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Prerequisites from Coding Challenge 5 %% __________2
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% CODE CHALLENGE 6 - Template Script
% The purpose of this challenge is to predict whether or not the
Boulder
% Reservior will have to close due to a major leak.
% In Coding Challenge 5, you did the following:
% - Part 1:
    1) Read in the provided data file
    2) Estimated reservoir volume w/ Trapezoidal and Simpson's 1/3
Rules
응
    3) Compared the accuracy of the two results
2
 - Part 2:
   1) Propagated t and h using Euler's Method
   2) Used plots to observe the effect of different timesteps on the
      estimation accuracy
% In Coding Challenge 6, you will build upon the code that you wrote
% for Coding Challenge 5. Fill in what you can in the below code
template
% by using the code you completed last week. Once you get to the
% Runge-Kutta approximation, calculate K-values and use the Runge-
Kutta
% equations to approximate the reservoir height over time.
% In the last section of this code, create plots that effectively
% illustrate differences between approximation methods and parameters,
% comparing Runge-Kutta using different time steps and also Runge-
Kutta vs.
% Euler's Method.
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% NOTE: DO NOT change any variable names already present in the code.
% Upload your team's script to Gradescope when complete.
```

Housekeeping

Don't clear variables (i.e. with "clear"); this makes grading difficult.

Prerequisites from Coding Challenge 5 %%

Set-up for Runge Kutta Method %%

Problem Parameters %

```
h0 = 20;
                               % Initial reservoir depth
  [ft]
                              % Relating volume change to depth
alpha = 1.5e6;
 [ft<sup>2</sup>/day]
                              % Volume inflow rate
dV in = 2e7;
[ft<sup>3</sup>/day]
% Approximation Parameters %
timestep = [16 8 4 2 1];
                          % Timesteps to use for approximation
 [days]
for j = 1:length(timestep)
    t end = 160;
                               % Choose an end time for your program
 [days]
```

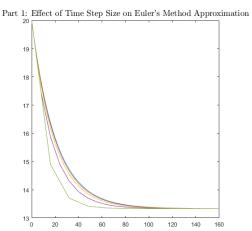
```
t = 0:timestep(j):t_end; % Allocate a time vector
 [days]
   h = zeros(1,length(t)); % Allocate a depth vector
  [ft]
   h(1) = h0;
                             % Set a depth vector initial value
  [ft]
   h_RK = h;
                             % Set a depth vector for Runge-Kutta
  [ft]
   for i = 1:(length(t)-1) % Euler's Method - use your code from Lab
 6
       dhdt = get_dhdt(h(i),L,alpha,dV_in);
                                                      % Get dh/dt at
 this depth
                        [ft/day]
       h(i+1) = (h(i)+(dhdt*timestep(j))); Compute next depth value
        t(i+1) = t(i) + timestep(j);
   end
   for i = 1:(length(t)-1) % Runge-Kutta Method
       K1 = get_dhdt(h_RK(i),L,alpha,dV_in);
                                                          % Calculate
your K1 value
       K2 = get_dhdt(h_RK(i) + (timestep(j) * .5 * K1), L, alpha, dV_in);
       % Calculate your K2 value
       K3 = get_dhdt(h_RK(i) + (timestep(j) * .5*K2), L, alpha, dV_in);
       % Calculate your K3 value
       K4 = get_dhdt(h_RK(i)+(timestep(j)*K3),L,alpha,dV_in);
   % Calculate your K4 value
       h RK(i+1) =
h_{K(i)}+((timestep(j)/6)*((K1)+(2*K2)+(2*K3)+(K4))); % Compute
your next reservoir height
   end
   % Don't touch these three lines of code... %
   eval(['t_' num2str(timestep(j)) ' = t;'])
   eval(['h E ' num2str(timestep(j)) ' = h;'])
    eval(['h_RK_' num2str(timestep(j)) ' = h_RK;'])
end
```

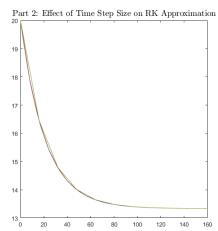
Plotting Results %%

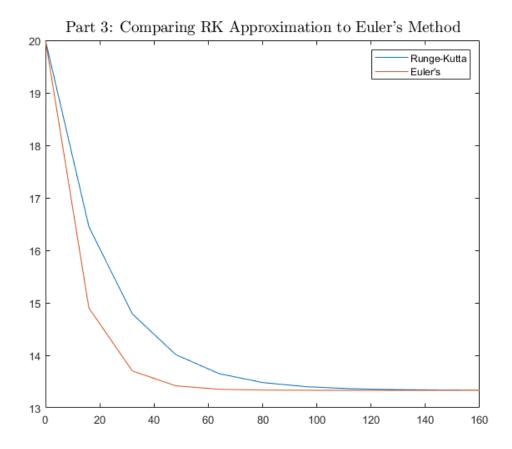
READ THIS: After the above code runs, the "eval" statements at the end of the loop create three sets of variables. One set holds the time vectors used in the various approximations, named "t_16" for the 16-day time step, "t_8" for the 8-day time step, etc. Another set holds the Euler approximation results for the various timesteps, named "h_E_16" for the 16-day time step, "h_E_8" for the 8-day time step, etc. The last set holds the Tunge-Kutta approximation results for the various timesteps, named "h_RK_16", "h_RK_8", etc. For simplicity, you may use these vectors in your plotting.

```
fig1 = figure('Units','Normalized','Position',[0 0.25 0.65 0.50]);
% Part 1: Effect of timestep on Euler's Method approximation %
subplot(1,2,1)
plot(t_1,h_E_1,t_2,h_E_2,t_4,h_E_4,t_8,h_E_8,t_16,h_E_16)
```

```
title('Part 1: Effect of Time Step Size on Euler''s Method
 Approximation', ...
    'Interpreter', 'latex', 'Fontsize', 14)
% Here, plot the results of your Euler's approximation using different
% time steps. Is there a significant difference between time steps?
% Part 2: Effect of timestep on Runge-Kutta approximation %
subplot(1,2,2)
plot(t_1,h_RK_1,t_2,h_RK_2,t_4,h_RK_4,t_8,h_RK_8,t_16,h_RK_16)
title('Part 2: Effect of Time Step Size on RK Approximation', ...
    'Interpreter', 'latex', 'Fontsize', 14)
% Here, plot the results of your Runge-Kutta Method approximation
using different
% time steps. Is there a significant difference between time steps?
fig2 = figure('Units','Normalized','Position',[0.65 0.25 0.35 0.50]);
% Part 3: Comparing Runge-Kutta to Euler's Method %
plot(t 16,h RK 16,t 16,h E 16)
title('Part 3: Comparing RK Approximation to Euler''s Method', ...
    'Interpreter', 'latex', 'Fontsize', 14)
legend('Runge-Kutta','Euler''s')
% Here plot the results of your Runge-Kutta and Euler's Method
% approximations together. You are encouraged to use a few different
 step
% sizes for Euler's Method, but you can decide for yourself how best
% illustrate the difference in accuracy between Euler and Runge-Kutta.
% there a significant difference in approximation accuracy?
```







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