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Summary Sheet

Managing The Zambezi River

Summary

Here is the abstract to be written!

Keywords: keyword1; keyword2

Managing The Zambezi River

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1 Introduction

The Kariba Dam is one of the biggest dam in the world, which is constructed on the Zambezi River. It supplies 1626 megawatts of electricity to parts of both Zambia and Zimbabwe and

2 Model A: Search for possible reaches to build dams

2.1 Description

To build new dams, we need to find a serial of possible reaches at first. In accordance with the norms, the choice of reaches should take geology, terrain, economic, ecology, disaster and so forth factors into consideration. However, the major determinant of a dams to be of valuable worthy is terrain.

2.2 Analysis

To be specific, we get two principle of searching for possible reaches to build dams:

1. The higher the throw is, the more abundant hydropower resources is contained;
2. In consideration of reducing ecological effects as much as possible and reducing the evaporation loss f water, the surface area of artificial reservoirs should be small under certain requirement of volume. To build reservoir with small surface area and certain volume, the average depth of reservoir should be deep, thus, dams should be built between deep ravines

Hydropower station convert gravitational potential energy of water into electrical energy. The gravitational potential energy is calculated as $E_p = mgh$, thus, higher throw implies bigger electricity-generation capacity.

To simplify model, we assume that the vertical section of a reservoir is a approximate trapezoid, then the submerged area can be expressed as below:

$$\int_A^B \frac{H(l)}{\sin[\alpha(l)]} dl + \int_C^D \frac{H(L)}{\sin[\alpha(L)]} dL + S_{bottom} \quad (1)$$

where l, L are the lengths of left bank and right bank respective; A, B indicate the start-ing position and end position of l ; similarly, C, D indicate the starting position and end position of L . The expression (1) is still hard to deal, because of the difficulty of the estimation of α . In order to make our assessment feasible, we need to simplify the expression

(1). Noticed that:

$$\int_A^B \frac{H(l)}{\sin[\alpha(l)]} dl = \frac{1}{\sin[\alpha(\zeta)]} \int_A^B H(l) dl = KH_{average}l \quad (2)$$

where K is a coefficient of inclination. expressions (2) is a application of mean value theorem for integrals, it fits in with the physics intuition. Then, the submerged area can be estimated as:

$$(K_1l + K_2L)H_{average} + S_{bottom} \quad (3)$$

Using expression (3), we can qualitatively explain why small surface area is desired. Using equation $H_{average} = \frac{V}{S}$, we get:

$$S_{submerged} \approx (K_1l + K_2L) \frac{V}{S} + S_{bottom}$$

and using the assumption of vertical section, the area of the bottom of a reservoir can be estimated as:

$$S_{bottom} = \int (\beta dS) \propto S \quad (4)$$

where β is a coefficient of position and water factors, the expression (4) qualitatively explain that S_{bottom} is proportional to S , thus we get:

$$S_{submerged} \approx (K_1l + K_2L) \frac{V}{S} + CS \quad (5)$$

where C is a coefficient to indicate that S_{bottom} is proportional to S . Since the right side of the expression (5) is a hyperbolic function and it monotonically decrease when $S \geq \sqrt{\frac{(K_1l + K_2L)V}{C}}$. In the actual situation, $S \gg \sqrt{V}$, so we can qualitatively conclude that under certain requirement of volume small surface area of reservoir is more beneficial than the bigger surface area.

According to the above discussion, we should find the reaches with big throws on the Zambezi river based on the first principle. In accordance with the second principle, the possible reaches should between deep ravines, because a reservoir in deep ravines can have deeper water depth and thus smaller surface area.

2.3 Model Building

In order to make the problem, finding suitable dam sites along the Zambezi River, clear, we established a simple model based on the geographical conditions. Relying on this model, we can find out some regions that are possible for the construction of dams. And, of course, other factors like construction costs and safety of dam system will be put into consideration in the following discussion.

To reduce the overall construction costs and maintain the original ecological appearance to the maximum extent, keep the ability to respond to emergencies including increasing water storage in prolonged low water conditions and attenuating flooding in the rainy season, the topography and inflow in the catchment becomes particular important in choosing candidate dam locations.

The reservoir storage of dams generally depend on the fall of water level (influence the height of dams), slope and height of the river bank (determine the reservoir area). The cost of construction basically depends on the dam's height and length, which can be quantified by the width of river.

Thus, there are three major parameter to be taken into account in choosing candidate regions:

- Fall of water level.
- Slope and height of the river bank.
- Width of river.

Apparently, a higher fall of water level means a greater power of the water and a larger volume of water available for storage. Therefore, the water level are required to experience a noticeable fall in the candidate dam site regions.

««««< HEAD We download the geomorphological remote sensing information data of the Zambezi River Basin and generate a Digital Elevation Model (DEM). The Figure 1 is a general overview of the elevation in that region (the Zambezi River is marked red in the chart). =====

3 Model A : Search for possible location to build dams

4 Select Candidate Dam Site Regions

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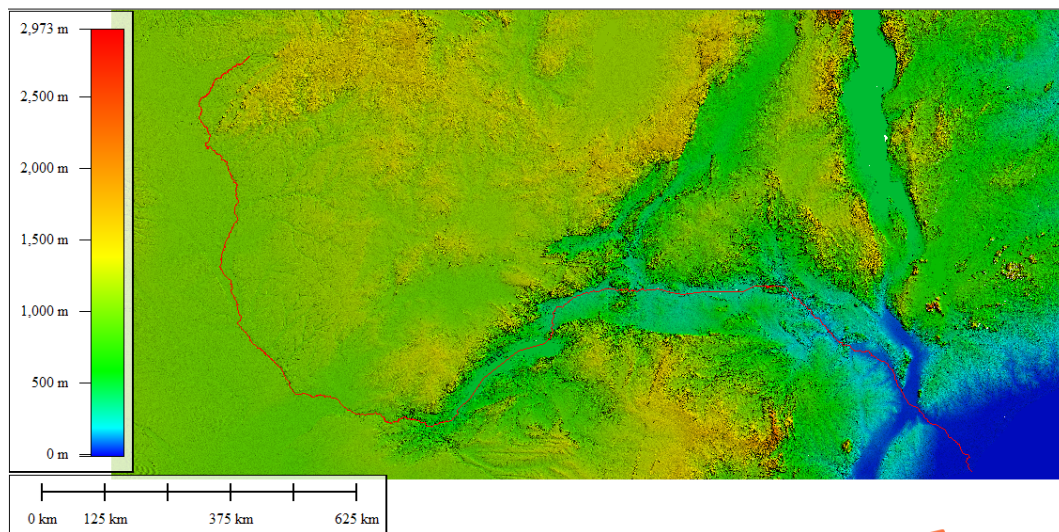


Figure 1: Overview Elevation Chart

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(6)

According to the DEM, we obtain the elevation along the whole Zambezi River. From the Figure 2, the origin of the

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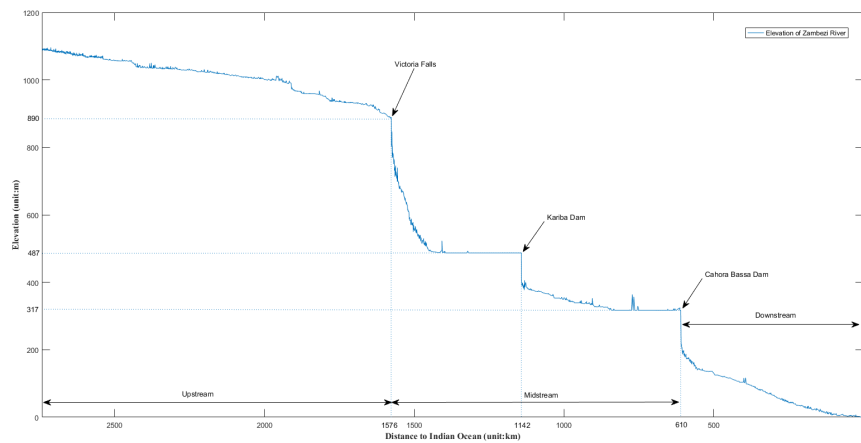


Figure 2: Elevation along the Zambezi River

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(7)

$$a^2$$

(7)

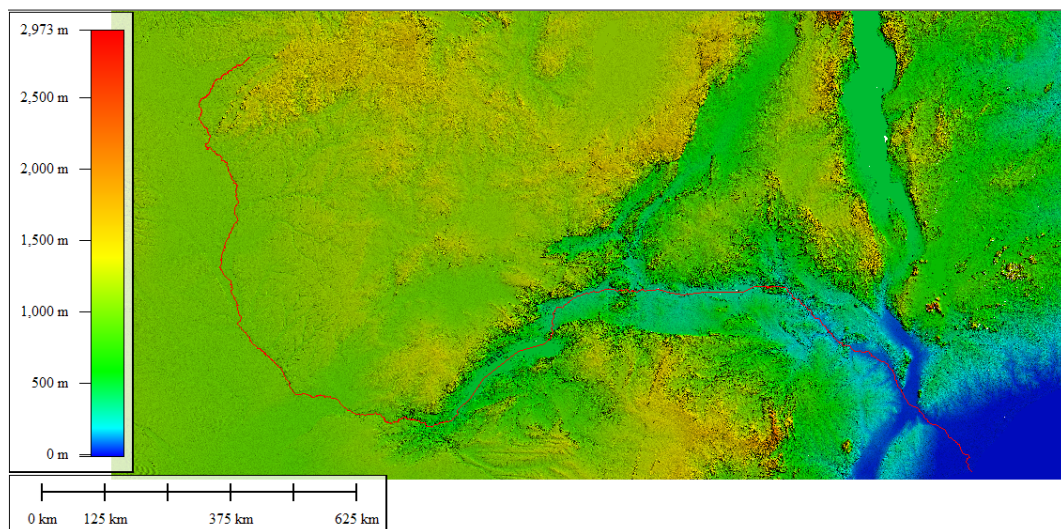


Figure 3: Overview Elevation Chart

According to the DEM, we obtain the elevation along the whole Zambezi River. From the Figure 2, the river can be divided into three sections, of which the source goes to the Victoria Falls for the upper reaches, the Victoria Falls to the Cahora Bassa Dam for the middle reaches and the Cahora Bassa Dam to the end for the downstream.

There is a clear trend that the upstream is smooth and have small water level drop, the water level decreases remarkably in the midstream and shoulders the most responsibility of storing water, the downstream have a rapid change of water level as well but there

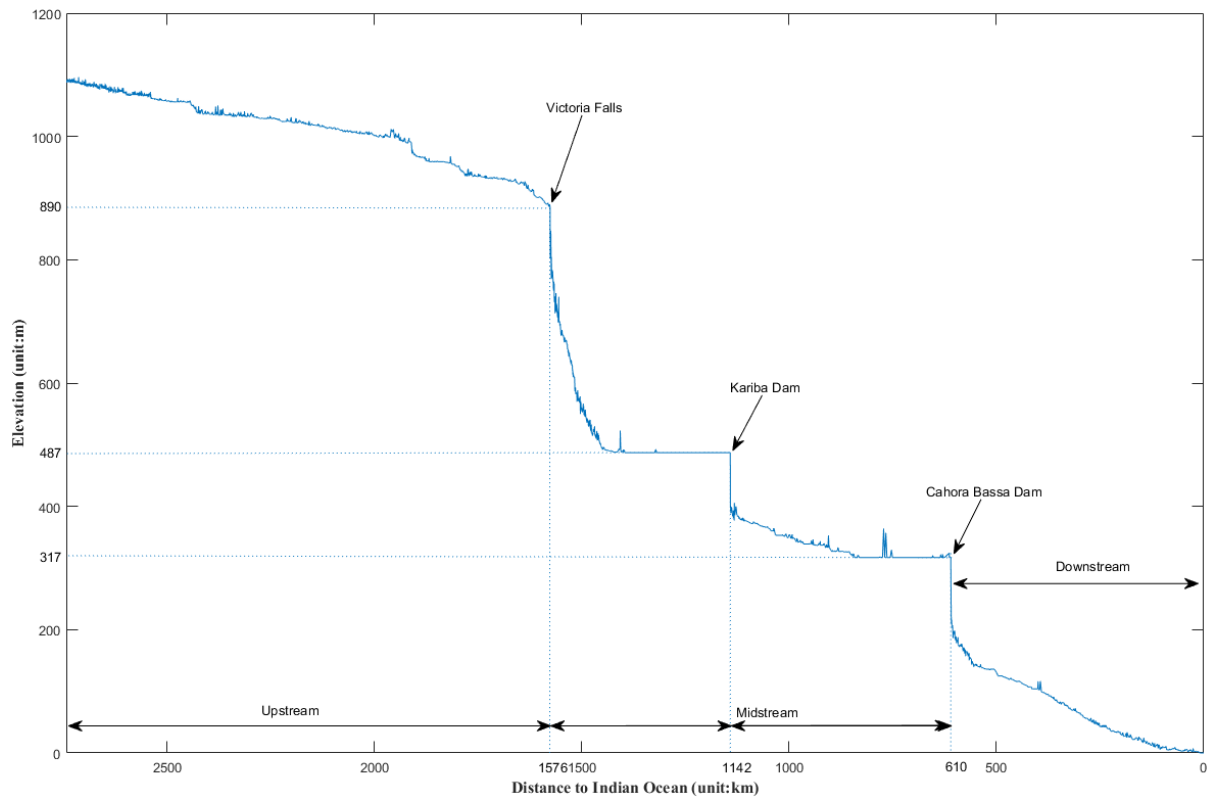


Figure 4: Elevation along the Zambezi River

are few dams. Three prominent falls in the water level occur in the Victoria Falls, the Kariba Dam and the Cahora Bassa Dam.

4.1 Model Validation

4.2 Result

According to Model A, We get some important equations as follow.

Meanwhile, based on the model, we make the following suggestions.

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5 Model B : The Best Arrangement

5.1 Description

5.2 Analysis and Assumptions

5.3 Model Building

5.4 Optimization

5.5 Sensitivity Analysis

5.6 Model Validation

5.7 Result

6 Strengths and weaknesses

6.1 Model A: Search for possible reaches to build dams

Model A has the following weaknesses.

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Despite of the weakness, it has more strengths.

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6.2 Model B: The Best Arrangement

In Model B, we consider , which is a weakness. However we have more strengths as below:

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7 Conclusion

Here is the conclusion to be done!

References

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- [2] Lamport, Leslie, \LaTeX : “ A Document Preparation System ”, Addison-Wesley Publishing Company, 1986.
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8 Brief Assessment of the options

The solution to the Kariba Dam problem can simply be divided into three options: repairing it, rebuilding it or removing it then replacing it with other dams. To the third method, ZRA suggests to build 10 ~ 20 small dams to replace the huge Kariba Dam.

Evaluating the options from the perspective of cost and benefit is a complex task, since it can be influenced by a number of factors. Only considering the cost of building dams, although it can be estimated accurately by using the cost formula below

$$C_p = K \left(\frac{V}{\left(\frac{H}{0.3}\right)^{0.3}} \right)^{0.82}$$

where C_p is the cost of building the hydropower station, V is the installed capacity, H is the design head, K is the proportional coefficient. However, the ecological costs of dam construction need to be considered more cautiously because damage to the ecological environment may be irreversible.

Option 1. Repairing the existing Kariba Dam. This is the option with the lowest cost of construction. Meanwhile, it won't change the submerged area, so there is no extra ecological cost. From the aspect of revenue, the reconstruction and expansion of Kariba Dam hydropower station can be carried out at the same time, which can effectively increase the total installed capacity of hydropower station, and thus improve the income of hydropower station. In fact, the expansion of the Kariba Dam hydropower station is underway. Since the reconstruction will not affect the Kariba Lake, the benefits from the use of water from the lake won't be reduced. The analysis above is based on the assumption that the climate will not change drastically in the future and no rare disasters which is outside the historical statistics will occur.

Option 2. Rebuilding the existing Kariba Dam. Because rebuilding the Kariba Dam need to remove the existing the dam and rebuild it at the origin site, it is an option with high risk and cost. What's more, the reconstruction of the dam will inevitably lead to the result that the hydropower station can't generate electricity in quite a long period, so this part of loss should also be included in the cost of reconstruction. However, rebuilding dams do have benefits. It helps to expand the installed capacity of hydropower station (benefit from re-designing the internal structure and using more advanced equipment). The new designed Dam would have better flood protection capacity, which allows river management to handle emergency with more flexibility. Stronger water storage capacity means we can raise the water level of Kariba Lake. It will increase the energy generation as well as bring the risk of ecologic damage which needs to be treated with caution.

Option 3. Removing the Kariba Dam and replacing it with a series of 10 ~ 20 smaller dams along the Zambezi River. This is quite an ambitious plan. Even if the sum of installed capacity of all these small dams is the same as that of Kariba Dam, the total construction cost is still expected to be higher than rebuilding Kariba Dam according to the cost formula above. With the same problem as option 2, removing Kariba Dam will definitely lead to the loss of energy generation, furthermore even the construction of a smaller dam in the original position of Kariba Dam may result in loss of water storage capacity, as the water level in Kariba Lake will decrease. Fortunately, these losses can be minimized through rational planning. Specifically, we can give priority to the con-

struction of small dams, and then gradually replace the Kariba Dam with their power generation capacity. New dams built in the down stream would store the water from Kariba Dam when it is removed, which can reduce the loss of water resources. Different from the previous two options, economic compensation of the new reservoirs' reserved area also needs to be include in the cost.(Here we can make an estimate by calculating the unit area GDP of the catchment)From the ecological point of view, the third option is also accompanied by greater risk. It will not only flood new areas, but also affect the ecology of Lake Kariba (the water level drops and the lake is divided into several parts). In terms of revenue, the scheduling of water resources between dams will reduce the loss of water resources caused by flooding discharge, which will actually help to increase the power generation capacity of hydropower stations. Moreover, the rational allocation of flood storage between dams will increase the safety of the dam system, the reduced reservoir area will reduce the evaporation loss of water and, in the face of emergencies, river management can also adopt a more flexible approach. Because of the high cost of the third option, a long-term analysis is of great significance. In the future, the flow of Zambezi River may reduce by 40% ~ 50% due to the climate change. Although the climate predictions nowadays are with a large degree of uncertainty, but we should never be blindly optimistic about the benefits of the new dam system.