# Fitting regression models EDH7916 | Spring 2020

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After your data have been wrangled from raw values to an analysis data set and you've explored it with summary statistics and graphics, you are ready to model it and begin making inferences. As one should expect from a statistical language, R has a powerful system for fitting statistical and econometric models.

In this lesson, we'll use data from the NCES Education Longitudinal Study of 2002. Much like HSLS, ELS is a nationally representative survey that initially surveyed students in their early high school career (10th grade) and followed them into college and the workforce. We'll use a smaller version of it because, unlike HSLS, the public use files for ELS include the variables we need to properly account for the survey design when we weight our data. Here's a codebook with descriptions of the variables included in our lesson today:

variable	description
stu_id	student id
$sch\_id$	school id
$strat\_id$	stratum
psu	primary sampling unit
bystuwt	student weight
bysex	sex-composite
byrace	student's race/ethnicity-composite
bydob_p	student's year and month of birth
bypared	parents' highest level of education
bymothed	mother's highest level of education-composite
byfathed	father's highest level of education-composite
byincome	total family income from all sources 2001-composite
byses1	socio-economic status composite, v.1
byses2	socio-economic status composite, v.2
bystexp	how far in school student thinks will get-composite
bynels2m	els-nels 1992 scale equated sophomore math score
bynels2r	els-nels 1992 scale equated sophomore reading score
f1qwt	questionnaire weight for f1
f1pnlwt	panel weight, by and f1 (2002 and 2004)
f1psepln	fl post-secondary plans right after high school
f2ps1sec	Sector of first postsecondary institution
female	== 1 if female
moth_ba	== 1 if mother has BA/BS
fath_ba	== 1 if father has BA/BS
par_ba	== 1 if either parent has BA/BS
$plan\_col\_grad$	== 1 if student plans to earn college degree
lowinc	== 1  if income < \$25k

Let's load the libraries and data!

...but first! You'll most likely need to install the survey package first, using install.packages("survey").

```
## libraries
library(tidyverse)
— Attaching packages —
                                                        —— tidyverse 1.3.0 —

✓ ggplot2 3.3.0

✓ purrr 0.3.3

✓ tibble 3.0.0 ✓ dplyr 0.8.5

✓ tidyr 1.0.2

✓ stringr 1.4.0

✓ readr 1.3.1

✓ forcats 0.5.0

— Conflicts —
                                                  ——— tidyverse_conflicts() —
* dplyr::filter() masks stats::filter()
               masks stats::lag()
* dplyr::lag()
library(haven)
library(survey)
Loading required package: grid
Loading required package: Matrix
Attaching package: 'Matrix'
The following objects are masked from 'package:tidyr':
   expand, pack, unpack
Loading required package: survival
Attaching package: 'survey'
The following object is masked from 'package:graphics':
   dotchart
## directory paths
## assume we're running this script from the ./scripts subdirectory
dat_dir <- file.path("..", "data")</pre>
## input data
## assume we're running this script from the ./scripts subdirectory
df <- read_dta(file.path(dat_dir, "els_plans.dta"))</pre>
```

#### t-test

One common statistical test is a t-test for a difference in means across groups (there are, of course, others and R can compute them). This version of the test can be computed using the R formula syntax:  $y \sim x$ . In

our example, we'll compute base-year math scores against mother's college education level. Notice that since we have the data = df argument after the comma, we don't need to include df\$ before the two variables.

Quick exercise Run a t-test of reading scores against whether the father has a Bachelor's degree (fath ba).

## Linear model

Linear models are the go-to method of making inferences for many data analysts. In R, the lm() command is used to compute an OLS regression. Unlike above, where we just let the t.test() output print to the console, we can and will store the output in an object.

First, let's compute the same t-test but in a regression framework. Because we assumed equal variances between the distributions in the t-test above (var.equal = TRUE), we should get the same results as we did before.

The output is a little thin: just the coefficients. To see the full range of information you want from regression output, use the summary() function wrapped around the fit object.

```
output, use the summary() function wrapped around the fit object.

## use summary to see more information about regression
summary(fit)

Call:
lm(formula = bynels2m ~ moth_ba, data = df)

Residuals:
    Min    10 Median    30 Max
-36.073 -9.869    0.593    10.004    36.223

Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 43.0471     0.1245     345.84     <2e-16 ***
moth_ba     8.4958     0.2376     35.75     <2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

Residual standard error: 13.09 on 15234 degrees of freedom
(924 observations deleted due to missingness)

Multiple R-squared: 0.07741, Adjusted R-squared: 0.07735
F-statistic: 1278 on 1 and 15234 DF, p-value: < 2.2e-16
```

Looks like the coefficient on moth\_ed, 8.4958392, is the same as the difference between the groups in the ttest, 8.4958392, and the test statistics are the same value: -35.7511914. Success!

# Multiple regression

To fit a multiple regression, use the same formula framework that we've use before with the addition of all the terms you want on right-hand side of the equation separated by plus (+) signs.

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 45.7155
                        0.1811 252.420 < 2e-16 ***
                        0.2387 28.511 < 2e-16 ***
byses1
             6.8058
female
            -1.1483
                        0.1985 -5.784 7.42e-09 ***
moth_ba
             0.4961
                        0.2892
                                1.715 0.08631 .
fath_ba
             0.8242
                        0.2903
                                2.840 0.00452 **
lowinc
            -2.1425
                        0.2947 -7.271 3.75e-13 ***
```

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 12.24 on 15230 degrees of freedom (924 observations deleted due to missingness)

Multiple R-squared: 0.1929, Adjusted R-squared: 0.1926

F-statistic: 728.1 on 5 and 15230 DF, p-value: < 2.2e-16

The full output tells you:

- the model that you fit, under Call:
- a table of coefficients with
  - the main estimate (Estimate)
  - the estimate error (Std. Error)
  - the test statistic (t value with this model)
  - the p value (Pr(>|t|)

- significance stars (. and \*) along with legend
- the R-squared values (Multiple R-squared and Adjusted R-squared)
- the model F-statistic (F-statistic)
- number of observations dropped if any

If observations were dropped, you can recover the number of observations used with the nobs() function.

```
## check number of observations
nobs(fit)
```

#### [1] 15236

The fit object also holds a lot of other information that is sometimes useful.

```
## see what fit object holds
names(fit)
```

```
[1] "coefficients" "residuals" "effects" "rank"
[5] "fitted.values" "assign" "qr" "df.residual"
[9] "na.action" "xlevels" "call" "terms"
[13] "model"
```

For example, both fitted.values and residuals are stored in the object. You can access these "hidden" attributes by treating the fit object like a data frame and using the \$ notation.

```
1 2 3 4 5 6
4.974173 6.785347 27.457659 -1.650095 -2.858552 -14.153323
```

Quick exercise Add the fitted values to the residuals and store in an object (x). Compare these values to the math scores in the data frame.

As a final note, the model matrix used fit the regression can be retrieved using model.matrix(). Since we have a lot of observations, we'll just look at the first few rows.

```
## see the design matrix
head(model.matrix(fit))
```

```
(Intercept) byses1 female moth_ba fath_ba lowinc
1
             1 - 0.25
                            1
                                     0
2
             1
                 0.58
                            1
                                     0
                                                     0
                                              0
3
               -0.85
                            1
4
               -0.80
             1
                            1
                                     0
                                              0
                                                     1
                -1.41
                                                     1
             1 - 1.07
```

What this shows is that the fit object actually stores a copy of the data used to run it. That's really convenient if you want to save the object to disk (with the save() function) so you can review the regression results later. But keep in mind that if you share that file, you are sharing the part of the data used to estimate it.

# Using categorical variables or factors

It's not necessary to pre-construct dummy variables if you want to use a categorical variable in your model. Instead you can use the categorical variable wrapped in the <code>factor()</code> function. This tells R that the underlying variable shouldn't be treated as a continuous value, but should be discrete groups. R will make the dummy variables on the fly when fitting the model. We'll include the categorical variable <code>byrace</code> in this model.

```
## add factors
fit <- lm(bynels2m ~ byses1 + female + moth_ba + fath_ba + lowinc + factor(byrace),
          data = df
summary(fit)
Call:
lm(formula = bynels2m ~ byses1 + female + moth_ba + fath_ba +
    lowinc + factor(byrace), data = df)
Residuals:
   Min
             10 Median
                             30
                                   Max
-39.154 -8.387
                 0.424
                          8.639 39.873
Coefficients:
                Estimate Std. Error t value Pr(>|t|)
(Intercept)
                 40.6995
                            1.0386 39.189 < 2e-16 ***
                             0.2345 24.456 < 2e-16 ***
byses1
                  5.7360
female
                 -1.1955
                             0.1900 -6.293 3.21e-10 ***
moth_ba
                  0.6500
                             0.2780
                                      2.338 0.019407 *
fath_ba
                  0.8482
                             0.2796
                                      3.033 0.002423 **
lowinc
                 -1.2536
                             0.2839 -4.416 1.01e-05 ***
                                     8.523 < 2e-16 ***
                 9.1538
factor(byrace)2
                             1.0740
factor(byrace)3 -2.2185
                             1.0603 -2.092 0.036419 *
factor(byrace)4
                 1.2778
                             1.0937
                                      1.168 0.242696
factor(byrace)5
                 0.2387
                             1.0814
                                      0.221 0.825295
                                      3.805 0.000142 ***
factor(byrace)6
                 4.2457
                             1.1158
factor(byrace)7
                 6.9514
                             1.0379
                                      6.698 2.19e-11 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 11.71 on 15224 degrees of freedom
  (924 observations deleted due to missingness)
Multiple R-squared: 0.2613,
                               Adjusted R-squared: 0.2608
F-statistic: 489.6 on 11 and 15224 DF, p-value: < 2.2e-16
```

If you're using labeled data like we have been for the past couple of modules, you can use the <code>as\_factor()</code> function from the haven library in place of the base <code>factor()</code> function. You'll still see the <code>as\_factor(<var>)</code> prefix on each coefficient, but now you'll have labels instead of the underlying values, which should make parsing the output a little easier.

```
lm(formula = bynels2m ~ byses1 + female + moth_ba + fath_ba +
lowinc + as_factor(byrace), data = df)
```

```
Residuals:
    Min
             10 Median
                              30
                                    Max
-39.154 -8.387
                  0.424
                           8.639 39.873
Coefficients:
                           Estimate Std. Error t value Pr(>|t|)
(Intercept)
                                         1.0386 39.189 < 2e-16 ***
                            40.6995
                                         0.2345 24.456 < 2e-16 ***
byses1
                             5.7360
female
                            -1.1955
                                         0.1900 -6.293 3.21e-10 ***
moth_ba
                             0.6500
                                         0.2780
                                                  2.338 0.019407 *
fath_ba
                             0.8482
                                         0.2796
                                                 3.033 0.002423 **
                                         0.2839 -4.416 1.01e-05 ***
lowinc
                            -1.2536
as_factor(byrace)asian_pi
                             9.1538
                                         1.0740
                                                  8.523 < 2e-16 ***
as_factor(byrace)black_aa
                            -2.2185
                                         1.0603 -2.092 0.036419 *
as_factor(byrace)hisp_nr
                             1.2778
                                         1.0937
                                                  1.168 0.242696
as_factor(byrace)hisp_rs
                             0.2387
                                         1.0814
                                                  0.221 0.825295
                                         1.1158
                                                  3.805 0.000142 ***
as_factor(byrace)mult_race
                             4.2457
as_factor(byrace)white
                              6.9514
                                         1.0379
                                                  6.698 2.19e-11 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 11.71 on 15224 degrees of freedom
  (924 observations deleted due to missingness)
Multiple R-squared: 0.2613,
                                Adjusted R-squared: 0.2608
F-statistic: 489.6 on 11 and 15224 DF, p-value: < 2.2e-16
If you look at the model matrix, you can see how R created the dummy variables from byrace.
## see what R did under the hood to convert categorical to dummies
head(model.matrix(fit))
  (Intercept) byses1 female moth_ba fath_ba lowinc as_factor(byrace)asian_pi
            1 -0.25
                          1
                                   a
                                           0
                                                                             0
1
                                                  0
2
            1
                0.58
                           1
                                   0
                                                  0
                                                                             1
3
            1 -0.85
                                   0
                                                                             0
                           1
                                           0
                                                  0
4
            1 - 0.80
                           1
                                   0
                                                  1
                                                                             0
5
            1 -1.41
                           1
                                   0
                                                                             0
                                           0
                                                  1
            1 - 1.07
                           0
                                                  0
  as_factor(byrace)black_aa as_factor(byrace)hisp_nr as_factor(byrace)hisp_rs
1
                                                    0
2
                           0
                                                    0
                                                                              0
3
                           0
                                                                              0
                                                    0
4
                           1
                                                    0
                                                                              0
5
                                                    1
                                                                              0
                                                    1
  as_factor(byrace)mult_race as_factor(byrace)white
1
                                                   0
2
                           0
                                                   0
3
                           0
                                                   1
4
                           0
                                                   0
5
                           0
                                                   0
                                                   0
6
```

Quick exercise Add the categorical variable byincome to the model above. Next use model.matrix() to check the RHS matrix.

#### Interactions

Add interactions to a regression using an asterisks (\*) between the terms you want to interact. This will add both main terms and the interaction(s) between the two to the model. Any interaction terms will be labeled using the base name or factor name of each term joined by a colon (:).

```
## add interactions
fit <- lm(bynels2m ~ byses1 + factor(bypared)*lowinc, data = df)</pre>
summary(fit)
Call:
lm(formula = bynels2m \sim byses1 + factor(bypared) * lowinc, data = df)
Residuals:
   Min
             10 Median
                             30
                                    Max
-38.998 -8.852
                  0.326
                          9.063
                                39.257
Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
(Intercept)
                         44.0084
                                     0.6345 69.355 < 2e-16 ***
byses1
                          7.6082
                                     0.2772 27.448 < 2e-16 ***
factor(bypared)2
                          1.5546
                                     0.6544
                                              2.376 0.017533 *
                                     0.7136
                                              0.916 0.359863
factor(bypared)3
                          0.6534
factor(bypared)4
                          1.8902
                                     0.7198
                                              2.626 0.008646 **
factor(bypared)5
                          1.5059
                                     0.7200
                                              2.091 0.036501 *
                                     0.7386
                                              1.967 0.049235 *
factor(bypared)6
                          1.4527
                                     0.8286
factor(bypared)7
                          2.0044
                                             2.419 0.015569 *
factor(bypared)8
                          0.8190
                                     0.9239
                                              0.887 0.375360
lowinc
                          2.0347
                                     0.8112
                                              2.508 0.012140 *
factor(bypared)2:lowinc -2.9955
                                     0.9298 -3.222 0.001278 **
factor(bypared)3:lowinc -4.0551
                                     1.0682 -3.796 0.000147 ***
factor(bypared)4:lowinc -4.8143
                                     1.1126
                                             -4.327 1.52e-05 ***
factor(bypared)5:lowinc -4.6890
                                     1.0947
                                             -4.283 1.85e-05 ***
factor(bypared)6:lowinc -4.5252
                                     1.0556 -4.287 1.82e-05 ***
factor(bypared)7:lowinc -7.2222
                                     1.3796 -5.235 1.67e-07 ***
factor(bypared)8:lowinc -9.8773
                                     1.6110 -6.131 8.94e-10 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 12.23 on 15219 degrees of freedom
  (924 observations deleted due to missingness)
Multiple R-squared: 0.1948,
                                Adjusted R-squared: 0.194
F-statistic: 230.2 on 16 and 15219 DF, p-value: < 2.2e-16
```

#### Polynomials

To add quadratic and other polynomial terms to the model, use the I() function, which lets you raise the term to the power you want in the regression using the caret (^) operator. In the model below, we add a quadratic version of the reading score to the right-hand side.

```
## add polynomials
fit <- lm(bynels2m ~ bynels2r + I(bynels2r^2), data = df)
summary(fit)</pre>
```

```
Call:
lm(formula = bynels2m \sim bynels2r + I(bynels2r^2), data = df)
Residuals:
   Min
            10 Median
                                   Max
-33.462 -5.947 -0.156
                         5.780 46.645
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
             12.7765815 0.6241194 20.471
(Intercept)
                                             <2e-16 ***
bynels2r
              1.1197116 0.0447500 25.021
                                             <2e-16 ***
I(bynels2r^2) -0.0006246 0.0007539 -0.828
                                              0.407
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 8.921 on 15881 degrees of freedom
  (276 observations deleted due to missingness)
Multiple R-squared: 0.5658,
                               Adjusted R-squared: 0.5657
F-statistic: 1.035e+04 on 2 and 15881 DF, p-value: < 2.2e-16
```

Quick exercise Fit a linear model with both interactions and a polynomial term. Then look at the model matrix to see what R did under the hood.

# Generalized linear model

To fit a model with binary outcomes, switch to the glm() function. It is set up just like lm(), but it has an extra argument, family. Set the argument to binomial() when your dependent variable is binary. By default, the link function is a logit link.

```
fit <- glm(plan_col_grad ~ bynels2m + as_factor(bypared),</pre>
           data = df
           family = binomial())
summary(fit)
Call:
glm(formula = plan_col_grad ~ bynels2m + as_factor(bypared),
    family = binomial(), data = df)
Deviance Residuals:
   Min
             10
                  Median
                                30
                                        Max
                   0.5211
-2.6467 -0.9581
                            0.7695
                                     1.5815
Coefficients:
                           Estimate Std. Error z value Pr(>|z|)
(Intercept)
                          -1.824413
                                      0.090000 -20.271 < 2e-16 ***
bynels2m
                           0.056427
                                      0.001636 34.491 < 2e-16 ***
as_factor(bypared)hsged
                           0.042315
                                      0.079973
                                                 0.529
                                                         0.5967
as_factor(bypared)att2yr
                           0.204831
                                      0.088837
                                                 2.306
                                                         0.0211 *
as_factor(bypared)grad2ry 0.480828
                                      0.092110
                                                 5.220 1.79e-07 ***
as_factor(bypared)att4yr
                                      0.090558
                                                 5.511 3.58e-08 ***
```

0.499019

```
as factor(bypared)grad4yr 0.754817
                                     0.084271 8.957 < 2e-16 ***
as_factor(bypared)ma
                          0.943558
                                     0.101585 9.288 < 2e-16 ***
as_factor(bypared)phprof
                          1.052006
                                     0.121849 8.634 < 2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 17545 on 15235 degrees of freedom
Residual deviance: 15371 on 15227 degrees of freedom
  (924 observations deleted due to missingness)
AIC: 15389
Number of Fisher Scoring iterations: 4
If you want a probit model, just change the link to probit.
## probit
fit <- glm(plan_col_grad ~ bynels2m + as_factor(bypared),</pre>
          data = df,
           family = binomial(link = "probit"))
summary(fit)
Call:
glm(formula = plan_col_grad ~ bynels2m + as_factor(bypared),
   family = binomial(link = "probit"), data = df)
Deviance Residuals:
             1Q Median
   Min
                               30
                                       Max
                  0.5238
                          0.7812
-2.7665 -0.9796
                                    1.5517
Coefficients:
                           Estimate Std. Error z value Pr(>|z|)
(Intercept)
                         -1.0522131 0.0539072 -19.519 < 2e-16 ***
                          0.0326902 0.0009357 34.938 < 2e-16 ***
bynels2m
as_factor(bypared)hsged
                          0.0325415 0.0488225
                                                0.667
                                                       0.5051
as_factor(bypared)att2yr
                          0.1316456 0.0539301
                                                 2.441 0.0146 *
                                                5.340 9.31e-08 ***
as_factor(bypared)grad2ry 0.2958810 0.0554114
as_factor(bypared)att4yr
                          0.3065176 0.0544813
                                                 5.626 1.84e-08 ***
as_factor(bypared)grad4yr 0.4553127 0.0505009
                                                9.016 < 2e-16 ***
as factor(bypared)ma
                          0.5525198 0.0588352
                                                 9.391 < 2e-16 ***
                                                8.878 < 2e-16 ***
as_factor(bypared)phprof
                          0.6115358 0.0688820
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 17545 on 15235 degrees of freedom
Residual deviance: 15379 on 15227 degrees of freedom
  (924 observations deleted due to missingness)
AIC: 15397
Number of Fisher Scoring iterations: 4
```

Quick exercise Fit a logit or probit model to another binary outcome.

# Using survey weights

So far we haven't used survey weights, but they are very important when using survey data. To use survey weights, you'll need to use the survey package (which we've already loaded above)

To use survey weights, you need to set the survey design using the <code>svydesign()</code> function. You could do this in the <code>svyglm()</code> function we'll use to actually estimate the equation, but it's easier and clearer to do it first, store it in an object, and then use that object in the <code>syvglm()</code>.

ELS has a complex sampling design that we won't get into, but the appropriate columns from our data frame, df, are set to the proper arguments in svydesign():

- ids are the primary sampling units or psus
- strata are indicated by the strat\_ids
- weight is the base-year student weight or bystuwt
- data is our data frame object, df
- nest = TRUE because the psus are nested in strat\_ids

Finally, notice the  $\sim$  before each column name, which is necessary in this function.

Now that we've set the survey design, let's compare the unweighted mean with one that accounts for the survey design;

We can also use the survey package to properly weight our t-tests and regression models — again, using the object svy\_df in the design argument in place of our unset df data frame.

```
data: bynels2m ~ moth_ba
```

```
t = 23.747, df = 389, p-value < 2.2e-16
alternative hypothesis: true difference in mean is not equal to \ensuremath{\text{0}}
95 percent confidence interval:
7.881366 9.299402
sample estimates:
difference in mean
           8.590384
```

```
QUICK EXERCISE Compare this to the output from t.test() above.
## fit the svyglm regression and show output
svyfit <- svyglm(bynels2m ~ byses1 + female + moth_ba + fath_ba + lowinc,</pre>
                design = svy_df)
summary(svyfit)
Call:
svyglm(formula = bynels2m ~ byses1 + female + moth ba + fath ba +
   lowinc, design = svy_df)
Survey design:
svydesign(ids = ~psu, strata = ~strat_id, weight = ~bystuwt,
   data = df, nest = TRUE)
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 45.2221 0.2710 166.867 < 2e-16 ***
             6.9470
                        0.2913 23.849 < 2e-16 ***
byses1
female
            -1.0715
                        0.2441 -4.389 1.47e-05 ***
moth_ba
             0.6633
                        0.3668 1.809 0.0713.
fath_ba
             0.5670
                        0.3798
                                1.493 0.1363
lowinc
            -2.4860
                        0.3644 -6.822 3.49e-11 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for gaussian family taken to be 159.713)
```

Number of Fisher Scoring iterations: 2

Note that the survey library has a ton of features and is worth diving into if you regularly work with survey data.

#### **Predictions**

Being able to generate predictions from new data can be a powerful tool. Above, we were able to return the predicted values from the fit object. We can also use the predict() function to return the standard error of the prediction in addition to the predicted values for new observations.

First, we'll get predicted values using the original data along with their standard errors.

```
## predict from first model
fit <- lm(bynels2m ~ byses1 + female + moth_ba + fath_ba + lowinc,</pre>
          data = df
## old data
fit_pred <- predict(fit, se.fit = TRUE)</pre>
```

[1] 0.1755431 0.2587681 0.2314676 0.2396327 0.2737971 0.2721818

#### Predictions with new data

Ideally, we would have a new observations with which to make predictions. Then we could test our modeling choices by seeing how well they predicted the outcomes of the new observations.

With discrete outcomes (like binary 0/1 data), for example, we could use our model and right-hand side variables from new observations to predict whether the new observation should have a 0 or 1 outcome. Then we could compare those predictions to the actual observed outcomes by making a 2 by 2 confusion matrix that counted the numbers of true positives and negatives (correct predictions) and false positives and negatives (incorrect predictions).

With continuous outcomes, we could follow the same procedure as above, but rather than using a confusion matrix, instead assess our model performance by measuring the error between our predictions and the observed outcomes. Depending on our problem and model, we might care about minimizing the root mean square error, the mean absolute error, or some other metric of the error.

#### Predictions using training and testing data

In the absence of new data, we instead could have separated our data into two data sets, a training set and test set. After fitting our model to the training data, we could have tested it by following either above procedure with the testing data (depending on the outcome type). Setting a rule for ourselves, we could evaluate how well we did, that is, how well our training data model classified test data outcomes, and perhaps decide to adjust our modeling assumptions.

### Margins

Using the predict() function alongside some other skills we have practiced, we can also make predictions on the margin a la Stata's -margins- suite of commands.

For example, after fitting our multiple regression, we might ask ourselves, what is the marginal "effect" of having a low family income on math scores, holding all other terms in our model constant?

To answer this question, we first need to make a "new" data frame with a column each for the variables used in the model and rows that equal the number of predictive margins that we want to create. In our example, that means making a data frame with two rows and five columns.

With lowinc, the variable that we want to make marginal predictions for, we have two potential values: 0 and 1. This is the reason our "new" data frame has two rows. If lowinc took on four values, for example, then our "new" data frame would have four rows, one for each potential value. But since we have two, lowinc in our "new" data frame will equal 0 in one row and 1 in the other row.

All other columns in the "new" data frame should have consistent values down their rows. Often, each column's repeated value is the variable's average in the data. Though we could use the original data frame (df) to generate these averages, the resulting values may summarize different data from what was used to fit the model if there were observations that lm() dropped due to missing values. That happened with our

model. We could try to use the original data frame and account for dropped observations, but I think it's easier to use the design matrix that's retrieved from model.matrix().

The code below goes step-by-step to make the "new" data frame.

```
## create new data that has two rows, with averages and one marginal change
## (1) save model matrix
mm <- model.matrix(fit)</pre>
head(mm)
  (Intercept) byses1 female moth_ba fath_ba lowinc
1
            1 - 0.25
                           1
2
            1
                0.58
                           1
                                    0
                                            0
                                                    0
3
            1
              -0.85
                                    0
                                                    0
4
            1 -0.80
                           1
                                    0
                                            0
                                                    1
5
            1
               -1.41
                           1
                                    0
                                                    1
6
            1 -1.07
                           0
                                    0
                                            0
                                                    0
## (2) drop intercept column of ones (predict() doesn't need them)
mm \leftarrow mm[,-1]
head(mm)
  byses1 female moth_ba fath_ba lowinc
1 - 0.25
              1
                       0
    0.58
                                       0
2
              1
                       0
                                0
3 -0.85
              1
                                       0
4 -0.80
                       0
              1
                                       1
5
  -1.41
              1
                       0
                                       1
6 -1.07
                       a
## (3) convert to data frame so we can use $ notation in next step
mm <- as.data.frame(mm)</pre>
## (4) new data frame of means where only lowinc changes
new_df <- data.frame(byses1 = mean(mm$byses1),</pre>
                      female = mean(mm$female),
                      moth_ba = mean(mm$moth_ba),
                      fath_ba = mean(mm$fath_ba),
                      lowinc = c(0,1))
## see new data
new df
                          moth_ba
                                     fath_ba lowinc
      byses1
                 female
```

```
byses1 female moth_ba fath_ba lowinc
1 0.04210423 0.5027566 0.2743502 0.3195064 0
2 0.04210423 0.5027566 0.2743502 0.3195064 1
```

Notice how the new data frame has the same terms that were used in the original model, but has only two rows. In the lowinc column, the values switch from 0 to 1. All the other rows are averages of the data used to fit the model.

To generate the prediction, we use the same function call as before, but use our new\_df object with the newdata argument.

```
## predict margins
predict(fit, newdata = new_df, se.fit = TRUE)
```

\$fit

1 2 45.82426 43.68173

\$se.fit

1 2

0.1166453 0.2535000

\$df

[1] 15230

\$residual.scale

[1] 12.24278

Our results show that compared to otherwise similar students, those with a family income less than \$25,000 a year are predicted to score about two points lower on their math test.

In this example, we held the other covariates at their means. We could have chosen other values (e.g. fath\_ba == 1 or female == 1), however, meaning that we could use the same procedure to produce predictions for low-income status (or other model covariates) across a range of margins.