```
function apply operation(a, b, operator)
      if operator is '+' then
            return a + b
      if operator is '-' then
            return a - b
      if operator is '*' then
            return a * b
      if operator is '/' then
            return a / b
function evaluate(expression)
      value stack \leftarrow init stack()
      ops stack ← init stack()
      i ← 0
      while i < expression.length() do</pre>
             curr ← expression[i]
             if curr is digit then
                   value stack.push(expression[i])
             else if curr is '(' then
                   ops stack.push(expression[i])
             else if curr is ')' then
                   if value stack has less than 2 values or top of ops stack is '('
                          then return "NotWellFormed"
                   while ops stack is non-empty and top of ops stack is not'(' do
                         v2 ← value stack.pop()
                         v1 \leftarrow value stack.pop()
                         operator ← ops stack.pop()
                         result \leftarrow apply operation(v1, v2, operator)
                         value stack.push(result)
                   if top of ops stack is not '(' then
                         return "NotWellFormed"
                   else
                         ops_stack.pop()
             else if curr is '+' or '-' or '*' or '/' then
                   if ops_stack is empty then
                         return "NotWellFormed"
                   while ops_stack is non-empty and value_stack has 2 or more values and
      ops stack.peek() has higher or equal precedence than curr, do
                         v2 ← value_stack.pop()
                         v1 ← value stack.pop()
                         operator ← ops stack.pop()
                          result ← apply_operation(v1, v2, operator)
                          value stack.push(result)
                   ops stack.push(curr)
             else
                   return "NotWellFormed"
             i ← i + 1
      if only one of ops stack and value stack is empty
             do return "NotWellFormed"
      while ops stack is non-empty do
             v2 ← value stack.pop()
             v1 ← value stack.pop()
             operator ← ops stack.pop()
             result ← apply operation(v1, v2, operator)
             value stack.push(result)
      return value_stack.pop()
```

```
/* step 1: read and parse first line of stdin */
      v ← number of trees (start index from 1 because 0 is mountain)
      e — number of edges (number of subsequent lines to be read) /*
      * Each sub-deque represent the adjacency list of the mountain/tree.
      \mathbf{v+1} sub-deques because \mathbf{v} deques for trees + \mathbf{1} deque for mountain */
      graph ← create_graph(with v+1 deques)
      /* step 3: read and parse e subsequent lines to add edges*/
      for each subsequent line, do
             from 

beginning of edge
             to 

destination of edge
             graph.append edge(from, to)
      /\!\!\!^{\star} step 4: decide whether all trees can be visited in one run
      * Topologically sort the graph with depth-first search approach.
      ^{\star} Check if every node in topological order have a direct edge to the next node ^{\star}/
      /* step 4a: implementing topological sort*/
function top sort(graph, total v)
      /* stack for reversed topological order */
      stack ← new deque()
      /* v+1 sized array for visit status, initially all FALSE(0) */
      visited \leftarrow new array(v+1, 0)
      for every node in visited, do
             if node not visited yet (0), do
                   top sort recursive (node, stack, visited, graph)
function top sort recursive (currrent node, stack, visited, graph)
      visited[current\_node] \leftarrow TRUE(\overline{1})
      if current node has no adjacent nodes, do
            stack.push(current node)
      else, do
             for every adjacent_node in current_node's adjacency list, do if
                   adjacent node not in stack, do
                         top_sort_recursive(adjacent_node, stack, visited, graph)
             if all adjacent nodes are already in stack, do
                   stack.push(current node)
      /* step 4b: determine if there is direct edge between nodes in topo-order */
      curr ← first node in topologically sorted deque
      while curr is not NULL, do
             if curr's next node is not in curr's adjacency list, do
                    return false (cannot traverse all trees in one go)
             increment curr to its next node
      return true (all nodes, except last node, have direct edge to their next node, so
can traverse all trees in one go)
      /* step 5: free all allocated memory */
      free all nodes from each sub-deque (adjacency lists)
      free all deques from the graph (deque of sub-deques)
      free the graph structure
Note 1: Topological Sorting
Topological sorting produces linearised data where for every edge (\mathbf{u},\mathbf{v}) in set E, the
topologically sorted order places node {\bf u} before node {\bf v}. If every node in the topological
order has a direct edge to connect to its next node, then that topological order
intuitively represents the path that allows traversal of all nodes in a DAG.
```

## Note 2: Time Complexity

function is single run possible()

Step 1-3: O(|V|+|E|)Step 4: O(|V|+|E|)

The algorithm employs multiple for-loops and while-loops, but none of them are nested. The nodes and edges are iterated at linear time in each step. The recursive part of topological sorting is called a maximum of V times (once for each node). Hence, overall complexity of the program: O(|V|+|E|)+O(|V|+|E|)=O(|V|+|E|), linear time.