

1. On Attached pdf.

2.

```
Node ArrayToBST(arr[], left, right)
{
    if (left > right)
        return;

    int mid = (left + right)/2;
    Node root = arr[mid];

    root.left = ArrayToBST(arr, left, mid-1);

    root.right = ArrayToBST(arr, mid+1, right);

    return root;
}
```

Recurrence Relation is handwritten on attached pdf.

3. With a set S sorted by its X values

OVERVIEW:

Maintain a global array for indexes and the set S-S'. In the combine method, we compare points, and check whether the condition holds for them to be added to set S-S'. If the condition does hold, we add it to S', and then add the index to the indexes array. In the end we have set S-S', and so we use this to construct the array S'.

PSEUDO CODE:

```
Point[] S-S';
ArrayList<Integer> indexes;

combine(Point[] S, left, mid, right){
    i = left;
    j = mid + 1;
```

```

while(i <= mid && j <= right)
    if(S[i].x < S[j].x && S[i].y < S[j].y)
        add S[i] to set S-S'
        add i to indexes;
        i++;
    else if(i == mid && j <= right)
        j++;
    else if(i <= mid && j == right)
        i++;
    else
        i++;
        j++;
}

```

```

public static void merge(int l, int r) {
    if(l < r) {
        int mid = l + (r-l)/2;
        merge(l, mid);
        merge(mid+1, r);
        combine(l, mid, r);
    }
}

```

OVERVIEW OF CONSTRUCT S':

We loop through the original set S, and construct S', by adding every element from S, that isn't in set S-S'.

```

constructS'(){
    for(int i =0; i < S.size(); i++) {
        if(!indexes.contains(i)) {
            System.out.println(S.get(i).getX() + " , " + S.get(i).getY());
        }
    }
}

```

***** Recurrence Relation for merge and combine are on attached sheet.

In addition to that recurrence relation, must also add the time to construct S', which is $O(n^2)$;

4. Do a DFS to get an array of all nodes:

For each node, get its neighbors from the adjacency list:

Check if the condition holds:

i.e. for each neighbor, check if they also have a neighbor

such that for edge $(a,b) \in E$, $(b,c) \in E$

if condition holds, add it to G2 adjacency matrix

Time Complexity $O(nm)$: For each node, we check all neighbors, thus nm .