

Regression_HW4

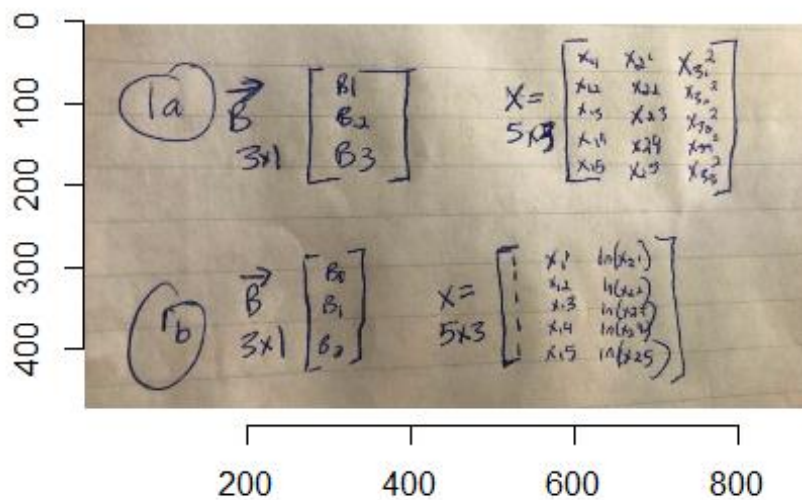
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Question: 1A & B

For each of the following regression models, carefully provide the design matrix X and vector of regression coefficients B

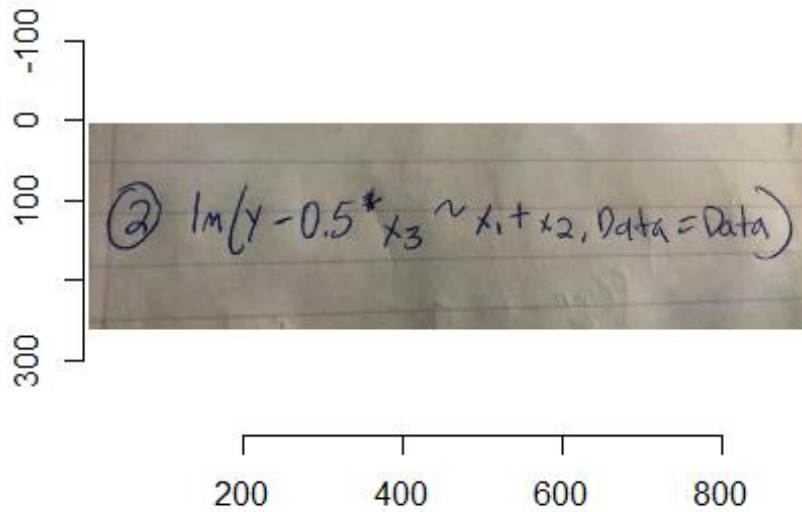
`plot(myimg)`



Question: 2

Suppose you want to fit the multiple regression model such as where $i=1, \dots, n$, by the method of least squares when you are given that $b_3 = 0.5$. Precisely explain how you can obtain the

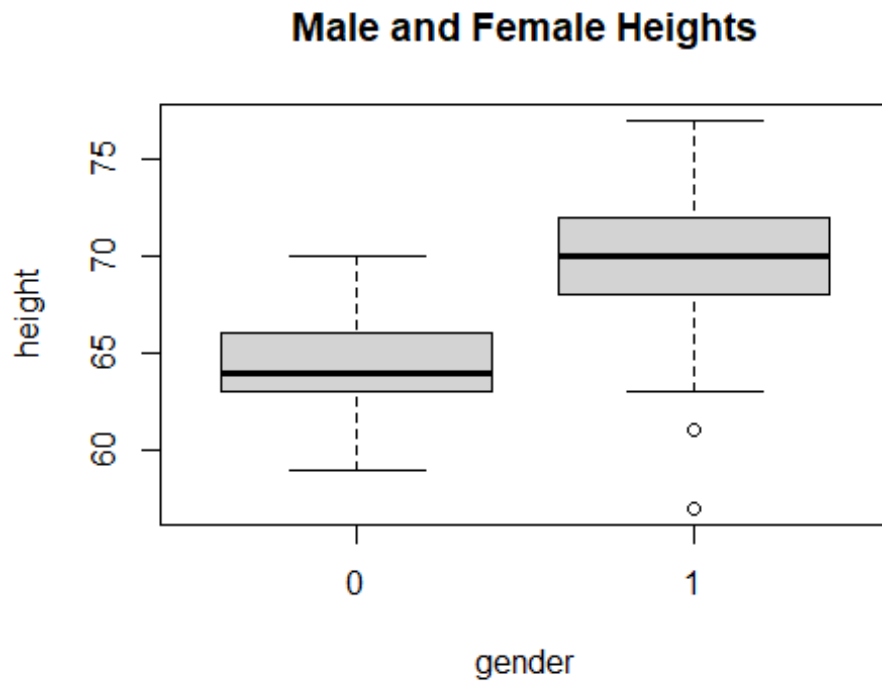
desired fitted multiple regression from a computer program.



Question: 3a

Provide side by side boxplots of heights of female and male children. Comment on the plot.

```
boxplot(height~male, data = childData, main = "Male and Female Heights", xlab = "gender")
```



We can see that male has a few outlier data points and the average height of male is much larger than the average height of female

Question: 3b

Provide a histogram of mothers' heights. Comment on the plot. Are there any missing values or extreme values (outliers)?

```
hist(childData$momht, main = "Mothers heights", xlab = "height")
```



```
summary(childData)
```

```
##      ID      alcohol      exercise      height
##  Min.   : 1.00   Min.   : 0.00   Min.   : 0.000   Min.   :57.00
## 1st Qu.:44.00   1st Qu.: 0.00   1st Qu.: 2.000   1st Qu.:64.00
## Median :86.00   Median : 1.00   Median : 3.000   Median :66.00
## Mean   :86.56   Mean    : 4.27   Mean    : 4.698   Mean    :66.84
## 3rd Qu.:131.00  3rd Qu.: 4.75   3rd Qu.: 6.000   3rd Qu.:69.50
## Max.   :173.00  Max.    :55.00   Max.    :30.000   Max.    :77.00
##
##      NA's :6      NA's :1
##      male      dadht      momht
##  Min.   :0.0000   Min.   :55.00   Min.   :54.00
## 1st Qu.:0.0000   1st Qu.:67.00   1st Qu.:61.00
## Median :0.0000   Median :69.00   Median :63.00
## Mean    :0.4545   Mean    :69.17   Mean    :63.27
## 3rd Qu.:1.0000   3rd Qu.:72.00   3rd Qu.:65.00
## Max.    :1.0000   Max.    :78.00   Max.    :71.00
##
```

```
IQR(childData$momht)*1.5 + 71
```

```
## [1] 77
```

```
54 - IQR(childData$momht)*1.5
```

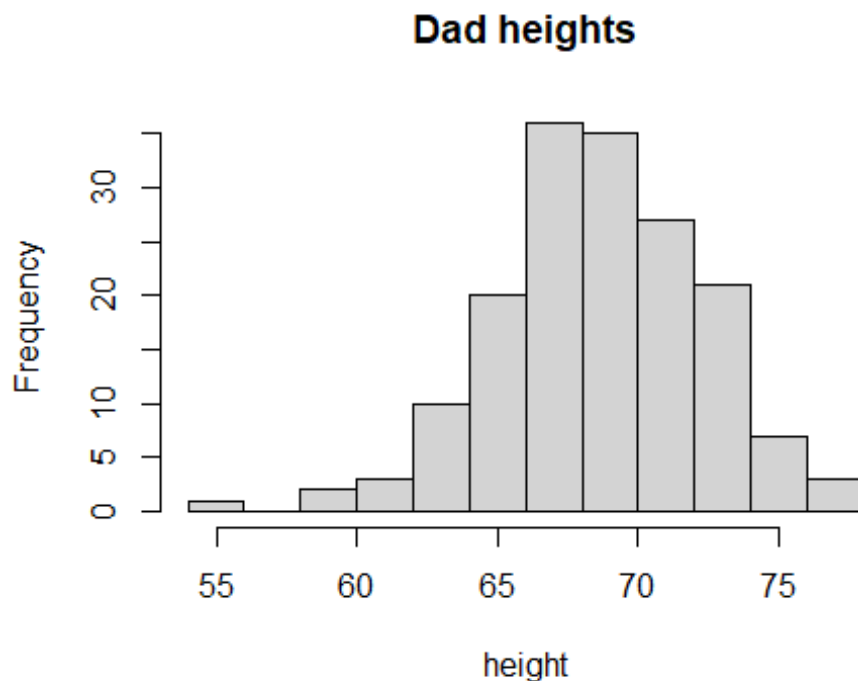
```
## [1] 48
```

We can see that the histogram just like the box plot doesnt show any data below 48 or above 77 indicating that there is no missing or outlier datapoints for mother height

Question: 3c

Provide a histogram of fathers' heights. Comment on the plot. Are there any missing values or extreme values (outliers)?

```
hist(childData$dadht, main = "Dad heights", xlab = "height")
```



```
summary(childData)
```

```
##           ID           alcohol           exercise           height
## Min.      : 1.00    Min.      : 0.00    Min.      : 0.000    Min.      :57.00
## 1st Qu.: 44.00    1st Qu.: 0.00    1st Qu.: 2.000    1st Qu.:64.00
## Median : 86.00    Median : 1.00    Median : 3.000    Median :66.00
## Mean      : 86.56    Mean      : 4.27    Mean      : 4.698    Mean      :66.84
## 3rd Qu.:131.00    3rd Qu.: 4.75    3rd Qu.: 6.000    3rd Qu.:69.50
## Max.      :173.00    Max.      :55.00    Max.      :30.000    Max.      :77.00
##           NA's      :6           NA's      :1
##           male           dadht           momht
## Min.      :0.0000    Min.      :55.00    Min.      :54.00
## 1st Qu.:0.0000    1st Qu.:67.00    1st Qu.:61.00
## Median :0.0000    Median :69.00    Median :63.00
## Mean      :0.4545    Mean      :69.17    Mean      :63.27
## 3rd Qu.:1.0000    3rd Qu.:72.00    3rd Qu.:65.00
```

```
## Max. :1.0000 Max. :78.00 Max. :71.00
##

IQR(childData$dadht)*1.5 + 78 # finding max outlier range
## [1] 85.5

55 - IQR(childData$dadht)*1.5 # finding min
## [1] 47.5

childData[childData$dadht > 85.5 | childData$dadht < 47.5,"dadht"] # There
are no extreme outliers

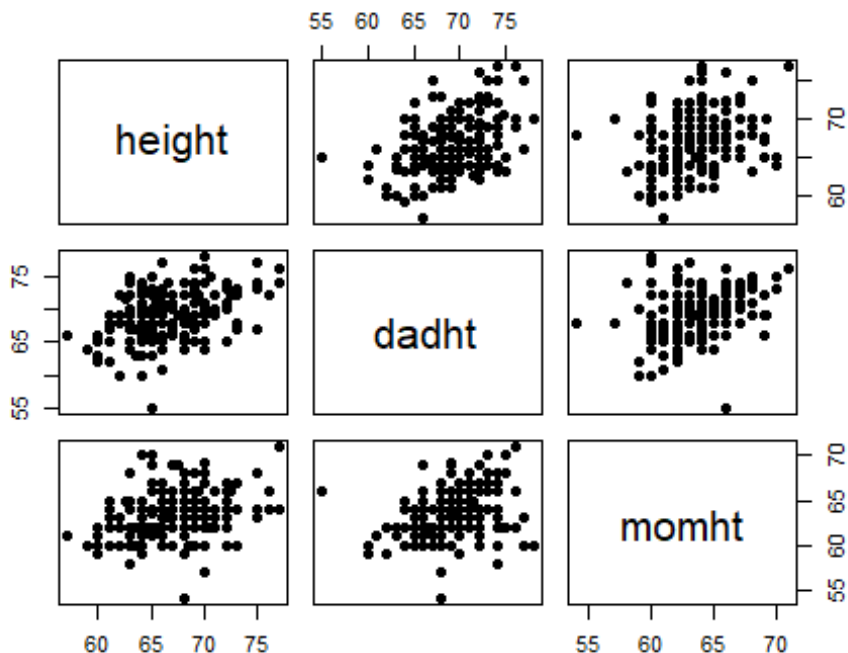
## numeric(0)

# We can see that the histogram just like the box plot there are outliers but
the outliers are not above the range establish by 1.5 * the IQR
```

Question: 3d

Provide a scatter plot matrix (as in Lecture 8 page 9) for 3 variables height, momht and dadht. Comment on the plot

```
pairs(childData[,c(4,6,7)], pch = 19)
```

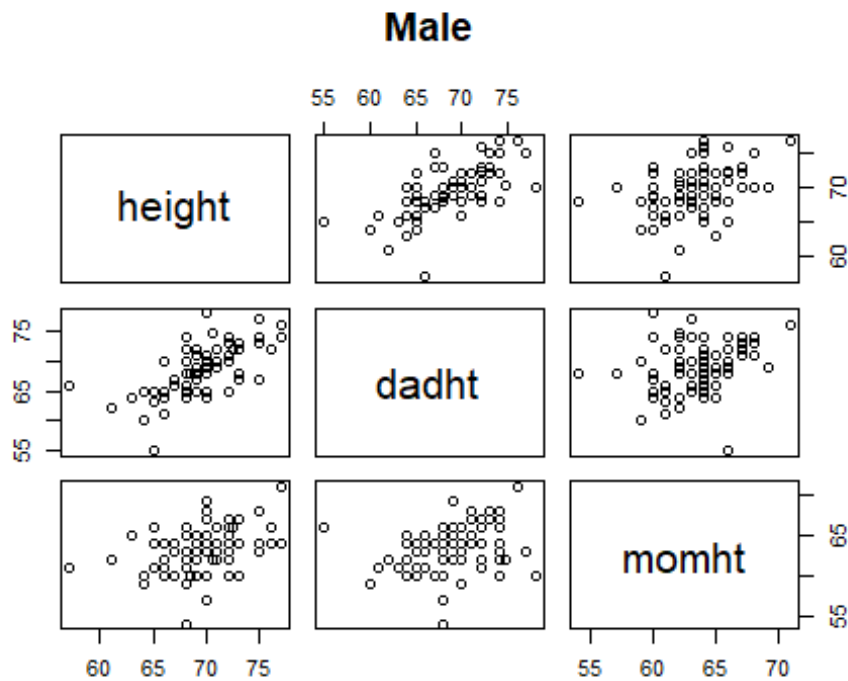


```
# It does not look like there is any strong relationship between any of the
independent variables indicating we dont need to investigate further
```

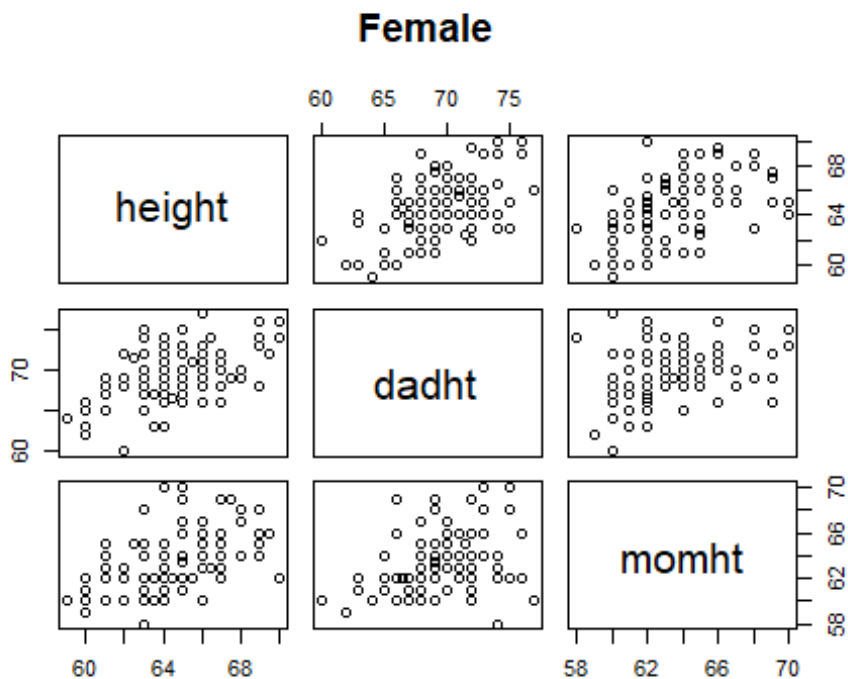
Question: 3e

Now provide scatter plot matrix in part (d) separately for male and female children.
Comment on the plot.

```
pairs(childData[which(childData$male == 1),c('height','dadht','momht')],main  
= "Male")
```



```
pairs(childData[which(childData$male == 0),c('height','dadht','momht')],main  
= "Female")
```



for the male matrix it looks like there is a stronger relationship between height and dad height when you compare the height and mom height relationship
 # for the female matrix there does not seem to be a distinct difference in the strength of relationship from height to dad height or mother height

Question: 3f

Show the summary and provide a precise interpretation of the coefficient β_3 that can be understood by a layman

```
model1 <- lm(height ~ male + momht + dadht, data = childData)
summary(model1)
```

```
##
## Call:
## lm(formula = height ~ male + momht + dadht, data = childData)
##
## Residuals:
```

	Min	1Q	Median	3Q	Max
	-10.7431	-1.4537	0.0191	1.5299	5.9459

```
##
## Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	16.96746	4.65831	3.642	0.000364	***
male	5.29822	0.36377	14.565	< 2e-16	***
momht	0.29962	0.06876	4.357	2.34e-05	***
dadht	0.41213	0.05107	8.069	1.54e-13	***


```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.316 on 161 degrees of freedom
## Multiple R-squared:  0.6604, Adjusted R-squared:  0.6541
## F-statistic: 104.4 on 3 and 161 DF,  p-value: < 2.2e-16
```

Here b3 represents fathers height and the .41213 means this. For every unit increase in dad height there will be a .41213 unit increase in height

Question: 3g

Show the summary and provide a precise interpretation of the coefficient β_1 that can be understood by a layman.

```
model2 <- lm(height ~ male + momht ,data = childData)
summary(model2)
```

```
##
## Call:
## lm(formula = height ~ male + momht, data = childData)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.4918  -1.4455   0.0776   1.6008   7.0776
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  34.38884    4.87674   7.052 4.85e-11 ***
## male         5.01498    0.42777  11.724 < 2e-16 ***
## momht        0.47685    0.07698   6.194 4.65e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.736 on 162 degrees of freedom
## Multiple R-squared:  0.5231, Adjusted R-squared:  0.5172
## F-statistic: 88.85 on 2 and 162 DF,  p-value: < 2.2e-16
```

Here b1 is 5.014 and reads as such means that a person who is a Male is 5.0149 units taller than a female on average this is with mother height as part of the model as a predictor

Question: 3h

Show the summary and provide a precise interpretation of the coefficient β_1 that can be understood by a layman.

```
model3 <- lm(height ~ male + dadht ,data = childData)
summary(model3)
```

```
##
## Call:
## lm(formula = height ~ male + dadht, data = childData)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.2355  -1.6516  -0.1012   1.4491   6.2813
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  30.97678    3.55308   8.718 3.2e-15 ***
## male         5.36620     0.38308  14.008 < 2e-16 ***
## dadht        0.48322     0.05101   9.472 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.441 on 162 degrees of freedom
## Multiple R-squared:  0.6204, Adjusted R-squared:  0.6157
## F-statistic: 132.4 on 2 and 162 DF,  p-value: < 2.2e-16

# Here b1 is 5.366 and reads as such means that a person who is a Male is
# 5.366 units taller than a female on average this is with dad height as part
# of the model as a predictor
```

Question: 3i

Based on R2, which model is best? Which model is second best?

```
summary(model1)$r.squared # best
## [1] 0.660445

summary(model2)$r.squared # worst
## [1] 0.523112

summary(model3)$r.squared #second best
## [1] 0.6204024
```