveal the private randomness used to construct the "check circuits," and *Eval* will verify their authenticity. *Eval* will evaluate the "evaluation circuits" as in the Yao protocol and select the output of the majority circuit as the protocol's output. However, for security purposes, *Gen* cannot know which circuits are check circuits and which are evaluation circuits, since if he did, he might change a circuit's output by switching the output keys for intermediate gates.

[1] showed that a 3:2 ratio of check circuits to evaluation circuits is near optimal (and better than 1:1). Eval performs random seed checking. Explain the checks that Eval performs and what she has to do in order to perform the checks. There's a piece missing somewhere about how to compute the hash of a circuit.

4.2 Defenses Against Malicious Eval

4.2.1 Gen's Output Privacy

As explained in Section 2, Gen's input privacy can be protected using a one-time pad circuit composed entirely of XOR gates. This does not change for the malicious setting.

4.2.2 Gen's Output Authenticity

At the end of circuit evaluation, Eval has outputs for both herself and Gen. Our protocol is not fair because Eval is not required to send Gen his outputs, but if Eval chooses to, she may attempt to deceive Gen. To convince Gen that Eval has been honest and to satisfy Gen's concerns, they use a witness-indistinguishable proof.

Proof of Gen's Output Authenticity

Private Inputs

Gen has the output keys $\{(u_0^j, u_1^j)\}_{j \in [s]}$. Eval knows the index $m \in [s]$ of the majority circuit and the random key ν corresponding to Gen's output wire of value a.

is $\nu = u_a^m$? This is the best I can tell.

Shared Inputs

Gen and Eval share the security parameter 1^k , statistical parameter 1^s , the commitments to Gen's output keys $\{(com(u_0^j), com(u_1^{(j)}))\}_{j \in [s]}$, and Gen's output a.

- 1. Gen chooses a random nonce $r \in \{0,1\}^k$ and he encrypts it with each gate key $u_a^{(j)}$. He sends Eval the encryptions $enc_{u_a^{(1)}}(r)||enc_{u_a^{(2)}}(r)||\cdots||enc_{u_a^{(s)}}(r)=c^{(1)}||c^{(2)}||\cdots||c^{(s)}|$
- 2. Eval commits to the decryption of $c^{(m)}$ and sends it to Gen. Formally, she sends $com(dec_v(c^m)) = com(r')$ to Gen.
- 3. Gen receives r' and then decommits to all of the keys $\{u_a^{(j)}\}_{j\in[s]}$
- 4. Eval checks Gen's decommitments to determine if:
 - (a) $com(u_a^j)$ correctly decommits to $u^{(j)}$ for $j \in [s]$
 - (b) $dec_{u^{(i)}}(c^{(i)}) = dec_{u^{(j)}}(c^{(j)})$ for all $i, j \in [s], i \neq j$

If any of the checks fails, Eval aborts. Otherwise, Eval decommits to r'

5. Gen checks that com(r') decommits properly to r. If so, he accepts. Otherwise, he rejects.

4.3 Defense Against Malicious Gen

4.3.1 Gen's Input Consistency

The intuition to defend against this attack is to supplement our objective circuit with a 2-universal hash circuit that will compute some function over Gen's inputs which Eval can verify for each circuit evaluation. It's critical that the hash function is both hiding and collision-free. Simply, to preserve the privacy property of the protocol, the output of the hash circuit should reveal no information to Eval about Gen's inputs. Collision-freeness effectively binds Gen to his inputs; because two inputs are hard for Gen to find that will evaluate to the same hash, Gen must use the same semantic inputs for each garbled circuit that uses the same hash circuit (and because all garbled circuits use the same hash circuit, Gen's input must be consistent). Two-Universal hash circuits satisfy the binding property by definition, since they fulfill the requirement that for fixed, distinct inputs x and y, the probability that a random hash function $h: A \to B$ satisfies h(x) = h(y) is at most 1/|B|.

It follows that if x_i is Gen's input to evaluation circuit i, then the consistency of the hashes $h(x_1), h(x_2), ..., h(x_n)$ will imply the consistency of each x_i with probability at least 1 - 1/|B|. Because the difficulty of finding collisions for 2-Universal hash functions is defined with a posteriori knowledge of the inputs x and y, the hash function must be chosen during the protocol after Gen commits to his inputs. Here, Gen commits to his input keys rather than his actual inputs in order to preserve privacy during the reveal phase.

It is not sufficient to simply add an auxiliary 2-Universal hash circuit to the protocol, since for circuits where Gen has few inputs, Eval can simply run all possible inputs by Gen through the hash circuit to find a matching hash and learn Gen's inputs. In addition, the 2-Universal hash circuit must also be randomized (or, in a sense, salted). [2] use the Leftover Hash Lemma to show that Gen must pick 2k + lg(k) bits of fresh randomness at the beginning of the protocol as input to this hash function in order to achieve security according to parameter k, and that the output of the 2-Universal hash function will appear pseudorandom even if the hash function is made public.

The hash function is chosen from the family

$$\mathcal{M} = \{h_M | M \in \{0, 1\}^{m \times n} \land h_M(x) = M \cdot x \text{ for some } m, n \in \mathbb{N}\}$$

which has the advantage that the hash circuit can be computed with only XOR-gates, making the computation overhead to the protocol minimal when using free-XOR.

4.3.2 Selective Failure

At a high level, he defense for this attack, first given by [5], is to provide a transformation that converts Eval's true input y into the her protocol input \overline{y} , and have an auxiliary circuit convert \overline{y} back into y during circuit evaluation. Eval does this by choosing some $M \in \{0,1\}^{n \times m}$ for some $m \in \mathbb{N}$ and computes $M \cdot \overline{y} = y$. This technique requires that the Gen be unable to infer any information about y from knowledge he may gain about \overline{y} . We require the following definition:

 $M \in \{0,1\}^{n \times m}$ for some $n,m \in \mathbb{N}$ is called k-probe-resistent for some $k \in \mathbb{N}$ if for any $L \subset \{1,2,...,n\}$, the Hamming distance of $\bigoplus_{i \in L} M_i$ is at least k, where M_i denotes the i-th row of M.

If M is k-probe-resistent for some parameter k, then Gen will have negligible probability of inferring information about Eval's input y from the protocol input \overline{y} , even if M is made public and computed exclusively with XOR gates.

Lindell and Pinkas [5] point out that as long as m is big enough, the M will not be k-probe-resistant with negligible probability. Although [5] choose m to be max(4n, 8k), [2] give a probabilistic algorithm that produces k-probe-resistant matrix M such that $m \leq lg(n) + n + k + max(lg(4n), lg(4k))$. The algorithm follows:

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Input: Eval's input size n and security parameter 1^k
Output: k-probe-resistent matrix M \in \{0,1\}^{n \times m} for some m \in \mathbb{N}
t \leftarrow \lceil \max(lg(4n), lg(4k)) \rceil \ // find the minimum t such that 2^t \geq k + (lg(n) + n + k)/t
while 2^{t-1} > k + (lg(n) + n + k)/(t-1) do
t \leftarrow t - 1
end while
K \leftarrow \lceil (lg(n) + n + k)/t \rceil
N \leftarrow K + k - 1
for i \leftarrow 1 to n do
\text{Pick } P(x) = a_0 + a_1 x + a_2 x^2 + ... + a_{K-1} x^{K-1}, where a_i \xleftarrow{\$} \mathbb{F}_{2^t}
M_i \leftarrow \lceil P(1)_2 || P(2)_2 ||... || P(N)_2 \rceil \ // where P(j)_2 denotes a t-bit row vector end for
return M // M \in \{0,1\}^{n \times m}, where m = Nt
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I still don't understand this. The coefficients are drawn from \mathbb{F}_{2^t} and used to find points in \mathbb{F}_{2^t} , and then points in the polynomial from 0 to N are concatenated to get a point in \mathbb{F}_{2^k} ? TODO: error correction codes

The algorithm constructs a k-probe-resistant matrix M by randomly picking polynomials $P_1, P_2, ..., P_n \in \mathbb{F}_{2^t}[x]$ with degree at most K-1,where n is the evaluator's input size. The polynomials are evaluated at points $x_1, x_2, ... x_N \in \mathbb{F}_{2^t}$, and the outputs for each P_i over the points are concatenated as a $N \cdot t$ -bit vector which becomes the i-th row of M.

5 Performance Considerations

This section details a couple of engineering improvements to reduce the amount of computation and communication involved in the protocol.

5.1 Pipelining Evaluation

When circuits become millions or billions of gates large, it becomes infeasible to retain the entire circuit in memory, especially when multiple circuits must be evaluated to attain security in the malicious setting. HEKM [6] showed that holding entire circuits in memory is unnecessary, as *Gen* and *Eval* can execute the

protocol while only retaining gates in memory that they need at the moment. To do this, Gen and Eval evaluate all of the circuits in lockstep and pipeline the garbling of gates with their evaluation. Gen garbles σ gates at once, all corresponding to the same gate in the evaluation circuit, and sends them to Eval together. While Gen is garbling, Eval evaluates the last batch that Gen sent.

explain issues with random seed checking and hash construction

5.2 Gate Communication

Recall that 60% of the circuits in our protocol are check circuits, but Gen does not know which circuits are check circuits and which are evaluation circuits. We'd like to find a way to prevent Gen from having to send all of the garbled gates over the communication channel when he only really needs to send 40% of them. Let the statistical security parameter used to decide the number of evaluation circuits be σ , and let μ be the number of check circuits. Gen should only have to communicate $\sigma - \mu$ pieces of information, one per evaluation circuit, in order for Eval to infer all of the garbled gates $\{g_0, g_1, \ldots, g_{\sigma-1}\}$.

To do this, Gen considers all of the garbled gate descriptions $\{g_0, g_1, \dots, g_\sigma\}$ to be coefficients of a polynomial,

$$P(x) = g_0 + g_1 x + g_2 x^2 + \dots + g_{\sigma-1} x^{\sigma-1}$$

and sends $Eval \ \sigma - \mu$ points of the polynomial $P(1), P(2), \dots, P(\sigma - \mu)$. Eval can now use the coefficients she generates from the check circuits and polynomial interpolation to recover the gates she does now know. This technique sacrifices this small amount of communication overhead to save 60% of the communication cost.

polynomial interpolation.

5.3 Random Seed Checking

Communication cost of check circuits is independent of circuit size.

6 A Protocol Secure Against Malicious Adversaries

We now describe the full protocol for [fast] secure two-party computation in the malicious setting.

Private Inputs: Gen's private inputs to the protocol are $x_i \in x$ and Eval's private inputs to the protocol are $y_i \in y$.

Shared Inputs: Gen and Eval agree upon a function $f:(x,y)\to (f_1,f_2)$. Gen and Eval also agree on a security parameter 1^k and a statistical parameter 1^σ . They use a commitment scheme com and a symmetric encryption scheme (enc. dec).

Notation: Gen's inputs \overline{x} (described in step 1) have length m_1 and Eval's inputs \overline{y} (described in step 1) have length m_2 . Consider any input key $K_{b,i}^{(j)} \in \{0,1\}^k$. K has length k and semantic value $k \in \{0,1\}$, is a key for the k wire k in its circuit, and belongs to circuit k. Let k be the k label corresponding to the k wire k in circuit k such that k label semantic value k. (k label semantic value).

1. Input Modification

Gen generates randomness $r \in \{0,1\}^{2k+\lg(k)}$, which will be used as input to the 2-Universal circuit described in section 4.3.1. Gen also generates a one-time pad e which will be used to mask his outputs, as described in section 4.2.1. Eval computes her k-probe-resistant matrix M (as described in section 4.3.2) and input \overline{y} such that $M \cdot \overline{y} = y$. Gen's input is now $\overline{x} = x||e||r$ and Eval's input is now \overline{y} .

2. Gen Randomly Generates Input Keys

Gen generates randomness $\{\rho^{(j)}\}_{j\in\sigma}$, where $\rho^{(j)}$ corresponds to the randomness used for the jth circuit.

He uses each $\rho^{(j)}$ to generate input keys and permutation bits $(K_{0,i}^{(j)}, K_{1,i}^{(j)}, \pi_i^{(j)}) \in \{0,1\}^{2k+1}$ for $i \in \overline{x}$ for each circuit $j \in \sigma$.

How much randomness does Gen need, or equivalently, how long should the seed ρ be?

3. Gen Commits to His Input

Gen generates new randomness $\gamma_i^{(j)}$ (independent of $\rho^{(j)}$) for $i \in \overline{x}$ and $j \in \sigma$ and commits to all of the keys that correspond to his circuit inputs. He sends $\Gamma = \{com(W_{i,b}^{(j)}; \gamma_i^{(j)})\}_{i \in \overline{x}}$ to Eval.

4. Agreement on the Objective Circuit

Eval announces M to Gen and then Gen and Eval run an interactive coin-flipping protocol to generate the two-universal circuit $H \in \{0,1\}^{k \times m_1}$ used to compute a hash over Gen's inputs. They now both know the full objective circuit C to compute $g: (\overline{x}, \overline{y}) \to (\bot, (h, c, g_2))$ where $h = H \cdot \overline{x}$, $c = g_1 \oplus e$, $g_1 = f_1(x, M \cdot \overline{y})$, and $g_2 = f_2(x, M \cdot \overline{y})$.

5. Gen Commits to Input and Output Labels

Gen uses $\rho^{(j)}$ to generate input keys for Eval's inputs and output keys for his own outputs.

Does *Gen* generate entire circuits here, or are these keys enough? It should be implied that *Gen* must actually generate the whole circuit in order to get the output keys.

He then sends $(\Theta^{(j)}, \Omega^{(j)}, \Phi^{(j)})_{j \in \sigma}$ to Eval, where Θ represents Gen's input labels, Ω represents Eval's input labels, and Φ represents Gen's output labels (specifically, the values of c):

(a) $\Theta^{(j)} = \{com(W_{i,0 \oplus \pi_i^{(j)}}^{(j)}; \theta_i^{(j)}), com(W_{i,1 \oplus \pi_i^{(j)}}^{(j)}; \theta_i^{(j)})\}_{i \in m_1}$ where θ is randomness used in the commitment.

Do the θ s in the above (which represent randomness for the commitment) need to be separate, or even independent?

To protect Gen's input privacy, the labels for each wire's 0 input and 1 input are permuted by (re)using the permutation bit π .

- (b) $\Omega = \{com(W_{i,0}^{(j)}; \omega_i^{(j)}), com(W_{i,1}^{(j)}; \omega_i^{(j)})\}_{i \in m_2}$ where ω is randomness used in the commitment. Unlike Gen's inputs labels, Gen does not permute Eval's input labels. She will need to know their ordering, and her inputs will be protected by OT in step 6.
- (c) $\Phi = \{com(W_{i,0}), com(W_{i,1})\}_{i \in c}$

Does Φ not require randomness in its commitments? Why?

Eval will discover the semantics of these wires anyway (in step ??), so there is no need to permute them.

6. Eval's Input OTs

For every $i \in \overline{y}$, Gen and Eval perform $\binom{2}{1}$ OTs for Eval's input, where Gen's input is $(\{W_{i,0}^{(j)}, W_{i,1}^{(j)}\}_{j \in \sigma})$ and Eval's input is \overline{y}_i . For each semantic value of \overline{y}_i , Gen sends the concatenation of the entire set of input keys over all j circuits.

We denote the set of decommitments that Eval receives for each circuit as $Y^{(j)} = \{(W_{i,\overline{y}_i}^{(j)},\omega^{(j)})\}.$

7. Cut and Choose

Eval randomly chooses $S \subset [\sigma]$ such that $S = 2\sigma/5$. Use the string $s \in \{0,1\}^{\sigma}$ to describe the circuits that Eval has chosen for cut-and-choose by denoting $s_j = 1$ if $j \in S$ and $s_j = 0$ otherwise. Gen and Eval perform cut-and-choose by doing σ $\binom{2}{1}$ OTs, where Eval's input is s_j and S_j and S_j input is S_j input i

Eval chooses a circuit as an evaluation circuit, she learns the de-commitments to Gen's input keys (which will be checked) and can evaluate the circuit.

are Gen's inputs to the OT the same length? Do we need padding?

Note: the OTs in 7 can all be run in parallel, as can the OTs in step 6, and they can be run in parallel with each other.

8. Circuit Garbling

For every garbled gate $g: \{0,1\} \times \{0,1\} \to \{0,1\}$ with input wires w_a, w_b and output wire w_c , Gen computes the garbled truth table:

$$G(g)^{(j)} = (\langle \pi_a^{(j)}, \pi_b^{(j)} \rangle, \langle \pi_a^{(j)}, 1 \oplus \pi_b^{(j)} \rangle, \langle 1 \oplus \pi_a^{(j)}, \pi_b^{(j)} \rangle, \langle 1 \oplus \pi_a^{(j)}, 1 \oplus \pi_b^{(j)} \rangle)$$

where
$$(\langle h_{\alpha}, h_{\beta} \rangle) = enc_{K_{a,h_{\alpha}}^{(j)}}(enc_{K_{b,h_{\beta}}^{(j)}}(W_{c,g(h_{\alpha},h_{\beta})}^{(j)})).$$

come back to this equation.

Gen sends $\{G(C)^{(j)}\}_{j\in\sigma}$ to Eval, where $G(C)^{(j)} = (\{G(g)^{(j)}\}_{g\in C}, \{\pi_i^{(j)} : w_i \text{ is an output wire }\})$

talk about using optimizations described above in communication (and talk about them!)

9. Checking Garbled Circuits

Eval must verify both check circuits and evaluation circuits.

(a) Check Circuits

For every $j \in [\sigma] \setminus S$, Eval uses $\rho^{(j)}$ to regenerate $\{\Theta^{(j)}, \Omega^{(j)}, \Phi^{(j)}\}$ received in step 5 and reconstruct $G(C)^{(j)}$.

(b) Evaluation Circuits

For every $j \in S$, Eval checks:

- i if the *i*th entry of $X_1^{(j)}$ received in step 7 successfully decommits the *i*th entry in $\Gamma^{(j)}$ received in step 3.
- ii if the *i*th entry of $X_2^{(j)}$ received in step 7 successfully decommits the $(2 \cdot i + \overline{x}_i \oplus \pi_i^{(j)})$ -th entry of $\Theta^{(j)}$ received in step 5.
- iii if the decommitted labels from the above two checks are consistent with each other.
- iv if the set of Eval inputs $Y^{(j)}$ received in step 6 is consistent with half of the commitments in $\Omega^{(j)}$ received in step 5. Specifically, the ith entry of $Y^{(j)}$ should decommit the $(2 \cdot i + \overline{y}_i)$ th entry in $\Omega^{(j)}$.

If any failure occurs, Eval aborts.

10. Evaluating Garbled Circuits

Eval evaluates the circuit according to the Yao protocol.

(a) For every gate $g \in G(C)$ with input labels $W_a^{(j)} = (K_a^{(j)}, \delta_a^{(j)})$ and $W_b^{(j)} = (K_b^{(j)}, \delta_b^{(j)})$, Eval finds the $(2 \cdot \delta_a^{(j)} + \delta_b^{(j)})$ index E of G(C) and computes

$$W_c^{(j)} = (K_c^{(j)}, \delta_c^{(j)}) = dec_{K_c^{(j)}}(dec_{K_c^{(j)}}(E))$$

(b) For every output wire w_i with label $W_i = (K_i, \delta_i)$, Eval computes the wire's value $b_i^{(j)} = \delta_i^{(j)} \oplus \pi_i^{(j)}$, where Eval learned $\pi_i^{(j)}$ at the end of step 8. She lets the set of outputs $\{b_i^{(j)}\}$ be the circuit outputs.

11. Finding the Majority Output

Eval finds the most commonly occurring element for each index in $\{b_i\}$ among the evaluation circuits and interprets the set of outputs $\{b_i\}$ as (h, c, g_2) . She then checks:

- (a) if $h^{(j)} \neq h$ for any $j \in S$, or
- (b) if (h, c, g_2) is not the majority output of $\{(h^{(j)}, c^{(j)}, g_2^{(j)})\}$. More formally, Eval checks if

$$\{(h^{(j)}, c^{(j)}, g_2^{(j)}) : (h^{(j)}, c^{(j)}, g_2^{(j)}) = (h, c, g_2)\} \le \frac{|S|}{2} = \frac{\sigma}{5}$$

If any of the above checks are true, Eval aborts. Otherwise, she accepts g_2 as her own output.

12. Proving Gen's Output Authenticity

Eval sends Gen his output c and must prove his output authenticity without revealing the index of the chosen majority circuit, as described in section 4.2.2.

There will be a version where Gen has to generate all the circuits twice (so as not to keep them in memory unnecessarily). Make this inclusion in the above list. Also, include the part about cutting down communication.

References

- [1] C.-h. Shen and A. Shelat, "Two-output secure computation with malicious adversaries," in *Advances in Cryptology–EUROCRYPT 2011*. Springer, 2011, pp. 386–405.
- [2] C.-h. Shen and a. shelat, "Fast two-party secure computation with minimal assumptions," in *Proceedings* of the 2013 ACM SIGSAC conference on Computer & communications security. ACM, 2013, pp. 523–534.
- [3] B. Kreuter, a. shelat, and C.-H. Shen, "Billion-gate secure computation with malicious adversaries." in *USENIX Security Symposium*, 2012, pp. 285–300.
- [4] A. YAO, "Protocols for secure computation," 23rd FOCS, 1982, 1982.
- [5] Y. Lindell and B. Pinkas, "An efficient protocol for secure two-party computation in the presence of malicious adversaries," in *Advances in Cryptology-EUROCRYPT 2007*. Springer, 2007, pp. 52–78.
- [6] Y. Huang, D. Evans, J. Katz, and L. Malka, "Faster secure two-party computation using garbled circuits," in *Proceedings of the 20th USENIX Conference on Security*, ser. SEC'11. Berkeley, CA, USA: USENIX Association, 2011, pp. 35–35. [Online]. Available: http://dl.acm.org/citation.cfm?id=2028067.2028102