

Johns Hopkins
Engineering for Professionals
605.767 Applied Computer Graphics

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Module 3C

Procedural Texturing



Procedural Textures

- Applying Texture to Ray Tracing
 - 3D and procedural textures
 - Wood grain
 - Perlin noise, turbulence, marble texture
- Texture Mapping



Adding Surface Texture to Ray Tracing

- Two methods of adding textures to ray-traced images
 - Solid or 3D texture
 - Usually a procedural method
 - <http://www.upvector.com/?section=Tutorials&subsection=Intro%20to%20Procedural%20Textures>
 - Image texture
 - Image is pasted onto the surface of the object
- Use the color returned from the texture function in one of 2 ways:
 - Use the texture color in place of the local illumination
 - “Decal” texture method
 - Use the texture color to modulate the local illumination
 - Modulate just the ambient and diffuse components
 - Modulate the entire local illumination



Three Dimensional Textures

- 3D texture mapping overcomes some of the 2D texture mapping problems
 - Particularly mapping and aliasing issues
 - Mapping 2D textures to complex objects can be difficult
- Solid textures assign texture values at all points in 3D texture space
 - Often called **solid texture**
 - Developed by Perlin and Peachey (1985)
 - Solid textures may have a lattice of texture values within some volume
 - Interpolate between lattice points for intermediate values
 - Most useful for simulating materials such as wood, concrete, marble
 - Internal structure of the material may be important
- Memory costs for storing a high resolution 3D texture is high
 - Procedural methods are generally used
 - Although it eliminates mapping difficulties, texture patterns are limited to definitions that can be analytically constructed
 - 2D texture mapping has a wealth of available frame-grabbed images



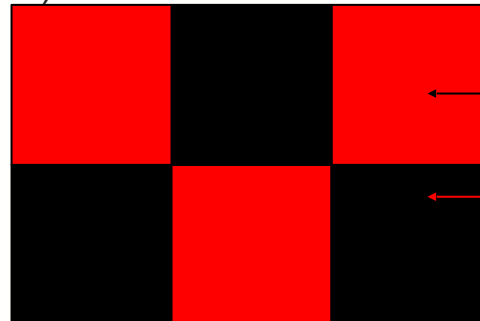
Solid Textures

- Procedural texture mapping
 - 3D texture maps are generally not stored because they would be too large
 - Procedurally defined and computed when needed
 - The texture map is defined in three dimensions, $T(x,y,z)$
 - $\text{color} = f(x, y, z)$
 - Known as the **identity mapping**
 - Color produced depends on position
 - A function (or procedural method) finds the corresponding point in the 3D texture map space
 - Evaluate a 3D texture function at the object's surface points
 - Analogous to sculpting or carving an object out of a block of material (e.g. wood)
 - Object color determined by the intersection of the surface with the texture field
 - For ray traced images, the intersection point is the 3D world point to use in the procedural texture
- Under modeling transformations: perform same transformations to the texture field as the object
 - Or map object into texture field using inverse of modeling transform
 - Such that the texture remains static on the surface of the object
 - However, moving an object through a static texture field can produce interesting effects



Checkerboard

- Simple example: checkerboard
- Boxes of alternating colors
 - Specify box dimensions (C_x , C_y , C_z)
 - Add the integer values of x, y, z divided by their cube dimension
 - Determine if the result is even or odd (mod 2)
 - If even: assign one color, if odd: assign other color
 - $((\text{int})(x/C_x) + (\text{int})(y/C_y) + (\text{int})(z/C_z)) \% 2$
- Issues
 - Truncation to int causes anomalies near 0
 - Can add a constant to translate x, y, z away from 0
 - Can have round off issues with the (int) truncation if a planar surface to be textured lies on a constant integral value (such as $z = 0.0$)



2.5, 1.5 = $(2+1)\%2=1$ (odd)

2.8, 0.9 = $(2+0)\%2=0$ (even)

2D Example with Unit Squares

Wood Grain Texture

- Wood grain can be simulated by a set of concentric cylinders with varying colors
 - As distance from an axis varies color jumps back and forth between 2 alternating values
 - For rings about the z axis: $rings(r) = ((\text{int})r) \% 2$ $r = \sqrt{x^2 + y^2}$

- Can jump between 2 values: D and D+A

$$wood(x,y,z) = D + A * rings\left(\frac{r}{M}\right)$$

- Produces rings of thickness M that are concentric about the z axis
- Can add interest by “wobbling” about the axis
 - Perturb r with a sinusoidal function

$$rings\left(\frac{r}{M} + K\sin\left(\frac{\theta}{N}\right)\right) \quad \theta = \tan^{-1}\left(\frac{x}{y}\right)$$

- Fluctuation of rings as theta varies
- Makes the ring wobble in and out N times about the z axis
- K: constant to determine the max variance of the “wobble”

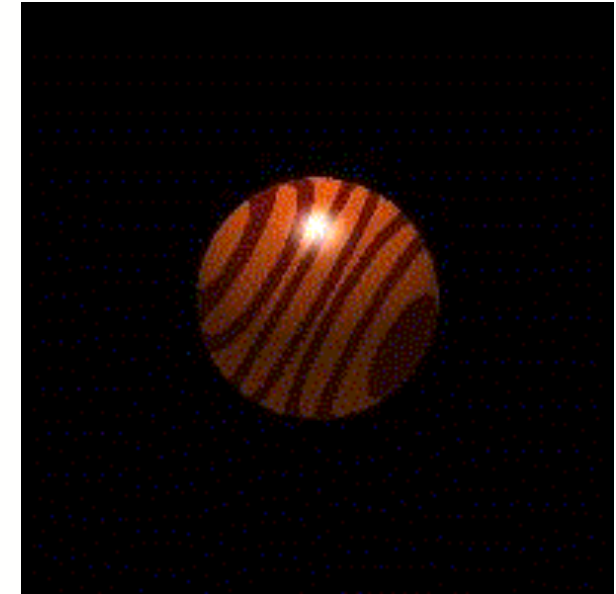


Wood Grain Texture (continued)

- Add a twist along the axis of the cylinders

$$rings\left(\frac{r}{M} + K\sin\left(\frac{\theta}{N} + Bz\right)\right)$$

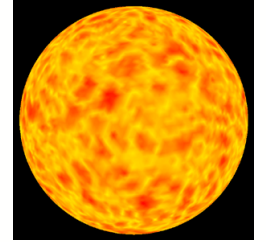
- To get textures so it is concentric about other than the z-axis
 - Apply a “tilt” function
 - $r = \sqrt{x'^2 + y'^2}$, where $(x', y', z') = T(x, y, z)$
 - T is a rotational transformation



[Link no longer valid]

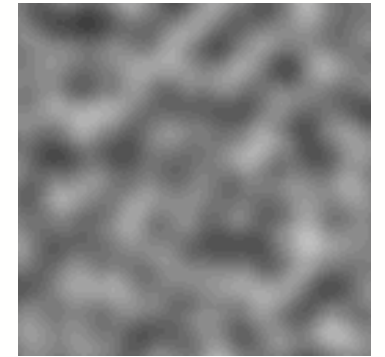
3D Noise Function

- Common basis of solid texture is a pseudo random noise function
- Noise function designed to have the following properties:
 - Statistical invariance under rotation
 - Statistical invariance under translation
 - Narrow bandpass limit in frequency (has no visible features larger or smaller than a certain range)
 - Statistical properties are the same when measured over different areas with different orientations
 - Function can be sampled without aliasing (band limited in frequency)
- Useful to model natural phenomena like clouds, wood, patterns in rock, fire
 - Appearance is random but has recognizable pattern



Perlin's Noise Function

- Perlin (1985) defined a $\text{noise}(x,y,z)$ function
 - Returns a single scalar value given a 3D position
- Created by smoothly interpolating between random values
 - In 3D: define integer lattice at locations (i,j,k) where i,j,k are integers
 - Each point on the lattice has a random number associated with it
 - Value of the noise function for points not on the lattice is found by interpolating from nearby lattice points
- Collection of noise values could be stored in a large 3D array
 - Would require lots of storage
- Easy to generate noise value each time it is used
 - `float latticeNoise(int i, int j, int k)`
 - Function must be efficient and repeatable
 - Always returning the same noise value for a specific (i,j,k)



http://en.wikipedia.org/wiki/Perlin_noise

Lattice Noise Function

- A noise initialization to set up the noise lattice
 - Create a fixed array of n pseudorandom noise values: **noiseTable**
 - Array of 256 or 512 is sufficient
 - Can be created with standard C function rand() scaled to lie in range[0,1]
- latticeNoise(i,j,k) indexes noise table in a repeatable manner
 - Use a hash function to scramble i,j,k input into an index
 - Minimizes any patterns seen in the noise values
 - Can do this with a second array of n values randomly permuted: **indexTable**
 - e.g. for n = 8: {2, 6, 4, 0, 5, 1, 7, 3}
 - Peachey suggests using 2 methods / macros
 - `int PERM(int x) { return indexTable[x & 255]; }`
 - Retains only the low order 8 bits
 - `int INDEX(int ix, int iy, int iz) { return PERM(ix + PERM(iy+ PERM(iz)));}`

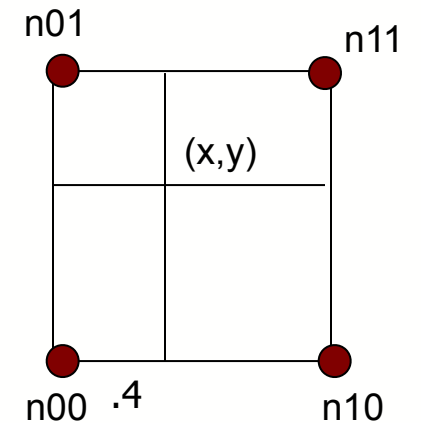
```
float latticeNoise(int i, int j, int k) { return noiseTable[INDEX(i, j, k)]; }
```



Linear Interpolation of Lattice Noise

- Implement a function $\text{noise}(x,y,z)$ that produces a pseudorandom value for any x,y,z
 - Want noise to vary smoothly as x,y,z vary
- Linear interpolation between lattice values produces acceptable results
 - Perlin and Peachey suggest that cubic interpolation provides more realistic results
 - $\text{lerp}(f, A, B) \{ \text{return } (A + f * (B - A)); \}$
- Sample noise method follows (from FS Hill)
 - Input a point and a scale value
 - Scale value and offset to ensure all components are positive
 - Does not impact the nature of the noise generated
 - Generate noise values at the eight lattice positions that surround the vertex
 - Perform linear interpolation

2D Example



Interpolate in x along $y=0$ and $y=1$
 $n(0.4,0)=\text{lerp}(0.4, n00, n10)$
 $n(0.4,1)=\text{lerp}(0.4, n01, n11)$
Then interpolate these in y
 $n(0.4,0.6)=\text{lerp}(0.6, n(0.4,0), n(0.4,1))$

Sample Noise Method

```
float noise(const Point3& p, const float scale) {
    Point3 pp(p.x*scale+10000, p.y*scale+10000, p.z*scale+10000);
    int ix  = (int)pp.x;          // Integer x
    float tx = pp.x - ix;         // Fractional part
    int iy  = (int)pp.y;          // Integer y
    float ty = pp.y - iy;         // Fractional part
    int iz  = (int)pp.z;          // Integer z

    // Get noise at 8 lattice points
    float d[2][2][2];
    for (int k = 0; k < 2; k++)
        for (int j = 0; j < 2; j++)
            for (int i = 0; i < 2; i++)
                d[k][j][i] = latticeNoise(ix+i, iy+j, iz + k);

    // Linear interpolation
    float x0 = lerp(tx, d[0][0][0], d[0][0][1]);
    float x1 = lerp(tx, d[0][1][0], d[0][1][1]);
    float x2 = lerp(tx, d[1][0][0], d[1][0][1]);
    float x3 = lerp(tx, d[1][1][0], d[1][1][1]);
    float y0 = lerp(ty, x0, x1);
    float y1 = lerp(ty, x2, x3);
    return lerp(pp.z - iz, y0, y1);
}
```



Scaled Noise Functions

- Many noise sampling functions require scaling the noise parameters
 - Can also add an offset
 - Scaled noise

$$\textit{scaledNoise}(s, x, y, z) = \textit{noise}((s * x), (s * y), (s * z))$$

- Scaled and Offset noise

$$\textit{scaledOffsetNoise}(s, o, x, y, z) = \textit{noise}((s * x + o), (s * y + o), (s * z + o))$$



Turbulence

- Common use of noise is with Perlin's turbulence function
 - Perlin used it to provide the appearance of marble
 - Perturbed sine wave to modulate color
 - Turbulence adds instances of Perlin noise
 - Creates a fractal character
- Turbulence mixes together several noise components
 - One that fluctuates slowly, one that fluctuates twice as fast, one that fluctuates four times as fast, etc.
 - Each successive term is given a smaller strength
 - For example:
$$turbulence(s, x, y, z) = \frac{1}{2}noise(s, x, y, z) + \frac{1}{4}noise(2s, x, y, z) + \frac{1}{8}noise(4s, x, y, z)$$
 - Parameter s scales distances



Turbulence

- Perlin's turbulence function takes a position and returns a turbulent scalar value

- Written in terms of a progression:

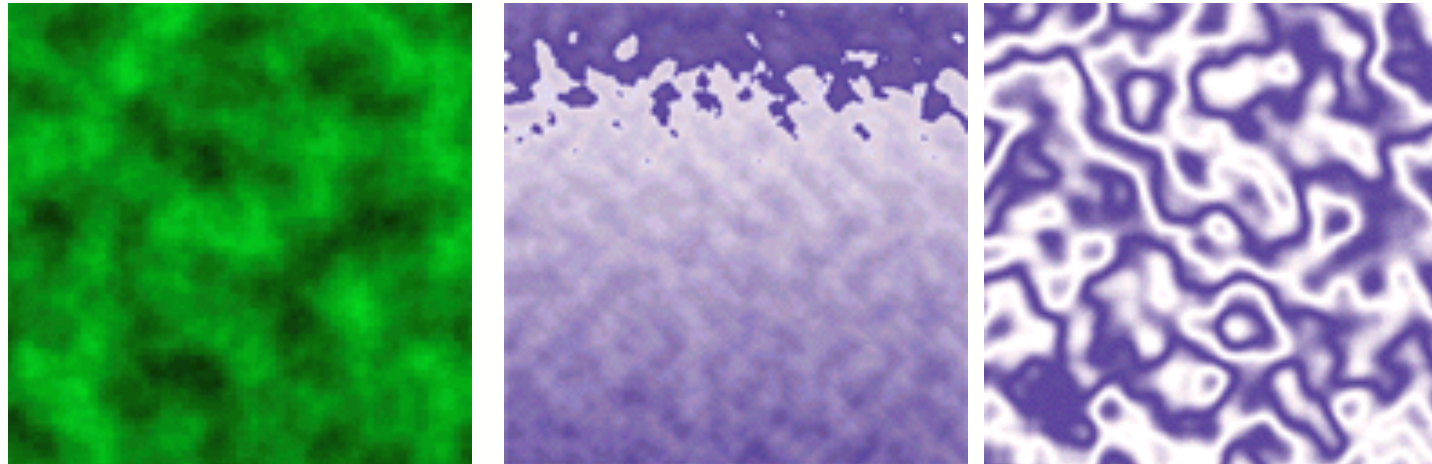
$$turbulence(s, x, y, z) = \sum_{k=0}^M \frac{1}{2^k} noise(2^k, s, x, y, z)$$

- M is the smallest integer satisfying $1 / (2^{M+1}) < \text{size of a pixel}$
 - Truncation limits the function to ensure proper anti-aliasing
 - Between successive terms the noise function will vary twice as fast in the second as the first
 - Will contain features that are half the size
 - At each detail scale the amount of noise added to the series is proportional to the detail scale and inversely proportional to the frequency of the noise
 - Self similarity



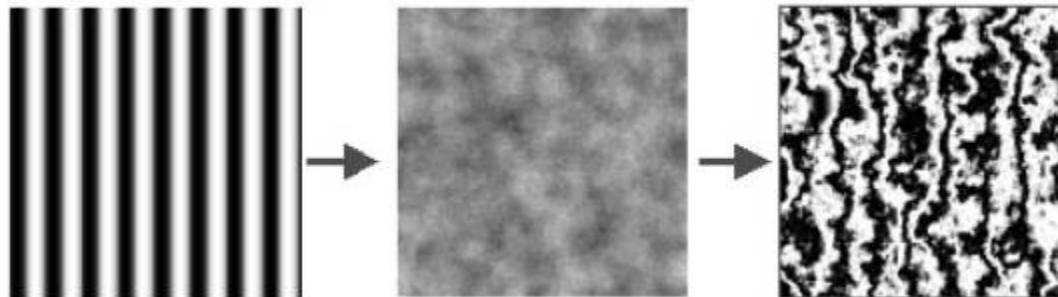
Turbulence

- Simulating turbulence is a two stage process
 - Represent the basic, first-order structural features of the texture through some functional form
 - Function is typically continuous and contains significant variations in its first derivative
 - Example: \sin
 - Addition of second and higher order detail by using turbulence to perturb the parameters of the function



Using Turbulence to Generate Marble Textures

- Perlin described turbulation of a sine wave to give the appearance of marble
 - Unperturbed color veins described by a sine wave and an intensity map
 - $\text{marble}(x) = \text{MarbleColor}(\sin(x))$
 - MarbleColor is a spline curve - mapping a scalar input to intensity
 - Add turbulence
 - $\text{marble}(x) = \text{MarbleColor}(\sin(x + \text{turbulence}(x)))$



Flame

- Watt and Watt describe using turbulence to create animated flame
 - Using a turbulence function defined over time
- Define a general flame shape: minimax coordinates $(-b,0)$, (b,h) in x,y plane
 - Define flame color: 3 spline curves mapping R,G,B intensity
 - Maximum intensity at $x = 0$ (flame center): falling off to 0 at $x = 1$
 - Blue and green fall off faster than red
 - Weight color based on height from the base to get variation in y
 - Apply turbulence
 - $\text{flame}(x,t) = (1 - y/h) \text{flame_color}(\text{abs}(x/b) + \text{turbulence}(x,t))$
- Apply $\text{flame}()$ to color a rectangular polygon covering the flame



Image Texture Mapping and Ray Tracing

- Need to associate an inverse mapping from object coordinates (x,y,z) to texture coordinates
 - Requires different mappings for different shapes
- Example: square
 - Simple scaling and translation
- Example: sphere
 - Convert x,y,z to latitude, longitude
 - Scale lat, lon values to lie in $[0,1]$ texture coordinate range
- Inverse mapping for triangle mesh objects
 - If object is modeled using a triangle mesh AND texture coordinates are associated with each vertex we can use barycentric coordinates to interpolate texture values
 - u,v from the ray/Triangle intersect method
 - Provides weightings to apply to each vertex's texture coordinate

