Applied Machine Learning for Business Analytics

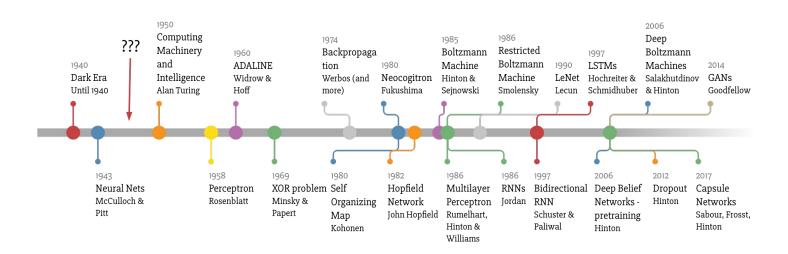
Lecture 3: Neural Networks and Deep Learning

Lecturer: Zhao Rui

Logistics

DL/NN is not New

Deep Learning Timeline



3

Why DL is Powerful Now?

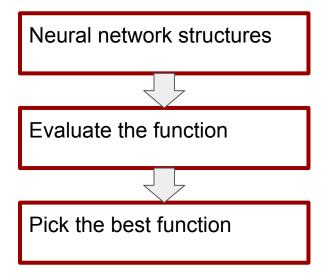
- Feature engineering require high-level expert knowledge, which are easily over-specified and incomplete.
- Large amounts of training data
- Modern multi-core CPUs/GPUs/TPUs
- Better deep learning 'tricks' such as regularization, optimization, transfer learning etc.

Three Steps in Deep Learning

To approximate the true function, define a function **space**

Need a **measure** to evaluate the quality of each potential function in the previous space

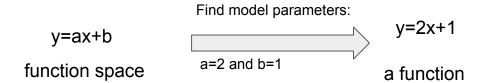
Search the function space to find the best function based on the measure.



Learning Representation

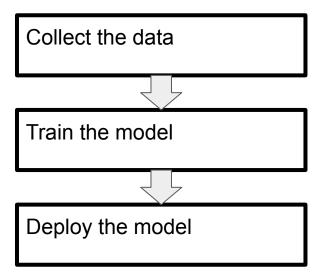
Objective Function

Optimization



Deep Learning Myth: Three Steps

To deploy deep learning (or other machine learning) systems





The Truth

- Select a metric for optimization 6
- Collect data 🙇
- Train model Management
- Realize many labels are wrong 😱
 - Relabel data 📥
- Train model Management

5.

- Model performs poorly on one class 🤦
- Collect more data for that class 🙇
- Train model Margarithm
- Model performs poorly on most recent data 🤦 10.
 - Collect more recent data
- Train model M 12.
- 13. Deploy model **9**
- 14. Dream 🤑
- 15. Get a call at 3am about complaints that model is biased 👱
- 16. Revert to the older version
- Collect more data, do more training and testing
- 18. Deploy model **9**
- 19. Pray 🙆
- Model performs well but revenue decreasing 2 20.
- 21. Cry 😭
- Choose a different metric ____
- Start over 👱



Agenda

- 1. Linear Regression
- 2. Neural Networks
- 3. Evaluation of Functions
- 4. Optimization
- 5. Deep Learning
- 6. Application of DL

1. Linear Regression

Linear Regression (Single Variable)

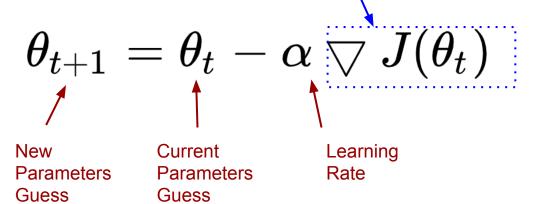
- Model architecture: y=ax+b
- Objective function: Mean Squared Error Function

$$J(a,b) = \frac{1}{n} \sum_{i=0}^{n} (y_i - (ax_i + b))^2$$

Optimization: Gradient Descent Algorithm

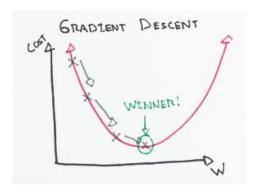
Gradient Descent

Gradient for the total loss function over parameters,





Like hiking down a mountain



Credit:https://ml-cheatsheet.readthedocs.i o/en/latest/gradient_descent.html 11

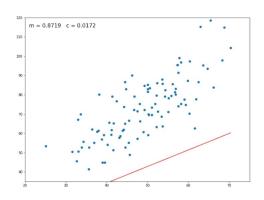
Simple Math

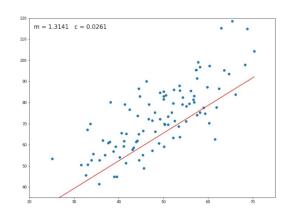
• Gradients for parameters:

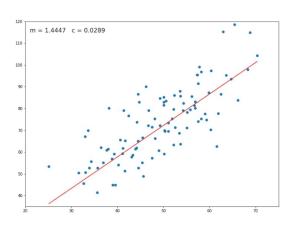
$$egin{aligned} rac{\partial}{\partial a}J(a,b) &= rac{1}{n}\sum_{i=0}^{n}2(y_i-(ax_i+b))(-x_i)\ rac{\partial}{\partial a}J(a,b) &= rac{-2}{n}\sum_{i=0}^{n}(y_i-y_i^{'})x_i \end{aligned}$$

$$rac{\partial}{\partial b}J(a,b)=rac{-2}{n}\sum_{i=0}^{n}(y_{i}-y_{i}^{'})$$

Optimization

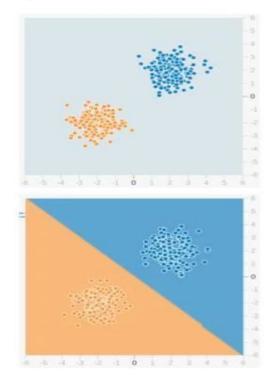


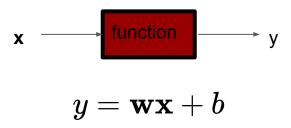




2. Neural Networks

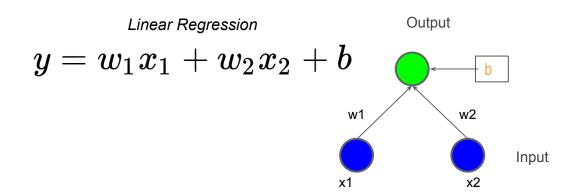
A "Simple" Classification Problem



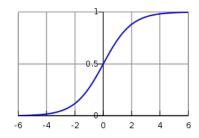


A Linear Model

- Linear Regression if output is continuous
- Logistic Regression if output is discrete

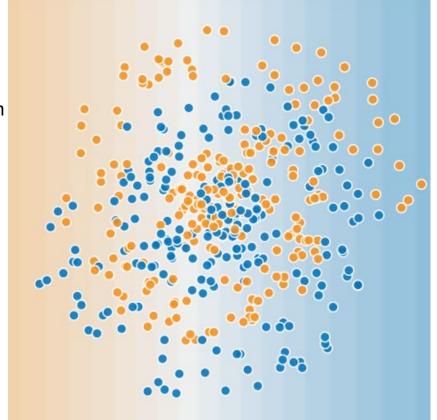


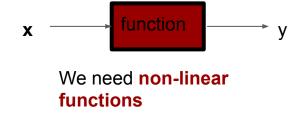
Logistic Regression $y = \sigma(\mathbf{w}\mathbf{x} + b)$



How about this classification problem?

Linear model can not solve it





Add Complexity

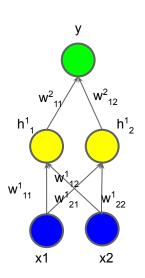
For Simplicity, the bias term is ignored here.

$$h_1^1=w_{11}^1x1+w_{12}^1x2 \ h_2^1=w_{21}^1x1+w_{22}^1x2 \ y=w_{11}^2h_1^1+w_{12}^2h_2^1 m y=m WX \ y=(w_{11}^2w_{11}^1+w_{21}^2w_{12}^1)x1+(w_{12}^2w_{12}^1+w_{12}^2w_{22}^1)x2$$

Add Complexity

Associative Law

$$egin{aligned} h_1^1 &= w_{11}^1 x 1 + w_{12}^1 x 2 \ h_2^1 &= w_{21}^1 x 1 + w_{22}^1 x 2 \ y &= w_{11}^2 h_1^1 + w_{12}^2 h_2^1 \end{aligned}$$



Matrix Format

Output

$$\left[egin{array}{c} h_1^1 \ h_2^1 \end{array}
ight] = \left[egin{array}{cc} w_{11}^1 & w_{12}^1 \ w_{21}^1 & w_{22}^1 \end{array}
ight] \left[egin{array}{c} x1 \ x2 \end{array}
ight]$$

Hidden Layer

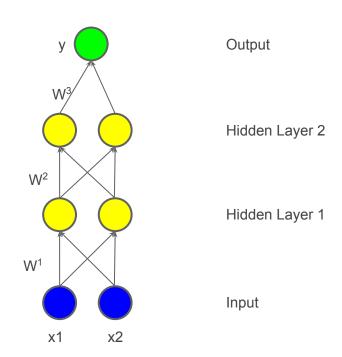
$$y = \left[egin{array}{cc} w_{11}^2 & w_{12}^2 \end{array}
ight] \left[egin{array}{c} h_1^1 \ h_2^1 \end{array}
ight]$$

Input

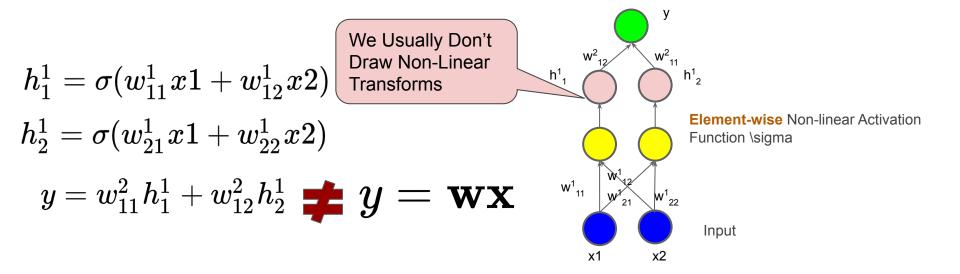
$$y=W^2W^1\left[egin{array}{c} x1\ x2 \end{array}
ight]=(W^2W^1)\left[egin{array}{c} x1\ x2 \end{array}
ight]=W\left[egin{array}{c} x1\ x2 \end{array}
ight]$$

Add Complexity

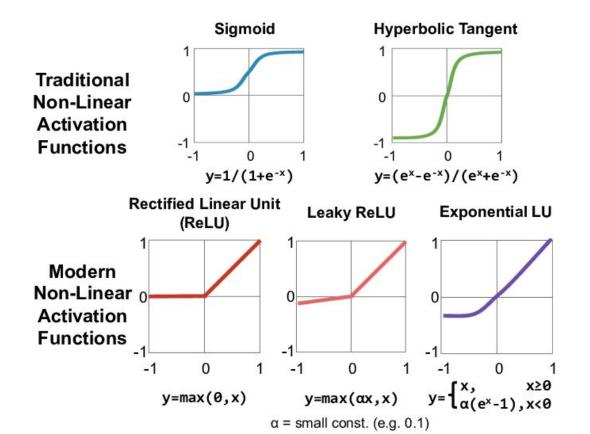
$$y = \mathbf{W}^3\mathbf{W}^2\mathbf{W}^1 \left[egin{array}{c} x1 \ x2 \end{array}
ight] = (\mathbf{W}^3\mathbf{W}^2\mathbf{W}^1) \left[egin{array}{c} x1 \ x2 \end{array}
ight]$$



Make it non-linear



Non-linear Activation Functions



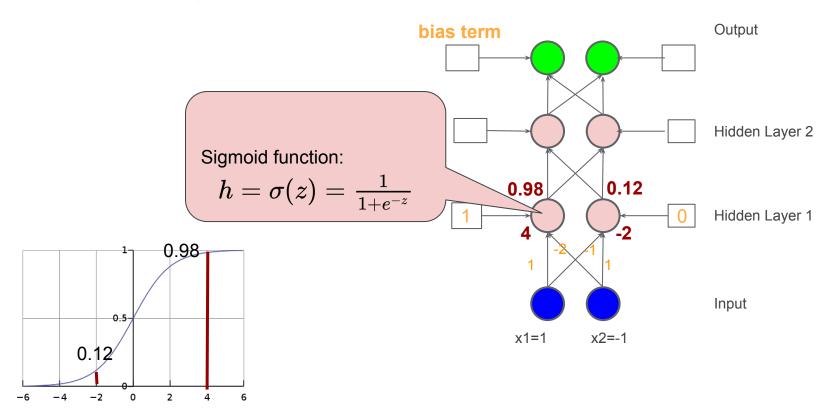
Add Non-linear Activation Function

$$y=\mathbf{W}^3\mathbf{h}^2$$
 y Output $y=\mathbf{W}^3\sigma(\mathbf{W}^2\sigma(\mathbf{W}^1\mathbf{x}))$ Hidden Layer 2 $\mathbf{h}^1=\sigma(\mathbf{W}^1\mathbf{x})$ Hidden Layer 1

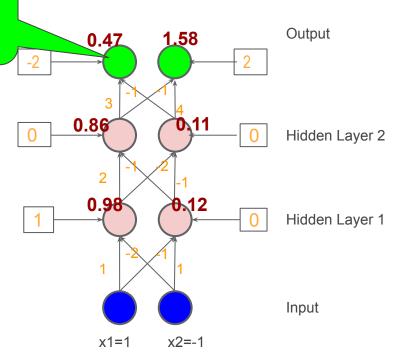
Why Non-linear Activation

- The non-linearities activation function increases the capacity of model
- Without non-linearities, deep neural networks is meaningless: each extra layer is just one linear transform.
- How to select activation functions?

You can select an activation function which will approximate the distribution faster leading to faster training process.



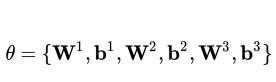
Identity Function. It can be non-linear functions specified by applications.



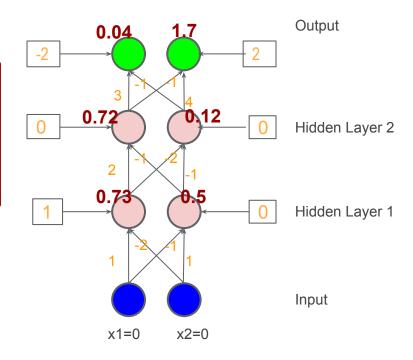
 Neural Network acts as a function that transforms the input vector into the output vector (target)

$$egin{aligned} egin{aligned} egin{aligned} 0.47 \ 1.58 \end{bmatrix} &= f_{ heta} (egin{bmatrix} 1 \ -1 \end{bmatrix}) \ egin{bmatrix} \mathbf{w}^1 &= egin{bmatrix} -2 \ -1 & 1 \end{bmatrix} & \mathbf{b}^1 &= egin{bmatrix} 1 \ 0 \end{bmatrix} \ egin{bmatrix} \mathbf{w}^2 &= egin{bmatrix} 2 & -1 \ -2 & -1 \end{bmatrix} & \mathbf{b}^2 &= egin{bmatrix} 0 \ 0 \end{bmatrix} \ egin{bmatrix} \mathbf{w}^3 &= egin{bmatrix} 3 & -1 \ -1 & 4 \end{bmatrix} & \mathbf{b}^3 &= egin{bmatrix} -2 \ 2 \end{bmatrix} \ egin{bmatrix} \mathbf{one} \ \mathbf{param.} \ \mathbf{set} \end{aligned}$$

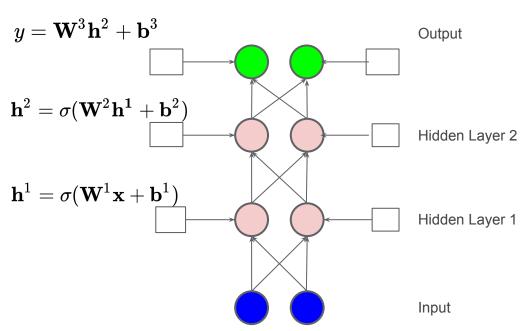
2. It is actually a function space parameterized by weights matrices and bias vectors.



Parameter space



$$y = \mathbf{W}^3 \sigma(\mathbf{W}^2 \sigma(\mathbf{W}^1 \mathbf{x} + \mathbf{b}^1) + \mathbf{b}^2) + \mathbf{b}^3$$

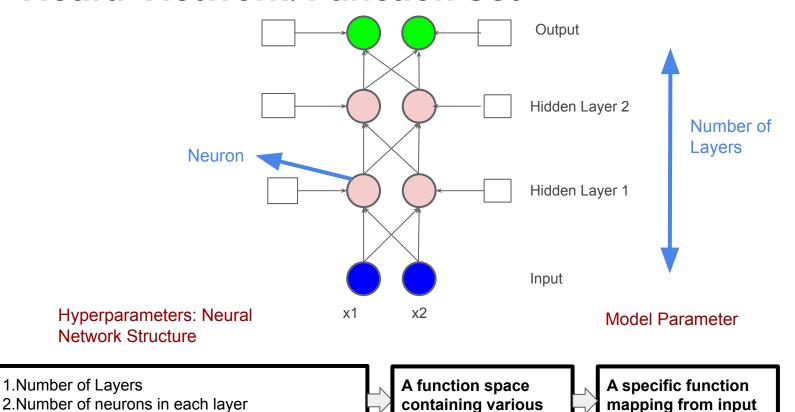


- 1. Neural Network is a model that **recursively** applies the matrix multiplication and non-linear activation function.
- 2. Parallel computing techniques can be used to speed up matrix operation.

Neural Network: Function Set

1. Number of Layers

3. Non-linear Activation function in each layer



functions

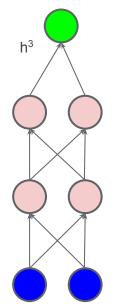
data to targets.

29

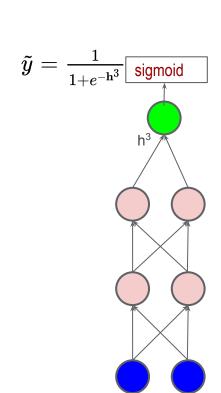
Output Layer

Regression

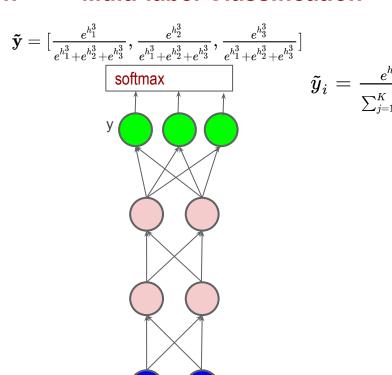
$ilde{y}=\mathbf{h}^3$



Binary Classification

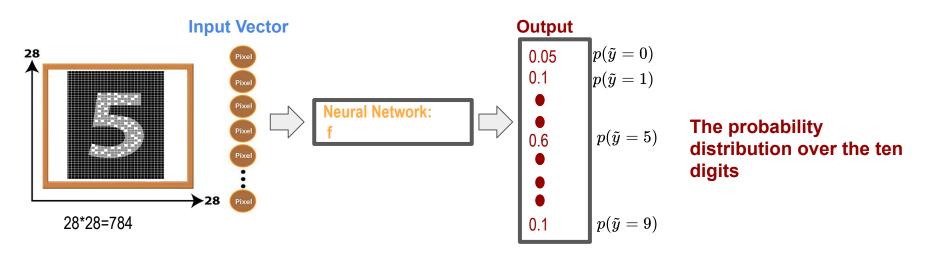


Multi-label Classification

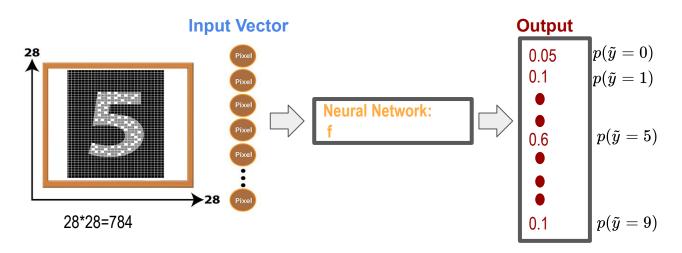


Example: MINST Dataset





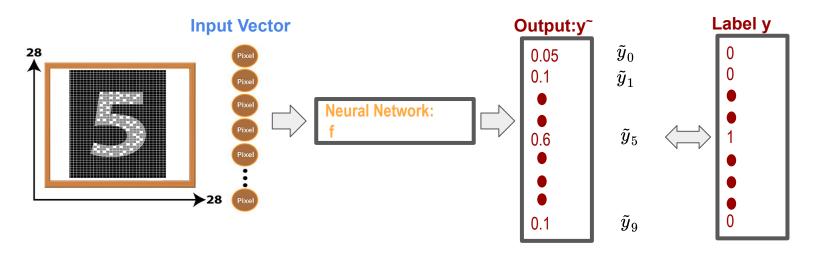
Example: MNIST Dataset



- 1. In this task, the neural network is a function mapping from the input 784-dim vector to the output 10-dim vector.
- The neural network structure should be decided to make sure the best function exists in the function set.

3. Evaluation of Functions

Cross-Entropy Loss



Given a set of parameters and one training sample,

$$loss(ilde{\mathbf{y}},\mathbf{y}) = -\sum_{i=0}^9 y_i ln(ilde{y}_i)$$

Total Loss

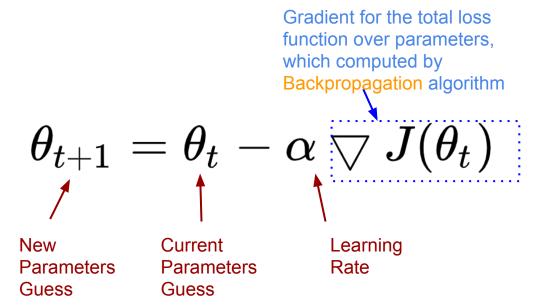
- Training dataset contains N training samples
- ullet The total loss is: $J = \sum_{n=1}^N loss(ilde{\mathbf{y}_n}, \mathbf{y}_n)$
- Find a function is the function set that minimizes the total loss J
- ullet Find the network parameters heta that minimizes the total loss J. Modern

For loss function, training data are fixed and model parameters are unknown.

$$argmin_{ heta}J$$

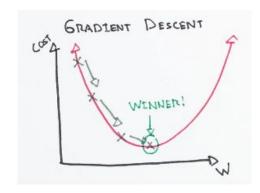
4. Optimization

Gradient Descent



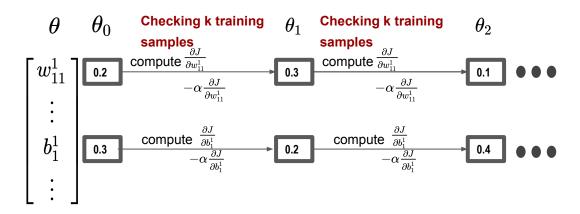


Like hiking down a mountain



Credit:https://ml-cheatsheet.readthedocs.i o/en/latest/gradient_descent.html 37

Gradient Descent



Backpropagation is used to compute gradients in an efficient way. $\frac{\partial S}{\partial \theta}$

Batch size: k

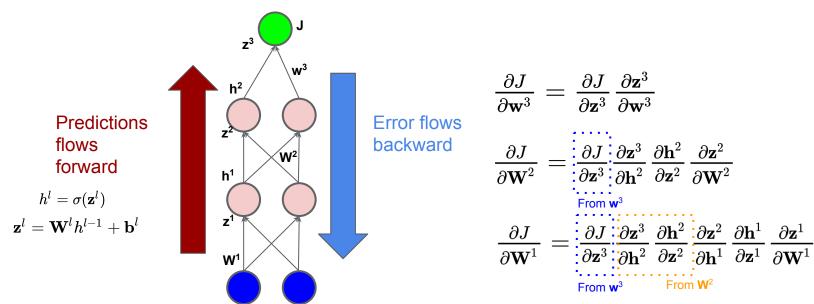
A dataset is [1,2,3,4,5,6] and the batch size is 2, one batch shuffle could be: batch0=[2,1], batch1=[3,6], batch2=[4,5]

Backpropagation

Definition (from wiki):

By computing the gradient of the loss function with respect to each weight by the **chain rule**, computing the gradient one layer at a time, iterating backward from the last layer to avoid redundant calculations of intermediate terms in the chain rule

 $\mathbf{x} = \mathbf{h}^0$



Batch Size

Three approaches to select batch sizes:

- 1. Batch Gradient Descent
- 2. Mini-batch Gradient Descent
- 3. Stochastic Gradient Descent

batch size = Number of training data

1<bath>batch size< number of training data

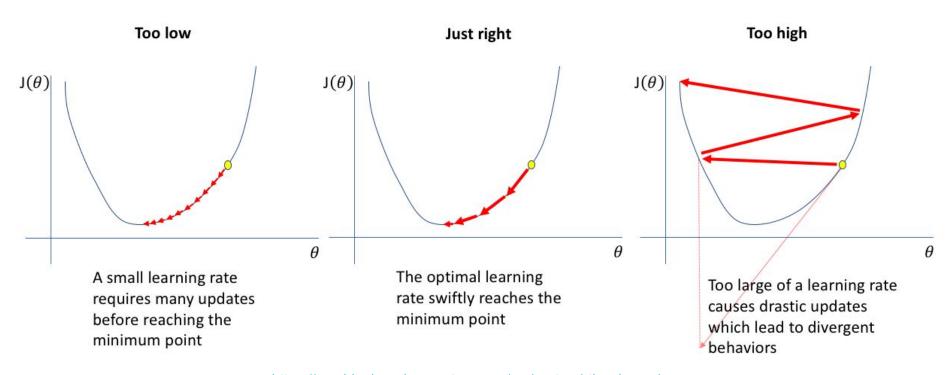
batch size = 1

Training Process

- Initialize neural network randomly
- For _ in range(number of epoch):
 - Shuffle all the training dataset into a list of batches
 - For _ in range(number of batches)
 - Get output with the input data in the batch
 - Compare outputs with ground truth in training data
 - Compute loss function with the batch data
 - Update weights with backpropagation and gradient descent algorithm



Learning Rate

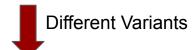


https://machinelearningmastery.com/understand-the-dynamics-of-learning-rate-on-deep-learning-neural-networks/

Except SGD

SGD

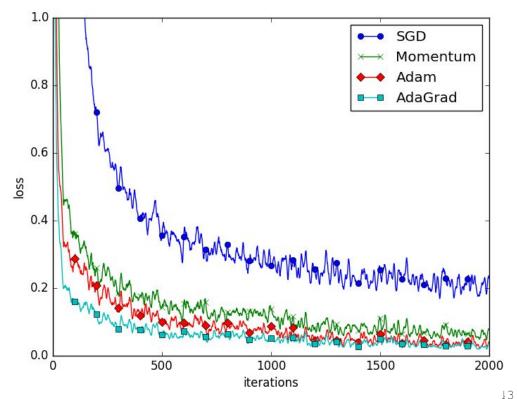
$$\mathbf{x}_{n+1} = \mathbf{x}_n - \alpha \bigtriangledown f(\mathbf{x}_n)$$



Momentum, Adam, AdaGrad, **RMSProp**



Auto-tune learning rates



Neural Network Visualization

Playground

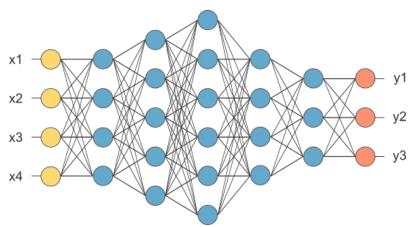
5. Deep Learning

Neural Network

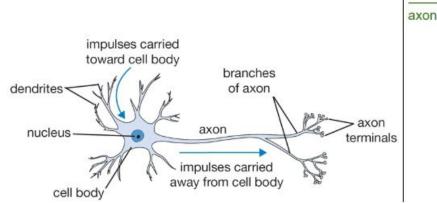
- From Wiki:
 - NN is based on a collection of connected units of nodes called artificial neurons which loosely model the neurons in a biological brain.
- From another way:

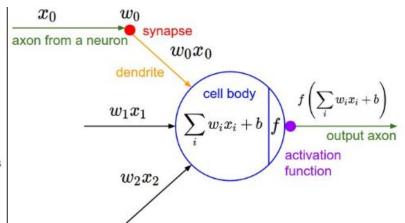
NN is running several 'logistic regression' at the same time (expanding at width and depth

dimensions).



Neural Computation

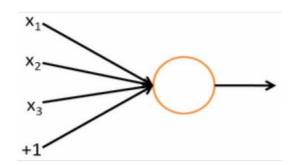




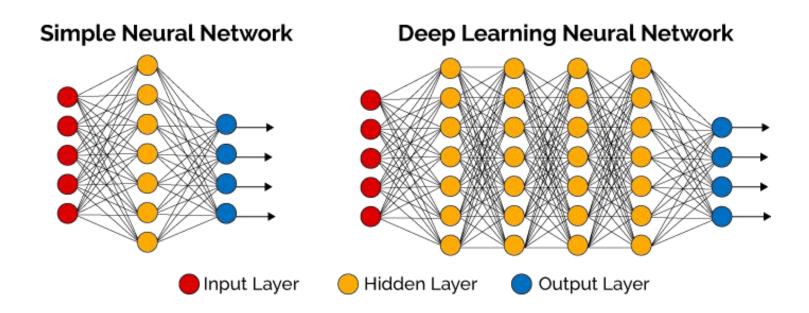
A cartoon drawing of a biological neuron (left) and its mathematical model (right).

The fact that a neuron is essentially a logistic regression unit:

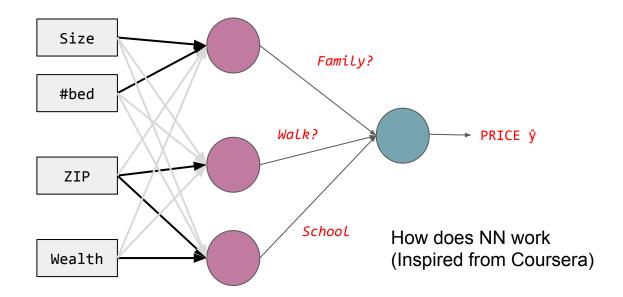
1 performs a dot product with the input and its weights
2 adds the bias and apply the non-linearity



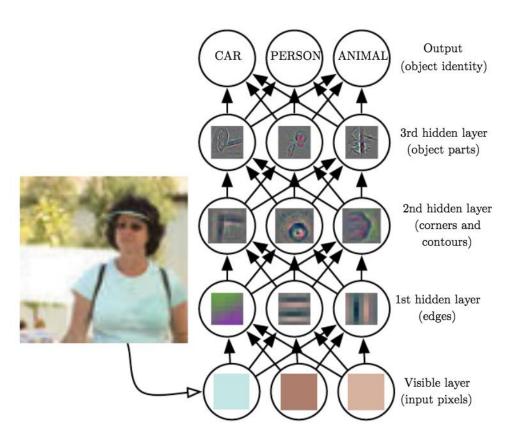
Shallow vs Deep



Representation Learning in DL

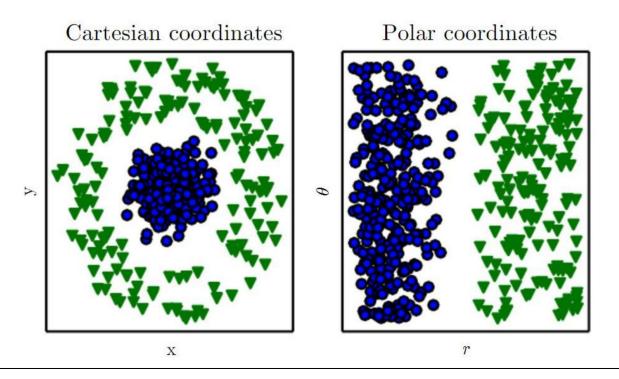


Representation Learning in DL

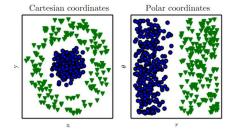


From Deep Learning (Goodfellow)

Representation Matters

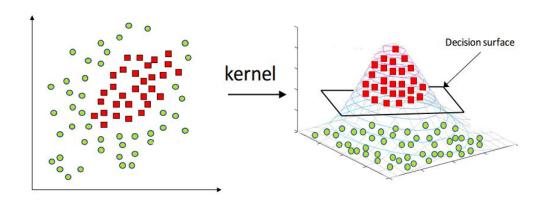


Task: Draw a line to separate the **green triangles** and **blue circles**.



We want to project the data into the **new** feature/vector space that data is **linearly separated**

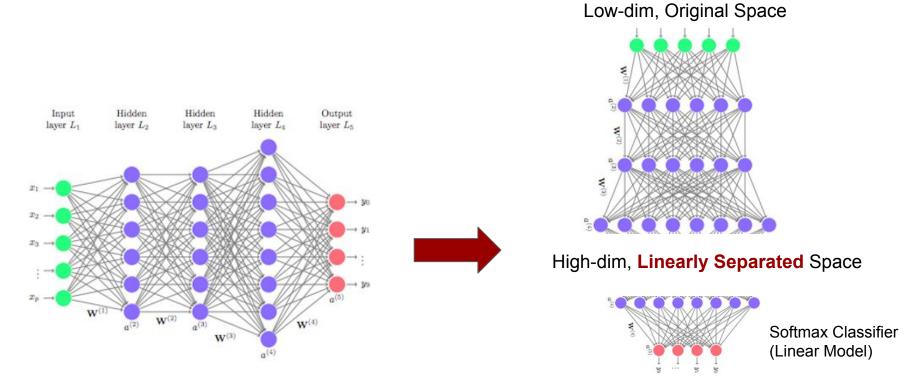
Kernel Tricks in SVM



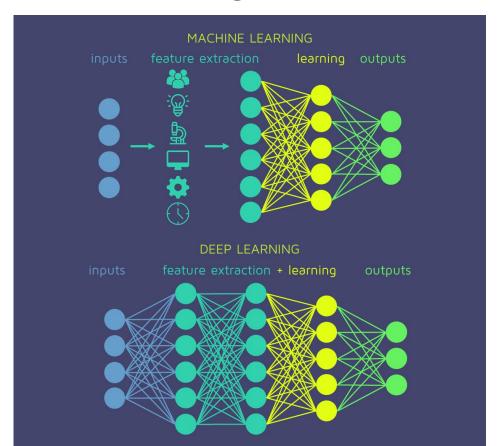
Low-dim, Original Space

High-dim, Linearly Separated Space

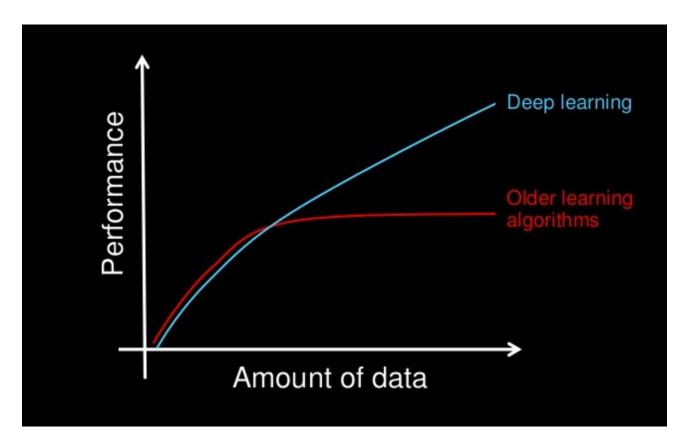
Hidden Representation in Deep Learning



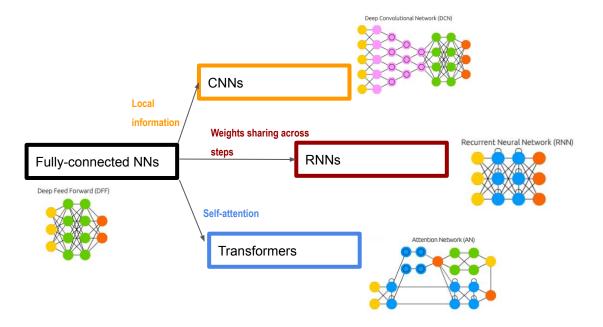
End-to-End Learning



Why Deep Learning



Deep Learning Structures



https://www.asimovinstitute.org/author/fjodorvanveen/

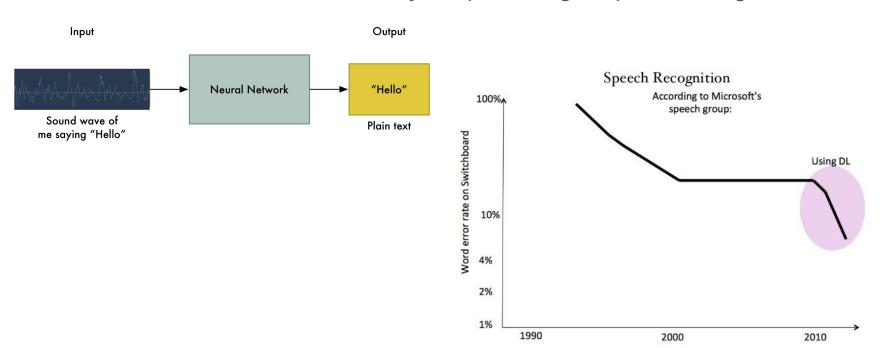
Deep Learning

- Deep learning is a subfield of machine learning
- Most machine learning methods work well because of high-quality feature engineering/representation learning.
- Deep learning is an end-to-end structure, which supports automatic representation learning
- Different network structures: CNN, RNN, LSTM, GRU, Attention model, etc.

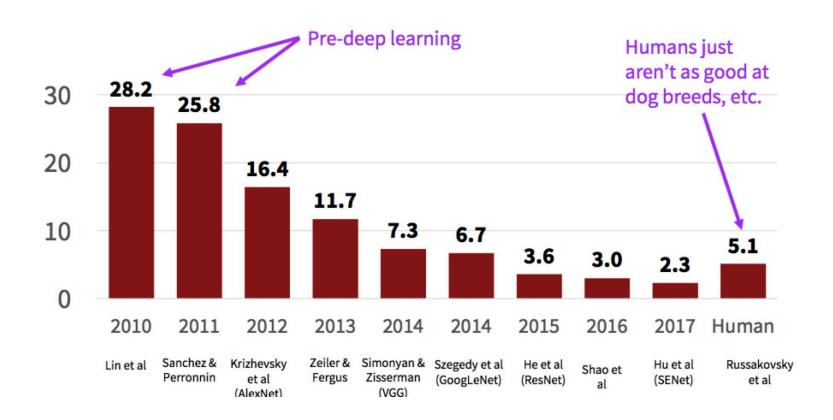
6. Applications of DL

Deep Learning for Speech

The first real-world tasks addressed by deep learning is speech recognition



Deep Learning for Computer Vision



Deep Learning for Arts



















Original photo

Reference photo

Result

Deep Learning for Data Generations

Given training data, generate new samples from same distribution



AutoML and Neural Architecture Search

