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%% Macro III: Problem Set 3
% Deadline: Friday, 17/09/2018
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%
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% Source code disponível em: <https://github.com/btebaldi/Macro3/tree/master/PSet_02
% https://github.com/btebaldi/Macro3/tree/master/PSet_03>
%
%
%% QUESTÃO 1 (a)-(e)

%% LIMPEZA DE VARIAVEIS
clearvars
clc
%% ITEM A DEFINICAO DE PARAMETROS
%
% Defininimos os parametros que sao utilizados pelo problema
Econom_param.PeriodsPerYear = 6;
Econom_param.Beta_anual = 0.96;
Econom_param.Beta = (Econom_param.Beta_anual)^(1/Econom_param.PeriodsPerYear);
Econom_param.Sigma = 1.5;

eps = 1e-5;

%% DEFINICAO DO GRID DE INCOME
%
% Vamos Construir a matrix de transição baseada nas informações fornecidas
Income.Grid.N = 2;
Income.Grid.Max = 1;
Income.Grid.Min = 0.1;
Income.Values = linspace(Income.Grid.Max, Income.Grid.Min, Income.Grid.N);
Income.PI = [0.925 (1-0.925); 0.5 (1-0.5)];
Income.P_LongRun = CalculaLongoPrazo(Income.PI);
%%
% Logo a renda media de equilibrio no longo prazo sera.
Income.Average = Income.Values*Income.P_LongRun;
Income.Early = Income.Average * Econom_param.PeriodsPerYear;
%%
% A duração média do desemprego é dada por 1/f, onde f neste caso é 0.5. Sendo assim a↙
duracao média do desemprego é dois periodos. Como o periodo é de dois meses, temos que a↙
duração média de desemprego é de 4 meses.

%% DEFINICAO DO GRID de ASSET

Borrow.Limit = -Income.Early;
Asset.Grid.N = 20;
Asset.Grid.Max = 3*Income.Average;
Asset.Grid.Min = Borrow.Limit;
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Asset.Values = linspace(Asset.Grid.Min, Asset.Grid.Max, Asset.Grid.N);


%% DEFINICAO DA TAXA DE JUROS
%
% Inicia a taxa de juros
Econom_param.r_anual = 0.034;
Econom_param.r_start = ((1+Econom_param.r_anual)^(1/Econom_param.PeriodsPerYear))-1;
Econom_param.r_UpperLimit = 1/Econom_param.Beta - 1;
Econom_param.r_LowerLimit = 0;
Econom_param.r = Econom_param.r_start;

% parametro que indica se a taxa esta fixa ou nao.
Econom_param.r_IsFixed = 0;

%% ACHANDO O EQUILIBRIO.
% # Determinar um r inicial
% # Resolver o Problema do Consumidor e obter a Politica
% # Determinar Lambda
% # Verificar se existe eequilibrio no mercado de assets
% # Se nao ha equilibrio estabelecer novo r, (voltar a ponto 2) onde
%   $e>0 \rightarrow r_j+1 < r_j$
%   $e<0 \rightarrow r_j+1 > r_j$


nIntLimit = 1000;

for i=1:nIntLimit

    % (2) Resolve o Problema do consumidor
    [V0, U_Cube, Policy] = SolveConsumerProblem(Asset, Income, Econom_param);

    % (3) Determina a distribuicao estacionaria
    Lambda = ConstructLambda(Policy, Asset, Income);

    % (4) Determina demanda de assets
    Demanda = Lambda(:)' * Policy.AssetPrime.Values(:);

    % (5) Verifica se há equilibrio
    if abs(Demanda) < eps
        break;
    elseif Demanda > eps
        Econom_param.r_UpperLimit = Econom_param.r;
    elseif  Demanda < -eps
        Econom_param.r_LowerLimit = Econom_param.r;
    end

    % Caso a taxa esteja fixa não ha mais nada o que fazer
    if Econom_param.r_IsFixed == 1
        break;
    end
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    % determina novo r
    r_old = Econom_param.r;
    Econom_param.r = (Econom_param.r_UpperLimit + Econom_param.r_LowerLimit)/2;

    % Caso a precisao da taxa seja muito pequena paramos a execucao.
    if abs(Econom_param.r - r_old) < eps^2
        break;
    end

    fprintf('Inter:%4d\tr_0: %1.6f\tr_1: %1.6f\tDem: %2.15f\n', i, r_old, Econom_param.r,↙
Demanda);
end

% Limpa variaveis nao utilizadas
clear nIntLimit r_old
%% GRAFICO DA FUNCAO POLITICA DE $A_{t+1}$ CONTRA $A_{t}$

fig1 = figure();
plot(Policy.AssetDomain, Policy.AssetPrime.Values(:,1),'b-.','LineWidth',1); hold on;
plot(Policy.AssetDomain, Policy.AssetPrime.Values(:,2),'r','LineWidth',2); hold on;
plot(Policy.AssetDomain, Policy.AssetDomain,'k:','LineWidth',1); hold off;
legend({'Low Employment State','High Employment State','45-degree Ray'});
title('Household Savings Policy Function');
xlabel('$a_{i,t}$','FontSize',12,'Interpreter','latex');
ylabel('$a_{i,t+1}$','FontSize',12,'Interpreter','latex');


%% SIMULACAO DE LIFE HISTORY
%
% define uma funcao que indica, dado um valor de asset, qual o valor do grid que mais se↙
aproxima do valor informado. Em outras palavras informa aonde um valor fornecido estaria↙
no grid.
Policy.AssetIndexFunction = @(value) round((value-Policy.AssetDomain(1))/(Policy.↙
AssetDomain(2)-Policy.AssetDomain(1))) + 1;

% Total de simulacoes
Simulation.N = 10000;

% Nivel inicial de ativos
asset_0 = 0;

% Estado inicial: Empregado.
Simulation.S0 = 1;
Simulation.Wage = 1;

% Inicializa os vetores da simulacao.
Simulation.Asset = nan(Simulation.N,1);
Simulation.AssetIndex = nan(Simulation.N,1);
Simulation.Consumption = nan(Simulation.N,1);
Simulation.Investment = nan(Simulation.N,1);
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```
Simulation.LaborIncome = nan(Simulation.N,1);
Simulation.AssetIncome = nan(Simulation.N,1);
Simulation.Shock = nan(Simulation.N,1);

% Gera uma cadeia de choques no salario
[stateValue, stateIndex] = MarkovSimulation(Income.PI, Simulation.N, Income.Values,↙
Simulation.S0);

for i = 1:Simulation.N
    % pega o estado do choque.
    Simulation.Asset(i) = asset_0;
    Simulation.AssetIndex(i) = Policy.AssetIndexFunction(asset_0);

    Simulation.Shock(i) = stateValue(i);

    % determina o investimento baseado no estado atual (asset\capital e
    % choque)
    Simulation.Investment(i) = Policy.AssetPrime.Values(Simulation.AssetIndex(i),↙
stateIndex(i));

    % Determina a renda proveniente do trabalho
    Simulation.LaborIncome(i) = Simulation.Wage*stateValue(i);

    % Determina a renda proveniente do rendimento dos assets
    Simulation.AssetIncome(i) = (1 + Econom_param.r)*Simulation.Asset(i);

    % Determina o consumo pela equacao de equilibrio
    Simulation.Consumption(i) = Simulation.AssetIncome(i) + Simulation.LaborIncome(i) -↙
Simulation.Investment(i);

    % Atualiza o asset
    asset_0 = Simulation.Investment(i);
end
fprintf('DONE\n');

%% GRAFICOS
% Grafico de investimento vs consumo
x = 1:Simulation.N;
plot(x, Simulation.Investment, x, Simulation.Consumption);
title('INVESTMENT AND CONSUMPTION');
legend({'Investment','Consumption'},'FontSize', 8, 'Location','southeast',↙
'Orientation','Horizontal');
%%
% Covariancia de consumo e investimento
cov(Simulation.Consumption,Simulation.Investment)
%%
% Grafico de renda vs consumo
figure
plot(x, Simulation.LaborIncome, x, Simulation.Consumption);
title('LABOR INCOME AND CONSUMPTION');
legend({'Labor income','Consumption'},'FontSize', 8, 'Location','southeast',↙
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'Orientation','Horizontal');
%%
% Covariancia de renda e consumo
cov(Simulation.LaborIncome, Simulation.Consumption)
%%
% Grafico de renda vs investimento
figure
plot(x, Simulation.LaborIncome, x, Simulation.Investment);
title('LABOR INCOME AND INVESTMENT');
legend({'Labor income','Investment'},'FontSize', 8, 'Location','southeast',↙
'Orientation','Horizontal');
%%
% Covariancia de renda e investimento
cov(Simulation.LaborIncome, Simulation.Investment)
%%
% Grafico de riqueza total
figure
plot(x, Simulation.LaborIncome + Simulation.AssetIncome);
title('Income');
legend({'Income'},'FontSize', 8, 'Location','southeast', 'Orientation','Horizontal');
%%
% Histograma de ativos
figure
histogram(Simulation.Investment)
title('HISTOGRAM OF ASSET HOLDINGS')
xlabel('Value of the Asset Holding','FontSize',10,'Interpreter','latex');
ylabel('Number of periods','FontSize',10,'Interpreter','latex')

% limpa variaveis
clear x
%% CALCULO DOS VALORES EXPERADOS
% average value of asset holdings

mean(Simulation.Asset)
%%
% Average decline in consumption in response to entering unemployment
Delta.Consumption = Simulation.Consumption(2:end) - Simulation.Consumption(1:end-1);
Delta.Shock =  Simulation.Shock(2:end) - Simulation.Shock(1:end-1);
mean(Delta.Consumption(Delta.Shock < 0))

clear Delta
%%
% Average consumption conditional on (i) employed; (ii) unemployed; (iii)
% unemployed for the last 12 months.
mean(Simulation.Consumption(Simulation.Shock==1))
mean(Simulation.Consumption(Simulation.Shock==0.1))

A = (Simulation.Shock==0.1)';
B = [1 1 1 1 1 1];
Unemployed6m = strfind(A,B)';
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```
Consumption6Months = 0;
TotalPeriods = size(Unemployed6m,1);
for i=1:TotalPeriods
    Consumption6Months = Consumption6Months + mean(Simulation.Consumption(Unemployed6m(i):Unemployed6m(i)+6));
end
Consumption6Months/TotalPeriods

clear A B Consumption6Months TotalPeriods Unemployed6m
%% %% INCOME DISTRIBUTION

Total_Income =  ((1+Econom_param.r)*Asset.Values)'*ones(1,Income.Grid.N) + ones(1,Asset.Grid.N)'*Income.Values;
[sortedIncome, index] = sort(Total_Income(:));
lambda_aux = Lambda(:);

figure
plot(sortedIncome, lambda_aux(index));
title('INCOME DISTRIBUTION');
xlabel('INCOME LEVEL');
ylabel('% OF AGENTS');


%%  STANDARD MEASURES FOR WEALTH DISPERSION

mean_w = mean(Simulation.AssetIncome+Simulation.LaborIncome);
stdr_w = std(Simulation.AssetIncome+Simulation.LaborIncome);

figure
histogram(Simulation.AssetIncome+Simulation.LaborIncome);
annotation('textbox',[.2 .3 .4 .5],...
    'String',{['Mean = ' num2str(mean_w)],['Stddev =' num2str(stdr_w)]},...
'FitBoxtoText','on');
title(sprintf('Wealth, sigma=%1.1f',Econom_param.Sigma));
```