

given $f(x) \neq 0$

$$\begin{aligned}\ln(f(x))' &= \frac{f'(x)}{f(x)} = 0 \\ f'(x) &= 0\end{aligned}$$