

Q1: Read the Final.csv data from D2L to R and Python and denote this data by d1.

```
import numpy as np
```

```
import pandas as pd
```

```
#q1
```

```
d1 = pd.read_csv("final.csv")
```

Q2: How many observations (number of rows) and Variables (columns) in the d1 data?

```
np.shape(d1)
```

Output: 17842 rows, 28 columns

Q3: How many variables are numerical/continuous and how many are them are integers/discrete?

```
d1.info()
```

Output:

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 17842 entries, 0 to 17841
Data columns (total 28 columns):
 #   Column                Non-Null Count  Dtype
---  -
 0   ID                    17842 non-null  object
 1   SW                    17842 non-null  int64
 2   MOI                   17842 non-null  int64
 3   YOI                   17842 non-null  int64
 4   DOICMC                17842 non-null  int64
 5   RMOB                  17842 non-null  int64
 6   RYOB                  17842 non-null  int64
 7   RDOBCMC               17842 non-null  int64
 8   RCA                   17842 non-null  int64
 9   Region                17842 non-null  int64
10   TPR                   17842 non-null  int64
11   DPR                   17842 non-null  int64
12   NV                    17842 non-null  int64
13   HEL                   17842 non-null  int64
14   Has Radio             17842 non-null  int64
15   Has TV                17842 non-null  int64
16   Religion              17842 non-null  int64
17   WI                    17842 non-null  int64
18   MOFB                  12335 non-null  float64
19   YOB                   12335 non-null  float64
20   DOBCMC                16025 non-null  float64
```

```

21  DOFBCMC      16025 non-null float64
22  AOR          16025 non-null float64
23  MTFBI        16025 non-null float64
24  DSOUOM.CMC   10279 non-null float64
25  RW           17842 non-null int64
26  RH           17842 non-null int64
27  RBMI         17842 non-null int64
dtypes: float64(7), int64(20), object(1)
memory usage: 3.8+ MB

```

Output:

Q4: Delete ID variable from the d1 data

```
d1.dtypes
```

```
del d1['ID']
```

```
d1.info()
```

Output:

```

RangeIndex: 17842 entries, 0 to 17841
Data columns (total 27 columns):
 #   Column          Non-Null Count  Dtype
---  -
 0   SW              17842 non-null  int64
 1   MOI             17842 non-null  int64
 2   YOI             17842 non-null  int64
 3   DOICMC          17842 non-null  int64
 4   RMOB            17842 non-null  int64
 5   RYOB            17842 non-null  int64
 6   RDOBCMC         17842 non-null  int64
 7   RCA             17842 non-null  int64
 8   Region          17842 non-null  int64
 9   TPR             17842 non-null  int64
10  DPR             17842 non-null  int64
11  NV              17842 non-null  int64
12  HEL             17842 non-null  int64
13  Has Radio       17842 non-null  int64
14  Has TV          17842 non-null  int64
15  Religion        17842 non-null  int64
16  WI              17842 non-null  int64
17  MOFB           12335 non-null  float64
18  YOB             12335 non-null  float64
19  DOBCMC          16025 non-null  float64
20  DOFBCMC         16025 non-null  float64
21  AOR             16025 non-null  float64
22  MTFBI           16025 non-null  float64
23  DSOUOM.CMC      10279 non-null  float64
24  RW              17842 non-null  int64
25  RH              17842 non-null  int64
26  RBMI            17842 non-null  int64
dtypes: float64(7), int64(20)

```

```
memory usage: 3.7 MB
```

Q5: Report the number of missing values for the variables MOFB, YOB, and AOR.

```
temp = d1[['MOFB', 'YOB', 'AOR']].copy()
num_nan = temp.isna().sum()
print(num_nan)
```

Output:

```
MOFB    5507
YOB      5507
AOR     1817
dtype: int64
```

Q6: Create d2 data from d1 data by selecting variables RMOB, WI, RCA, Religion, Region, AOR, HEL, DOBCMC, DOFBCMC, MTFBI, RW, RH, and RBMI variables.

```
d2 = d1[['RMOB', 'WI', 'RCA', 'Religion', 'Region',
        'AOR', 'HEL', 'DOBCMC', 'DOFBCMC', 'MTFBI', 'RW',
        'RH', 'RBMI']].copy()
```

Output:

```
RangeIndex: 17842 entries, 0 to 17841
Data columns (total 13 columns):
 #   Column      Non-Null Count  Dtype
---  -
 0   RMOB        17842 non-null   int64
 1   WI          17842 non-null   int64
 2   RCA         17842 non-null   int64
 3   Religion    17842 non-null   int64
 4   Region      17842 non-null   int64
 5   AOR         16025 non-null   float64
 6   HEL         17842 non-null   int64
 7   DOBCMC      16025 non-null   float64
 8   DOFBCMC     16025 non-null   float64
 9   MTFBI       16025 non-null   float64
10   RW          17842 non-null   int64
11   RH          17842 non-null   int64
12   RBMI        17842 non-null   int64
dtypes: float64(4), int64(9)
```

Q7: Delete rows that have missing values for any variable in the d2 data and denote this new data by d3.

```
d3 = d2.dropna()
```

Output:

```
d3 = d2.dropna()
print(d3.isna())
```

	RMOB	WI	RCA	Religion	Region	AOR	HEL	DOBCMC	DOFBCMC	\
0	False	False	False	False	False	False	False	False	False	
1	False	False	False	False	False	False	False	False	False	
2	False	False	False	False	False	False	False	False	False	
3	False	False	False	False	False	False	False	False	False	
4	False	False	False	False	False	False	False	False	False	
...	
17837	False	False	False	False	False	False	False	False	False	
17838	False	False	False	False	False	False	False	False	False	
17839	False	False	False	False	False	False	False	False	False	
17840	False	False	False	False	False	False	False	False	False	
17841	False	False	False	False	False	False	False	False	False	

	MTFBI	RW	RH	RBMI
0	False	False	False	False
1	False	False	False	False
2	False	False	False	False
3	False	False	False	False
4	False	False	False	False
...
17837	False	False	False	False
17838	False	False	False	False
17839	False	False	False	False
17840	False	False	False	False
17841	False	False	False	False

```
[16025 rows x 13 columns]
```

Q8: Find the summary statistics of the d3 data.

```
d3.describe()
```

output:

	RMO B	WI	RCA	Relig ion	Regi on	AOR	HEL	DOB CMC	DOF BCM C	MTF BI	RW	RH	RBMI
c o u n t	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000	1602 5.000 000
m e a n	6.437 067	3.128 799	31.84 1373	1.120 562	3.934 727	17.90 2902	1.210 109	1252. 6493 60	1174. 1900 78	35.43 6505	702.4 7756 6	1700. 9552 57	2343. 2044 31
s t d	3.491 742	1.424 111	8.886 835	0.356 198	1.901 758	3.323 532	0.930 617	75.32 4979	107.3 1785 2	83.80 8245	1398. 1235 57	1263. 8574 53	1243. 5694 93
m i n	1.000 000	1.000 000	13.00 0000	1.000 000	1.000 000	11.00 0000	0.000 000	921.0 0000 0	893.0 0000 0	0.000 000	229.0 0000 0	1044. 0000 00	1245. 0000 00

	RMO B	WI	RCA	Relig ion	Regi on	AOR	HEL	DOB CMC	DOF BCM C	MTF BI	RW	RH	RBMI
2 5 %	3.000 000	2.000 000	24.00 0000	1.000 000	2.000 000	16.00 0000	0.000 000	1212. 0000 00	1091. 0000 00	12.00 0000	423.0 0000 0	1474. 0000 00	1876. 0000 00
5 0 %	6.000 000	3.000 000	31.00 0000	1.000 000	4.000 000	17.00 0000	1.000 000	1273. 0000 00	1188. 0000 00	22.00 0000	482.0 0000 0	1510. 0000 00	2114. 0000 00
7 5 %	10.00 0000	4.000 000	39.00 0000	1.000 000	6.000 000	19.00 0000	2.000 000	1311. 0000 00	1264. 0000 00	38.00 0000	556.0 0000 0	1547. 0000 00	2420. 0000 00
m a x	12.00 0000	5.000 000	49.00 0000	4.000 000	7.000 000	40.00 0000	3.000 000	1344. 0000 00	1344. 0000 00	996.0 0000 0	9999. 0000 00	9999. 0000 00	9999. 0000 00

Q9: Add a new variable in the d3 data by finding the average of DOBCMC, DOFBCMC and MTFBI.

```
x = ['DOBCMC', 'DOFBCMC', 'MTFBI']
```

```
d3["average"] = d3[x].mean(axis = 1)
```

```
d3['average']
```

output:

```
0      813.333333
1      907.000000
2      867.666667
3      793.666667
4      860.333333
...
17837   815.000000
17838   870.333333
17839   766.333333
17840   737.333333
17841   885.333333
```

Q10: Create a new variable named “Newreligion” by recoding ‘1’ as ‘1’ and rest as ‘2’ from the Religion Variable.

```
d3["NewReligion"] = d3['Religion']
```

```
d3.loc[d3['NewReligion'] != 1] = 2
```

Output:

```
Out[110]:
```

	col_0	count
NewReligion		
	1	14215
	2	1810

Q11: Find the frequency table for the Region variable

```
pd.crosstab(index = d3["Region"], columns = "count")
```

Output:

	col_0	count
Region		
	1	1686
	2	4142
	3	2564
	4	2070
	5	2184
	6	1829
	7	1550

Q12: Find the joint frequency table for the variables Region and Religion.

```
pd.crosstab(index = d3["Region"], columns = d3["Religion"])
```

Output:

	Religion	1	2
Region			
	1	1686	0
	2	2332	1810
	3	2564	0
	4	2070	0
	5	2184	0
	6	1829	0
	7	1550	0

Q13: Find the mean values of AOR variable corresponding to each label of Region variable.

```
d3_byRegion = d3.groupby('Region')
```

```
d3_byRegion.mean().transpose()
```

Output:

Region	1	2	3	4	5	6	7
RMOB	6.354686	4.507001	6.384165	6.560870	6.449176	6.478950	6.435484
WI	2.873665	2.725495	3.361544	3.221256	3.065934	2.671405	3.241935
RCA	31.672598	18.311685	31.759360	32.107246	32.120421	31.494806	31.887097
Religion	1.000000	1.436987	1.000000	1.000000	1.000000	1.000000	1.000000
AOR	17.781139	10.943747	17.880265	17.566667	17.607601	17.279388	18.572903
HEL	1.358244	1.579189	1.169267	1.276329	1.180861	1.137233	0.978710
DOBCMC	1255.581851	714.960406	1254.570203	1240.954589	1242.006868	1250.049754	1273.264516
DOFBCMC	1173.952550	667.447851	1175.865835	1167.916425	1166.230769	1171.449426	1181.184516
MTFBI	33.395611	19.965476	35.419657	32.613527	41.543498	35.294150	36.478710
RW	961.041518	414.558909	704.145086	664.336232	702.423077	515.057408	658.692258
RH	1946.447805	970.093433	1690.661076	1653.341063	1707.211538	1550.246583	1670.567742
RBMI	2545.765718	1340.294785	2346.479719	2348.993720	2355.123168	2159.464735	2268.927742
average	820.976671	467.457911	821.951898	813.828180	816.593712	818.931110	830.309247
NewReligion	1.000000	1.436987	1.000000	1.000000	1.000000	1.000000	1.000000

Q14: Find the variances of AOR variable corresponding to each label of Religion variable.

```
d3_byReligion = d3.groupby('Religion')
```

```
d3_byReligion.std().transpose()
```

Output:

Religion	1	2
RMOB	3.494648	0.0
WI	1.423346	0.0
RCA	8.874438	0.0
Region	1.880966	0.0
AOR	3.273809	0.0
HEL	0.926591	0.0
DOBCMC	74.201189	0.0
DOFBCMC	107.415022	0.0
MTFBI	83.961840	0.0
RW	1402.118068	0.0
RH	1267.567788	0.0
RBMI	1247.216736	0.0
average	62.029359	0.0
NewReligion	0.000000	0.0

Q15: Draw a boxplot for the MTFBI variable.

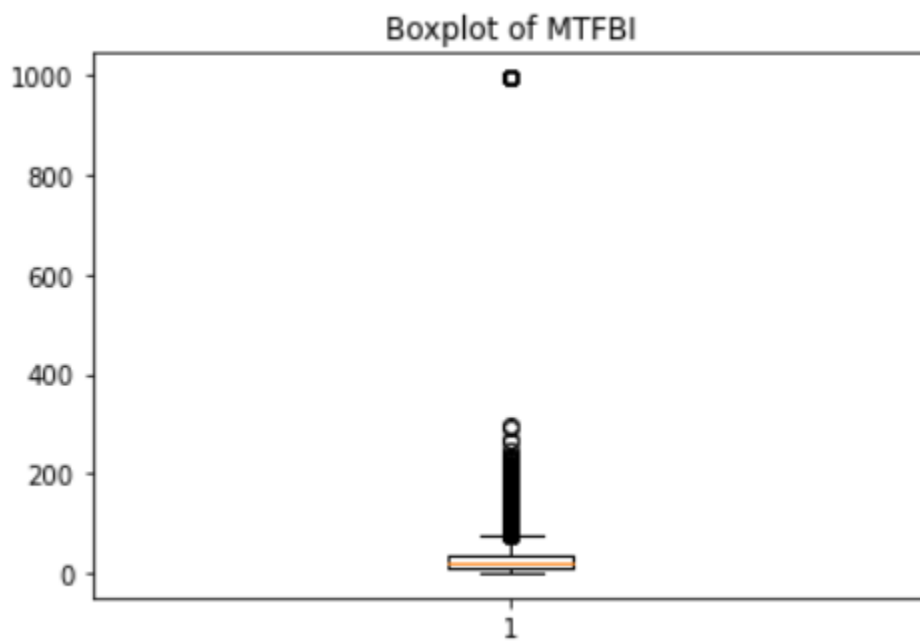
```
import matplotlib.pyplot as plt
```

```
y = d3['MTFBI']
```

```
plt.boxplot(y)
```

```
plt.title("Boxplot of MTFBI")
```

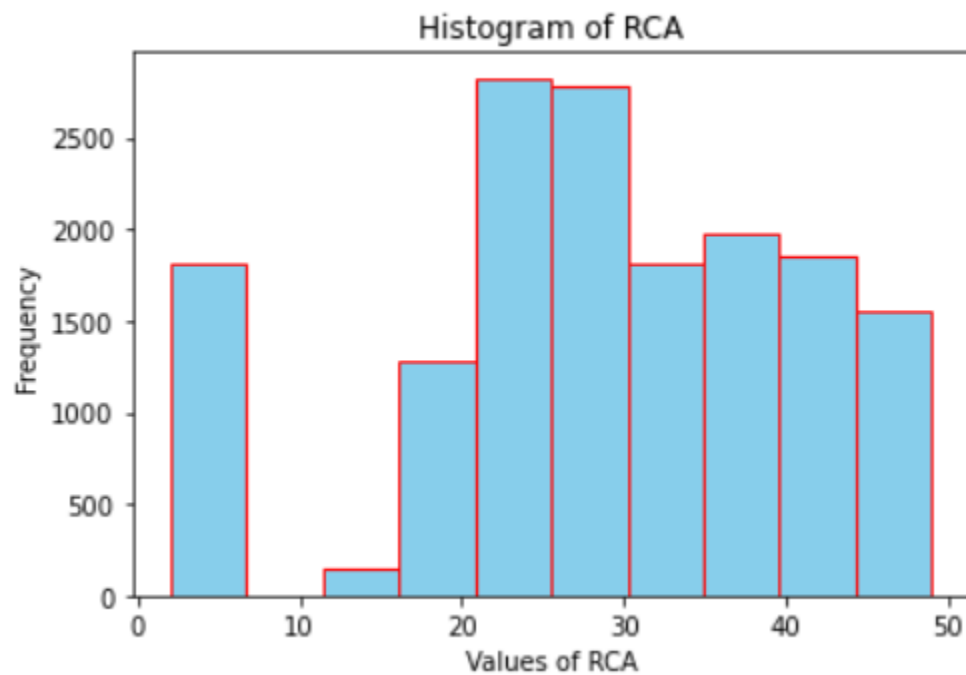
Output:



Q16: Draw a histogram for the RCA variable.

```
r = d3['RCA']  
plt.hist(r, color = "skyblue", ec = "red")  
plt.title("Histogram of RCA")  
plt.xlabel("Values of RCA")  
plt.ylabel("Frequency")
```

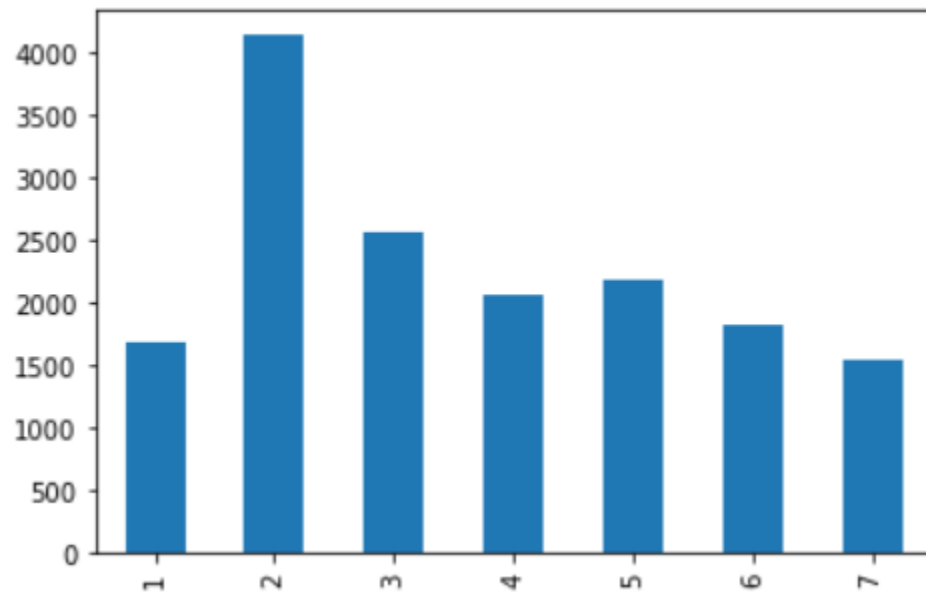
Output:



Q17: Draw a bar chart for the Region variable

```
d3['Region'].value_counts(sort = False).plot.bar()
```

Output:



Q18: Draw a pie chart for the Region variable

```
labels = ['1', '2', '3', '4', '5', '6', '7']
```

```
cols = ['r', 'b', 'g', 'y', 'c', 'w', 'm']
```

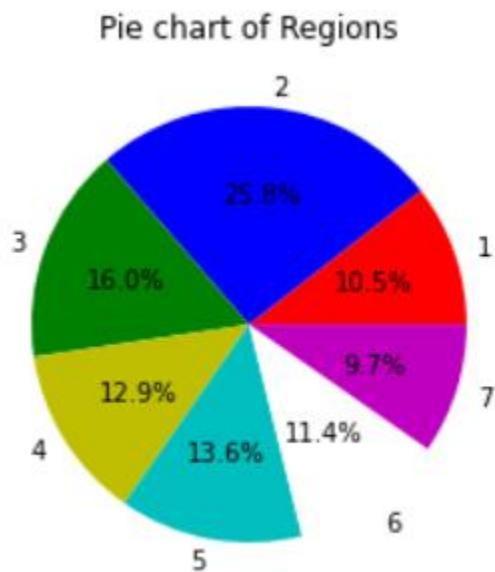
```
sizes = ['1686', '4142', '2564', '2070', '2184', '1829', '1550']
```

```
plt.pie(sizes, explode = None, labels = labels, autopct = '%1.1f%%', colors = cols)
```

```
plt.title("Pie chart of Regions")
```

```
plt.show()
```

Output:



Q19: Put above four figures (question 15 to question 18) in a 2 by 2 grid

```
b = d3['MTFBI']
```

```
h = d3['RCA']
```

```
reg = d3['Region']
```

```
ba = d3['Region'].value_counts(sort = False)
```

```
labels = ['1', '2', '3', '4', '5', '6', '7']
```

```
cols = ['r', 'b', 'g', 'y', 'c', 'w', 'm']
```

```
sizes = ['1686', '4142', '2564', '2070', '2184', '1829', '1550']
```

```
plt.subplot(2,2,2)
```

```
plt.hist(h, color = "skyblue", ec = "red")
```

```
plt.subplot(2,2,1)
```

```
plt.boxplot(b)
```

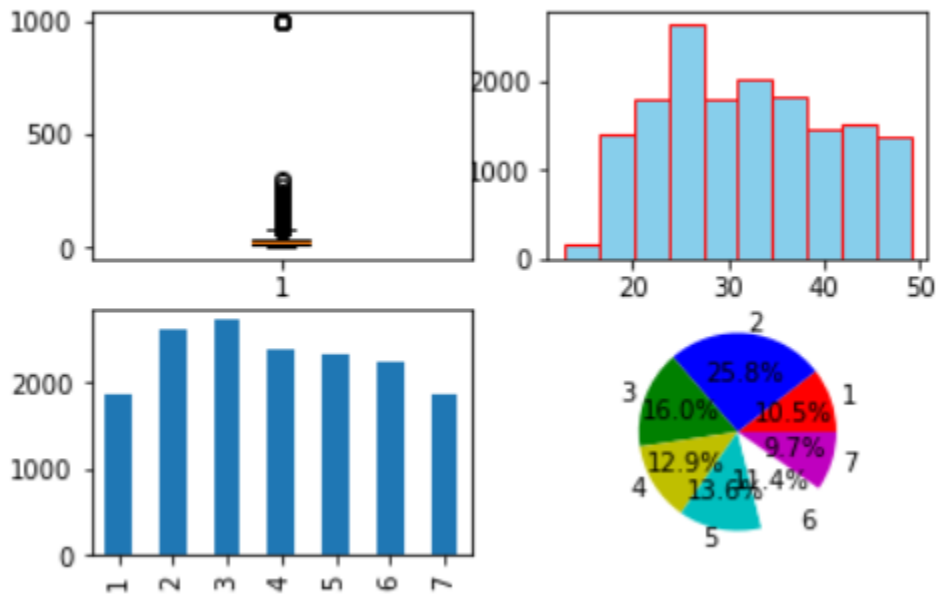
```
plt.subplot(2,2,3)
```

```
d3['Region'].value_counts(sort = False).plot.bar()
```

```
plt.subplot(2,2,4)
```

```
plt.pie(sizes, explode = None, labels = labels, autopct = '%1.1f%%', colors = cols)
```

Output:



Q20: Split the d3 data by WI variable and denote it by d4

```
d4 = d3.groupby('WI', as_index = False)
```

Output:

Q21: For each split data in d4 write a single loop to find the mean, minimum, maximum, standard deviation of MTFBI.

```
import statistics as ss
```

```
ds = [rows for _, rows in d4]
```

```
datalist = []
```

```
for i in range(len(ds)):
```

```

datalist.append(pd.DataFrame({'WI' : [ss.mean(ds[i].WI)], 'MTFBI mean' : [ss.mean(ds[i].MTFBI)],
                              'MTFBI min' : [min(ds[i].MTFBI)], 'MTFBI Max' : [max(ds[i].MTFBI)],
                              'MTFBI Variance' : [ss.variance(ds[i].MTFBI)]
                              , 'MTFBI Median' : [ss.median(ds[i].MTFBI)]}))

new_data = pd.concat(datalist)

print(new_data)

```

Output:

WI	MTFBI mean	MTFBI min	MTFBI Max	MTFBI Variance	MTFBI Median	
0	1	37.295088	0.0	996.0	7890.267841	22.0
0	2	21.975794	0.0	996.0	4433.464318	8.0
0	3	34.084646	0.0	996.0	6400.766659	22.0
0	4	34.814576	0.0	996.0	7217.257909	22.0
0	5	36.252577	0.0	996.0	6859.687171	23.0

Q22: Conduct a one sample mean test of hypothesis to check whether MTFBI has a mean of 30 or not.

```

import scipy.stats as st

st.stats.ttest_1samp(d3.MTFBI, 30)

```

Output: Ttest_1sampResult(statistic=2.8121680810452396, pvalue=0.004926859651115069)

Q23: Conduct a normality test of the MTFBI variable

```

import scipy

scipy.stats.shapiro(d3.MTFBI)

```

Output: ShapiroResult(statistic=0.24056196212768555, pvalue=0.0)

Q24: Check the equality of mean for MTFBI variable corresponding to two labels of “Newreligion” variable.

```

scipy.stats.ttest_ind(d3[d3.NewReligion == 1].MTFBI, d3[d3.NewReligion == 2].MTFBI)

```

Output: Ttest_indResult(statistic=17.0063732678908, pvalue=2.698791769280193e-64)

Q25: Find the correlation matrix of the variables DOBCMC, DOFBCMC, AOR, MTFBI, RW, RH and RBMI from the d3 data.

```

columns = ["DOBCMC", "DOFBCMC", "AOR", "MTFBI", "RW", "RH", "RBMI"]

c1=d3[columns]

import matplotlib.pyplot as plt

plt.matshow(c1.corr())

```

```
# correlation matrix
```

```
c1.corr()
```

Output:



Q27: Fit a multiple regression model by considering MTFBI as dependent variable and AOR, RW, Region as independent variables

```
#q27
```

```
import statsmodels.tools as sm
```

```
from statsmodels.api import OLS
```

```
y=d3.MTFBI
```

```
x=d3[['AOR','RW','Region']]
```

```
x1=sm.add_constant(x)
```

```
model = OLS(y, x1).fit()
```

```
model.summary()
```

Output:

Out[126]: OLS Regression Results

Dep. Variable:	MTFBI	R-squared:	0.030			
Model:	OLS	Adj. R-squared:	0.030			
Method:	Least Squares	F-statistic:	168.0			
Date:	Mon, 06 Dec 2021	Prob (F-statistic):	3.15e-107			
Time:	19:57:45	Log-Likelihood:	-92669.			
No. Observations:	16025	AIC:	1.853e+05			
Df Residuals:	16021	BIC:	1.854e+05			
Df Model:	3					
Covariance Type:	nonrobust					
	coef	std err	t	P> t	[0.025	0.975]
const	-7.0307	1.966	-3.577	0.000	-10.883	-3.178
AOR	2.3469	0.111	21.051	0.000	2.128	2.565
RW	-0.0004	0.000	-0.876	0.381	-0.001	0.001
Region	0.4137	0.346	1.196	0.232	-0.264	1.092
Omnibus:	26291.859	Durbin-Watson:	1.995			
Prob(Omnibus):	0.000	Jarque-Bera (JB):	12555518.901			
Skew:	11.269	Prob(JB):	0.00			
Kurtosis:	138.262	Cond. No.	4.70e+03			

Q28 – 32: Simulate one data from the following equation $y=50+10X+20U+100N+E$. Where X is binomial with $n=20$, $p=.70$. U is uniform between 15 and 30 (inclusive). N is normal with mean 0 and standard deviation 5. E is random uniform between -1 and 1. True mean is 640. True variance is 257920. Repeat the procedure 100 times and check the true mean with the simulated mean. Repeat the procedure 100 times and check the true variance with the simulated variance. Repeat the procedure 500 times and check the true mean with the simulated mean. Repeat the procedure 500 times and check the true variance with the simulated variance.

```
import numpy as np
import pandas as pd
import scipy.stats as stats
import statsmodels.stats.api as sms

#q28
def sim(n):
    x = np.random.binomial(20,.70,n)
    u = np.random.normal(0,5,n)
```



```

N = np.random.uniform(15,30,n)
E = np.random.uniform(-1, 1, n)
y= 50 + 10*x + 20 * u + 100 * N + E
y1=pd.DataFrame(y)
return y1

a = sim(1000)

# mean and variance
np.mean(a)
np.var(a)
stats.ttest_1samp(a,1000)
# repeating 100 times
B=100
repeat=[sim(1000) for i in range(B)]
alldata=pd.concat(repeat)
# computing mean and variance from simulated data
simulated_mean=np.mean(alldata)
simulated_variance=np.var(alldata)
# Theoretical Mean and Variance
theoretical_mean= 640
theoretical_variance= 257920
# difference between them
#29
print("100 iterations mean: " , abs(simulated_mean-theoretical_mean))
#30
print("100 iterations variance: " , abs(simulated_variance-theoretical_variance))

C=500

```

```

repeat=[sim(1000) for i in range(C)]
alldata=pd.concat(repeat)

# computing mean and variance from simulated data
simulated_mean=np.mean(alldata)
simulated_variance=np.var(alldata)

# Theoretical Mean and Variance
theoretical_mean= 640
theoretical_variance= 257920

# difference between them

#31
print("500 iterations mean: " , abs(simulated_mean-theoretical_mean))

#32
print("500 iterations variance: " , abs(simulated_variance-theoretical_variance))

```

Output:

```

100 iterations mean:  0      1798.40595
dtype: float64
100 iterations variance:  0      59598.103901
dtype: float64
500 iterations mean:  0      1800.528569
dtype: float64
500 iterations variance:  0      59601.945352

```

Q33: For five values of $x=1:5$, $y=2:6$, and $z=3:7$, compute 5 values for $f(x)=e^x - \log_{10}(z^2)/(5+y)$

```

import math

def fun(x, y, z):
    return (math.exp(x) - math.log(z**2))/(5+y)

```

```
x = 1
```

```
y = 2
```

```
z = 3
```

```
for i in range(5):
```

```
print(fun(x,y,z))
```

```
x += 1
```

```
y += 1
```

```
z += 1
```

Output:

```
0.07443675016040364
0.5770584220863586
1.8740734553688299
5.1014631094688125
13.138303527678726
```

Q34: Solve the following system of linear equations: $70x+100y+40z=900$; $120x+450y+340z=1000$; $230x+230y+1230z=3000$

```
a=np.array([[70,100,40],[120,450,340],[230,230,1230]])
```

```
b=np.array([900,1000,3000])
```

```
x=np.linalg.solve(a,b)
```

```
print(x)
```

Output:

```
[15.53852758 -1.8270015 -0.12491951]
```

Q35: Find the inverse of the following matrix: $A=(20, 30, 30$

$20,80,120$

$40,90,360)$

```
a = np.array([[20, 30, 30],
```

```
              [20, 80, 120],
```

```
              [40, 90, 360]])
```

```
print(np.linalg.inv(a))
```

Output:

```
[ [ 0.07317073 -0.03292683  0.00487805]
  [-0.0097561  0.02439024 -0.00731707]
  [-0.00569106 -0.00243902  0.00406504] ]
```

Q36: Suppose $b = \begin{pmatrix} 10 \\ 20 \\ 30 \end{pmatrix}$.

Then find $(A'A)^{-1} A'b$. Here A' means A transpose.

```
a_2 = a.transpose()
b = np.array([[10],
              [20],
              [30]])

v1 = np.linalg.inv(a_2.dot(a))
v2 = a_2.dot(b)
print(v1.dot(v2))
```

Output:

```
[ [ 0.2195122 ]
  [ 0.17073171]
  [ 0.01626016] ]
```

Q37: Draw the graph for the function $f(x) = e^x/x!$;for $2 \leq x \leq 15$.

```
import numpy as np
from matplotlib import pyplot as plt

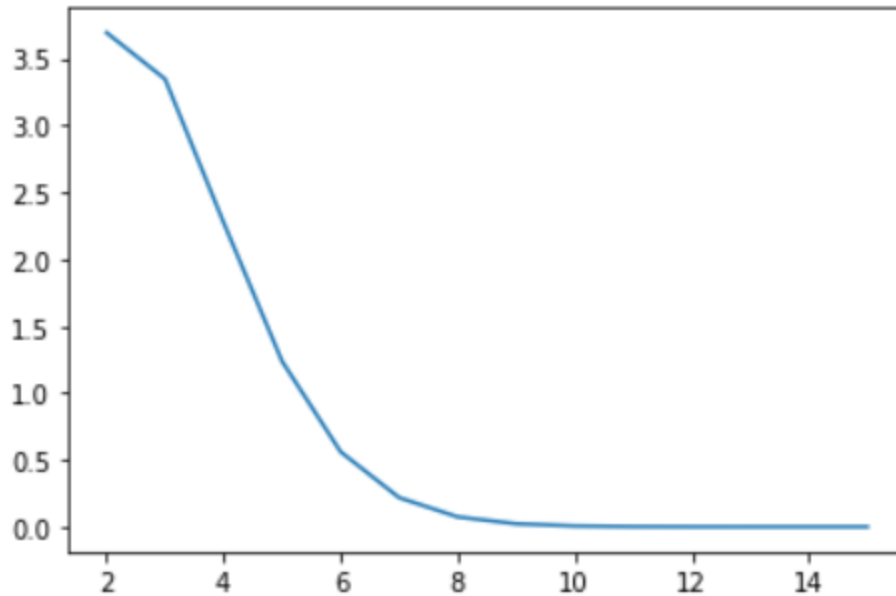
def f(x):
    return math.exp(x) / math.factorial(x)

x = [2,3,4,5,6,7,8,9,10,11,12,13,14,15]
y = []

for i in range(len(x)):
    y.append(f(x[i]))

plt.plot(x,y)
plt.show()
```

Output:



Q38: Draw the graph for the step functions Consider the continuous function

$$f(x) = \begin{cases} 2x^2 + e^x + 3; & \text{if } x < 0 \\ 9x + \log_{10}(20); & \text{if } 0 \leq x < 10 \\ 7x^2 + 5x - 17; & \text{if } 10 \leq x \end{cases}$$

$$9x + \log_{10}(20); \text{ if } 0 \leq x < 10$$

$$7x^2 + 5x - 17; \text{ if } 10 \leq x$$

def g(x):

 out = 0

 if x < 0:

 out = 2 * (x**2) + math.exp(x) + 3

 elif x >= 0 and x < 10:

 out = 9 * x + math.log(20)

 else:

 out = 7 * (x**2) + 5 * x - 17

 return out

x = [i for i in range(-10, 20)]

y = []

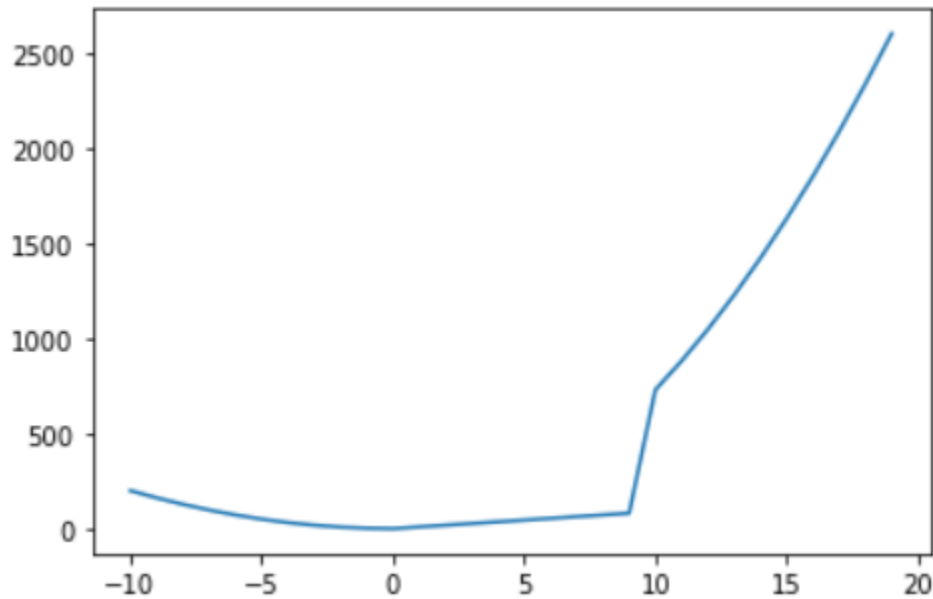
for i in range(len(x)):

 y.append(g(x[i]))

```
plt.plot(x, y)
```

```
plt.show()
```

Output:



Q39: Find the areas of 10 circles, which have radii 10:19. The Area of a circle is given πr^2 .

```
def circ_area(r):
```

```
    return math.pi * r**2
```

```
for i in range(10, 20):
```

```
    print("Area of circle with radius " + str(i))
```

```
    print(round(circ_area(i),2))
```

Output:

```
Area of circle with radius 10
314.16
Area of circle with radius 11
380.13
Area of circle with radius 12
452.39
Area of circle with radius 13
530.93
Area of circle with radius 14
615.75
Area of circle with radius 15
```

```
706.86
Area of circle with radius 16
804.25
Area of circle with radius 17
907.92
Area of circle with radius 18
1017.88
Area of circle with radius 19
1134.11
```

Q40: Find $\sum(1/\log x)$ for $x = 2$ to 10000

```
def h(x):
```

```
    return 1/(math.log(x))
```

```
sum = 0
```

```
for i in range(2, 10000):
```

```
    sum += h(i)
```

```
print(sum)
```

Output:

```
1245.839690648031
```

Q41: Find $\sum(i^{10}/(3+j))$ for $i = 1$ to 30 and $j = 1$ to 10

```
sum = 0
```

```
for i in range(30):
```

```
    for j in range(10):
```

```
        sum += (i ** 10)/ (3 + j)
```

```
print(sum)
```

Output:

```
2134775903297949.8
```

Q42: Compute the integral \int from 0 to positive infinity for equation: $x^{15} * e^{-40x} dx$.

```
from scipy.integrate import quad
```

```
def f(x):
```

```
return (x ** 15) * (math.exp(-(40 * x)))
```

```
res, err = quad(f, 0, math.inf)
```

```
print(res, err)
```

Output:

```
3.044666888955981e-14 2.76644736276991e-14
```

Q43: Compute the integral \int from 0 to 1 for equation: $x^{150} * (1-x)^{30}dx$

def g(x):

```
return (x ** 150) * (math.pow(1-x,30))
```

```
res,err = quad(g, 0 ,1)
```

```
print(res, err)
```

Output:

```
4.167698831230213e-37 6.182522311694294e-37
```

Q44: For five values of $x=1:5$, $y=2:6$, and $z=3:7$, compute 5 values for $f(x)=e^x - \log_{10}(z^2)/(5+y)$

```
import math
```

```
def fun(x, y, z):
```

```
return (math.exp(x) - math.log(z**2))/(5+y)
```

```
x = 1
```

```
y = 2
```

```
z = 3
```

```
for i in range(5):
```

```
    print(fun(x,y,z))
```

```
    x += 1
```

```
    y += 1
```

```
    z += 1
```


Output:

```
0.07443675016040364
0.5770584220863586
1.8740734553688299
5.1014631094688125
13.138303527678726
```

Q45: Solve the equation $x^2 - 33x + 1 = 0$.

```
import sympy as sym
```

```
solution = sym.solve('x**2 - 33 * x + 1', 'x')
```

```
solution[0]
```

Output:

$$\frac{33}{2} - \frac{\sqrt{1085}}{2}$$

Q47: If \$40 is invested today for 50 years with interest rate .10, the find the total amount of money in 50 years. The formula is $p(1+r)^t$. $p=40$, $t=50$, and $r=.10$.

```
def interest(p, t, r):
```

```
    return p * ((1 + r) ** t)
```

```
print(interest(40, 50, 0.1))
```

Output:

```
4695.634115187831
```

Q48: Fit a simple regression model by using MTFBI as dependent variable and AOR as independent variable.

```
import statsmodels.api as sm
```

```
model = sm.OLS(d3.MTFBI, d3.AOR).fit()
```

```
predictions = model.predict(d3.AOR)
```

```
model.summary()
```

Output:

OLS Regression Results						
Dep. Variable:		MTFBI		R-squared (uncentered):		0.162
Model:		OLS		Adj. R-squared (uncentered):		0.162
Method:		Least Squares		F-statistic:		3109.
Date:		Mon, 06 Dec 2021		Prob (F-statistic):		0.00
Time:		19:57:46		Log-Likelihood:		-92676.
No. Observations:		16025		AIC:		1.854e+05
Df Residuals:		16024		BIC:		1.854e+05
Df Model:		1				
Covariance Type:		nonrobust				
	coef	std err	t	P> t	[0.025	0.975]
AOR	2.0314	0.036	55.755	0.000	1.960	2.103
Omnibus:		26283.715		Durbin-Watson:		1.995
Prob(Omnibus):		0.000		Jarque-Bera (JB):		12520190.557
Skew:		11.263		Prob(JB):		0.00
Kurtosis:		138.069		Cond. No.		1.00

Q49: Check whether AOR and MTFBI are correlated or not.

```
import scipy
scipy.stats.pearsonr(d3.AOR, d3.MTFBI)
```

Output:

```
(0.1742337620135717, 1.9819270155456687e-109)
```

Q50: Check whether variance of AOR is 10 or not.

```
def chi_sq_test_for_variance(variable, h0):
    sample_variance = variable.var()
    n = variable.notnull().sum()
    degrees_of_freedom = n - 1
    x_sq_stat = (n-1) * sample_variance / h0
    p = stats.chi2.cdf(x_sq_stat, degrees_of_freedom)

    if p > 0.05:
```

```
p = 1 - p
return (x_sq_stat,p,degrees_of_freedom)

aor_variance = round(d3["AOR"].var(),2)
x_sq_stat,pval,dof = chi_sq_test_for_variance(d3["AOR"], h0 = 10)
print(round(x_sq_stat, 2),pval,dof)
```

Output:

```
55214.29 0.0 16024
```