TopoAna: A generic tool for the topology analysis of inclusive Monte-Carlo samples in high energy physics experiments

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Abstract

Inclusive Monte-Carlo samples are indispensable for signal selection and background suppression in many high energy physics experiments. A clear knowledge of the topology of the samples, including the categories of physics processes and the number of processes in each category, is a great help to investigating signals and backgrounds. To help analysts obtain the topology knowledge from the truth information of the samples, we develop a topology analysis program, TopoAna, with C++, ROOT, and LaTeX. The program implements the functionalities of component analysis and signal identification by recognizing, categorizing, counting, and tagging events. Independent of specific software frameworks, the program is applicable to many experiments. At present, it has come into use in three e^+e^- colliding experiments: the BESIII, Belle, and Belle II experiments. The use of the program in other experiments is also prospective.

Keywords:
event topology; component analysis; signal identification; inclusive Monte-Carlo samples; high energy physics experiments

1. Introduction

One of the most important tasks in the data analysis of high energy physics experiments is to select signals, or in other words, to suppress backgrounds. As for the task, inclusive/generic Monte-Carlo (MC) samples are extremely useful, in that they provide basic, though not perfect, descriptions of the signals and/or backgrounds involved. However, due to the similarities between signals and some backgrounds, it usually takes efforts to establish a set of selection criteria that retain a high signal efficiency and meanwhile keep a low background level. Further optimization of preliminary criteria is often needed in the process. Under the circumstances, a comprehensive understanding of the samples is required. In particular, a clear knowledge of the

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The program is now available at https://github.com/buaazhouxingyu/topoana.

topology of the samples is quite helpful. To be specific, the topology information includes the categories of physics processes and the number of processes in each category, involved both in the entire samples and in the individual events. Here, the physics process could be a complete production and decay process involved in an event, or merely a part of it, such as the decay of an intermediate resonance. With the information, one can figure out the main backgrounds (especially the peaking ones), and optimize the selection criteria further by analyzing the differences between the main backgrounds and the signals. Even if it is difficult to further suppress these backgrounds, the knowledge of their topology is beneficial to estimate the systematic uncertainties associated with them.

The analysis of the topology information described above is a sort of component analysis, or in technical words, cluster analysis. It is complex since it has to classify physics processes actively and finely. Another sort of topology analysis often required in practice is signal identification, which only aims to search for certain processes of interests. It is relatively simple because its core technique is merely pattern matching. Mostly, signal and background events coexist in the inclusive MC samples. It is meaningful to differentiate them in such cases. The identified signal events can be used to make up a signal sample (removed to avoid repetition) in the absence (presence) of specialized signal MC sample. Occasionally, we have to pick out some decay branches in order to re-weight them according to new theoretical predictions or updated experimental measurements. Signal identification also plays a part in this occasion.

However, since the raw topology truth information of inclusive MC samples is counter-intuitive, diverse, and overwhelming, it is difficult for analysts to check the topology of the samples directly. To help them obtain the information quickly and easily, a topology analysis program called TopoAna is developed with C++, ROOT [1], and LaTeX. Here, C++ is the programming language, ROOT is the C++ based data analysis software universally used in high energy physics experiments, and LaTeX is used for generating pdf documents containing the topology information. The program implements the functionalities of component analysis and signal identification by recognizing, categorizing, counting, and tagging events accurately, and exports the obtained topology information to plain text, tex source, pdf, and root (TFile [2]) files clearly. Here, accurate pattern recognition is the foundation of developing these functionalities. To meet a variety of practical requirements, many kinds of fine, customizable clustering and matching algorithms are implemented in the program.

The program is applicable to inclusive MC samples at any data analysis stage of high energy physics experiments. In the overwhelming majority of situations, it is run over the samples which have undergone some selections, in order to examine the signals and backgrounds in the selected samples as well as the effect of the imposed selections. In such situations, the results of topology analysis are usually used together with other quantities for physics analysis. In spite of this, applying the program to the samples without undergoing any selection facilitates us to validate the generators and decay cards that produce the samples and helps novices get familiar with the topology of the samples.

Not relying on any specific software frameworks, the program applies to many high energy physics experiments. At first, the program was developed for the BESIII experiment, an experiment in the τ-Charm energy region with abundant research topics under study [3, 4]. Then, it was extended substantially for the Belle II experiment, which is primarily dedicated to search for physics beyond the Standard Model in the flavor sector and has already started data taking in the recent two years [5]. Besides, the program has also been tried and used in the Belle experiment, the predecessor of the Belle II experiment, where some physics studies are still ongoing [6].

This user guide aims to give a detailed description of TopoAna, without involving the technicalities of implementing the program. Its structure is organized as follows: Section 2 introduces the basics of the program; Sections 3 and 4 expatiate the two sorts of functionalities of the program — component analysis and signal identification, respectively; Sections 5 and 6 present some common settings and auxiliary facilities for the executing of the program, respectively; Section 7 summarizes the user guide. It is worth mentioning here that, aside from the detailed description in the user guide, an essential description of the program can be found in the file "paper_draft_v*.pdf" under the directory "share" of the package.

2. Basics of the program

This section introduces the basics of the program, including the package, input, execution, and output of the program. The package implements the program via a C++ class called "topoana" and a main function invoking the class. Compiling the package creates the executable file of the program, that is, "topoana.exe". To execute the program, we have to first obtain the input data of the program, namely the raw topology truth information of the inclusive MC samples, with some interfaces to the program in the software systems of the corresponding experiments. Normally, the input data contain all the topology information of the samples. With the data, all sorts of the topology analysis presented in the user guide can be performed.

To carry out the topology analysis desired in our work, we have to provide some necessary input, functionality, and output information to the program. The information is required to be filled in the setting items designed and implemented in the program, and the items have to be put in a plain text file named with a suffix ".card". With the card file, one can execute the program with the command line: "topoana.exe cardFileName", where the argument "cardFileName" is optional and its default value is "topoana.card". After the execution of the program, we can examine the results of topology analysis in the output files and use them to analyze other experimental quantities. The results help us gain a better understanding of the signals and backgrounds and are conducive to carrying our work forward. In the next four subsections, we will present the package, input, execution, and output of the program in detail, with each part in one subsection.

2.1. *Package of the program*

The package consists of six directories — "include", "src", "bin", "share", "examples", and "utilities" — and five files — "LICENSE", "README.md", "Configure", "Makefile", and "Setup". While the directory "include" only includes one header file "topoana.h", the directory "src" contains sixty source files "*.cpp" as well as a script file "topoana.C". At present, only one class, namely "topoana", is defined in the program for all of its functionalities. The class is declared in "topoana.h", implemented in "*.cpp" files, and invoked in "topoana.C".

The file "template_topoana.card" under the directory "share" saves all the items which are developed to set user specified information for the execution of the program. One can refer to the file when filling in the cards for their own needs. Some plain text files "pid_3pchrg_txtpnm_texpnm_iccp.dat_*" are also included in the directory "share". They store the basic information of the particles used in the program. The suffixes of their names indicate the experiments they apply to. One of them will be copied to "pid_3pchrg_txtpnm_texpnm_iccp.dat" when we set up the program. Besides, the directory "share" also contains three LaTeX style files " geometry.sty", "ifxetex.sty", and "makecell.sty", which are invoked by the program for generating pdf files. The directory "examples" includes plenty of detailed examples. Particularly, all the examples involved in this user guide are under its sub-directory "in_the_user_guide". The directory "utilities" contains some useful bash scripts.

The program is released under MIT license [7]. The file “README.md” briefly introduces how to install and use the program. To set up the program, one should first set the package path with the command “./Configure”. Output of the command are the guidelines for manually adding the absolute path of “topoana.exe” to the environment variable “PATH”, in order to execute it without any path. The second step is executing the command “make”. This command compiles the header, source, and script files into the executable file “topoana.exe” under the directory “bin”, according to the rules specified in the “Makefile”. The last step is specifying the experiment name with the command line “./Setup experimentName”. Currently, the supported experiment names are “BESIII”, “Belle”, and “Belle_II”. Besides, “./Setup Example” is required for the execution of the examples in the user guide.

2.2. Input of the program

The input of the program is one or more root files including a TTree [8] object which contains raw topology truth information of the inclusive MC samples under study. To be specific, the information in each entry of the TTree object consists of the following three ingredients associated with the particles produced in an event of the samples: the number of particles, PDG [9] codes of particles, and mother indices of particles. Notably, the particles do not include the initial state particles (e^+ and e^- in e^+e^- colliding experiments), which are default and thus omitted. Besides, the indices of particles are integers starting from zero (included) to the number of particles (excluded); they are obvious and hence not taken as an input ingredient for topology analysis. Equation (1) shows an example of the input data.

$$
\begin{array}{lcl}
\text{Number of particles} & : & 63 \\
\text{PDG codes of particles} & : & 300553, \\
 & & -511, 511, -433, 421, 211, 22, -413, 111, 111, 113, \\
 & & 211, -431, 22, -323, 213, -421, -211, 22, 22, 22, \\
 & & 22, 211, -211, 333, 11, -12, 22, -311, -211, 211, \\
 & & 111, 221, 331, 321, -321, 310, 22, 22, 111, 111, \\
 & & 111, 111, 111, 221, 111, 111, 22, 22, 22, 22, \\
 & & 22, 22, 22, 22, 22, 22, 22, 22, 22, 22, \\
 & & 22, 22 \\
\text{Mother indices of particles} & : & -1, \\
 & & 0, 0, 1, 1, 1, 1, 2, 2, 2, 2, \\
 & & 2, 3, 3, 4, 4, 7, 7, 8, 8, 9, \\
 & & 9, 10, 10, 12, 12, 12, 12, 14, 14, 15, \\
 & & 15, 16, 16, 24, 24, 28, 31, 31, 32, 32, \\
 & & 32, 33, 33, 33, 36, 36, 39, 39, 40, 40, \\
 & & 41, 41, 42, 42, 43, 43, 44, 44, 45, 45, \\
 & & 46, 46
\end{array} \tag{1}
$$

The complete physics process contained in the data is displayed as follows.

$$
\begin{array}{clc@{\qquad}clc}
0 & e^+e^- \to \Upsilon(4S) & \text{-1} & 9 & \rho^+ \to \pi^0\pi^+ & 6 \\
1 & \Upsilon(4S) \to B^0\bar{B}^0 & 0 & 10 & K^{*-} \to \pi^-\bar{K}^0 & 6 \\
2 & B^0 \to \pi^0\pi^0\rho^0\pi^+D^{*-} & 1 & 11 & D_s^- \to e^-\bar{\nu}_e\phi\gamma & 7 \\
3 & \bar{B}^0 \to \pi^+D^0D_s^{*-}\gamma & 1 & 12 & \eta \to \pi^0\pi^0\pi^0 & 8 \\
4 & \rho^0 \to \pi^+\pi^- & 2 & 13 & \eta' \to \pi^0\pi^0\eta & 8 \\
5 & D^{*-} \to \pi^-\bar{D}^0 & 2 & 14 & \bar{K}^0 \to K_S^0 & 10 \\
6 & D^0 \to \rho^+K^{*-} & 3 & 15 & \phi \to K^+K^- & 11 \\
7 & D_s^{*-} \to D_s^-\gamma & 3 & 16 & \eta \to \gamma\gamma & 13 \\
8 & \bar{D}^0 \to \eta\eta' & 5 & 17 & K_S^0 \to \pi^0\pi^0 & 14
\end{array} \tag{2}
$$

Here, the decay branches in the process are placed into two blocks in order to make full use of the page space. In both blocks, the first, second, and third columns are the indices, textual expressions, and mother indices of the decay branches. Notably, all the decay branches of $\pi^0 \to \gamma\gamma$ are omitted in Eq. (2) in order to make the process look more concise. Since the topology diagram of such a process looks like a tree, we refer to the complete processes as decay trees. Obviously, the input data do not show the structure automatically. Thus, we need the program to do the topology analysis work.

From the first branch in Eq. (2), only one particle $\Upsilon(4S)$ is produced after the e^+e^- annihilation. Thus, $\Upsilon(4S)$ can be referred to as the root particle of the decay tree. Similarly, many other resonances with the quantum numbers $J^{PC} = 1^{--}$, such as J/ψ, can be solely produced at other proper energy points. Besides the cases with only one root particle, the program can deal with the cases with multiple root particles. For example, the program can recognize the following raw topology truth information

$$\begin{array}{lcl}
\text{Number of particles} & : & 25 \\
\text{PDG codes of particles} & : & 433, \\
 & & -321, 223, 211, -413, 431, 111, 211, -211, 111, -411, \\
 & & 111, 321, 113, 22, 22, 22, 22, 321, -211, -211, \\
 & & 22, 22, 211, -211 \\
\text{Mother indices of particles} & : & -1, \\
 & & -1, -1, -1, -1, 0, 0, 2, 2, 2, 4, \\
 & & 4, 5, 5, 6, 6, 9, 9, 10, 10, 10, \\
 & & 11, 11, 13, 13
\end{array} \tag{3}$$

as the following process

$$\begin{array}{clc@{\qquad}clc}
0 & e^+e^- \to \pi^+\omega K^- D^{*-} D_s^{*+} & -1 & 4 & D^- \to \pi^-\pi^- K^+ & 2 \\
1 & \omega \to \pi^0\pi^+\pi^- & 0 & 5 & D_s^+ \to \rho^0 K^+ & 3 \\
2 & D^{*-} \to \pi^0 D^- & 0 & 6 & \rho^0 \to \pi^+\pi^- & 5 \\
3 & D_s^{*+} \to \pi^0 D_s^+ & 0 & & &
\end{array} \tag{4}$$

Here, the particles $\pi^+\omega K^- D^{*-} D_s^{*+}$ in the first branch arise from hadronization processes, in which quark pairs produced from initial state particles turn into hadrons. The processes with hadronization ignored have a tree structure and thus are easy to resolve. On the other hand, some hadronization processes, particularly those in high energy regions, contain complicated loop structures that are hard to resolve without sophisticated algorithms. Resolving the hadronization processes is not involved in the program at present.

It is recommended to save the input data in the TTree object together with other quantities for physics analyses, in order to facilitate the examination of the distributions of the quantities with the topology information. The input data can be stored in several types. Normally, the number of particles can be simply stored in a TBranch [10] object as a scalar integer, while the PDG codes of particles, as well as the mother indices of particles, can be stored in a TBranch object as an array of integers, in a TBranch object as a vector of integers, or in a group of TBranch objects as multiple scalar integers. In the analysis software of the Belle II experiment, double-precision variables are used uniformly to store all the quantities involved in the experiment, and TBranch objects are not recommended to store arrays and vectors in order to use other tools such as NumPy [11] and pandas [12]. In such a situation, we have to store the number of particles in a TBranch object as a scalar double-precision number, and store the PDG codes of particles, as well as the mother indices of particles, in a group of TBranch objects as multiple scalar double-precision numbers. Summing up the above, we have mentioned four storage types of the input information. For the sake of simplification, we refer to them with the following acronyms: AOI, VOI, MSI, and MSD, which are short for array of integers, vector of integers, multiple scalar integers, and multiple scalar double-precision numbers, respectively. All of the storage types are supported by the program, and their acronyms will be used in the related item of the card file (see next subsection for details).

It is easy to get the input of the program within the software framework of high energy physics experiments. In order to facilitate its use, we have developed the interfaces of the program to the software systems of the BESIII, Belle, and Belle II experiments. Similar interfaces for other experiments can also be implemented with ease. Beyond the scope of the user guide, we will not discuss the details of the interfaces here.

Considering the diversity of the raw topology truth information, the program does not simply translate the counter-intuitive data into the intuitive processes. Here, the diversity means that a definite process can be represented with multiple permutations of the same set of data. For example, both the two permutations (113 –> 211, −211) and (113 –> −211, 211) stand for the decay branch $\rho^0 \to \pi^+\pi^-$. A decay tree can consist of many decay branches. As a consequence, the diversity issue is complex. To avoid the same set of data in different permutations are classified as different processes, the program first sorts the input data to adjust the possible permutations to a unique order, according to the PDG codes and charges of the involved particles, and the numbers of daughter particles in the case of identical particles present in the same decay branch. The sorting algorithm is implemented in the source file "sortPs.cpp", where some common settings are also involved. One can see the reference file "sortPs.cpp_core" for the core of the sorting algorithm. This is the foundation of accurate pattern recognition in the program.

2.3. Execution of the program

To execute the program, we have to first configure some necessary setting items in a card file, and then run the program with the command line: "topoana.exe cardFileName". This subsection introduces the essential items for the input, basic functionality, and output of the program. More items that can be set in the card file will be described in the following three sections. Sections 3 and 4 expatiate the available items for the functionalities of the program, and Section 5 presents the optional items for the common settings to control the execution of the program.

An example of the card file containing the essential items is shown as follows.

```
# The following six items set the input of the program.

% Names of input root files
{
   ../input/jpsi_1.root
   ../input/jpsi_2.root
}

% TTree name
{
   evt
}

% Storage type of input raw topology truth information (Four options: AOI, VOI, MSI, and MSD. Default: AOI)
{
   AOI
}

% TBranch name of the number of particles (Default: nMCGen)
```

```
{
   Nmcps
}

% TBranch name of the PDG codes of particles (Default: MCGenPDG)
{
   Pid
}

% TBranch name of the mother indices of particles (Default: MCGenMothIndex)
{
   Midx
}

# The following item sets the basic functionality of the program.

% Component analysis — decay trees
{
   Y
}

# The following item sets the output of the program.

% Main name of output files (Default: Main name of the card file)
{
   jpsi_ta
}
```

In the card file, “#”, “%”, and the pair of “{” and “}”, are used for commenting, prompting, and grouping, respectively. The first six, seventh, and last one items are set for the input, basic functionality, and output of the program, respectively.

The first item sets the names of the input root files. The names ought to be input one per line without tailing characters, such as comma, semicolon, and period. In the names, both the absolute and relative paths are allowed and wildcards “[]?*” are supported, just like those in the root file names input to the method Add() of the class TChain [13]. The second item specifies the TTree name. The third item tells the program the storage type of the input raw topology truth information, and the input should be one of the following four acronyms: AOI, VOI, MSI, and MSD, as we introduce in the previous subsection. The following three items set the TBranch names of the three ingredients of the input raw topology truth information. Of the first six items, the former two are indispensable, whereas the latter four can be removed or left empty if the input values are identical to the default values indicated in their prompts. Besides, the latter four items can be moved to the underlying card file, which is developed for frequently used items and will be introduced in Section 6.1, because the input values are usually fixed for a user or a group of users, though they might be different from the default values.

The seventh item sets the basic functionality of the program, namely the component analysis over decay trees. The item can be replaced or co-exist with other functionality items expatiated in Sections 3 and 4. Here, we note that at least one functionality item has to be specified explicitly in the card file, otherwise the program will terminate soon after its start because no topology analysis to be performed is set up.

The last item specifies the main name of the output files. Though in different formats, the files are denominated with the same main name for the sake of uniformity. They will be introduced at length in the next subsection. This item is also optional, with the main name of the card file as its default input value. It is a good practice to first denominate the card file with the desired main name of the output files and then remove this item or leave it empty.

To provide a complete description, we list and explain all the essential items in the paragraphs above. However, in practical uses, we suggest removing the optional items if the input values are identical to the default ones, or moving them to the underlying card file if the input values are fixed for most of your use cases. In this way, the contents of the card file will become much more concise, making the use of the program easier and quicker. For example, only the following two items are used to set the essential information in Sections 3, 4, and 5.

```
% Names of input root files
{
   ../input/mixed_1.root
   ../input/mixed_2.root
}

% TTree name
{
   evt
}
```

Besides, all the items in the program, also including those to be introduced in the following sections, are not required to be filled in the card files in a certain order. Nonetheless, we recommend filling them in a logical order for clearness.

During the execution of the program, some standard output and error messages are printed to the screen to provide some information on the input, progress, and output of the program, as well as the possible problems and proposed solutions to them. The standard output messages include the following four parts: (1) the values of the items with active inputs; (2) the total number of entries contained in the input root files and the progress of the program to process these entries; (3) the information output by the pdflatex command when it compiles the tex source file to get the pdf file; (4) and the hints on the output of the program. The standard error messages are prompted with "ERROR" and "INFOR" in order to differentiate themselves from the standard output massages. The messages started with "ERROR" point out the problems encountered by the program directly, while those started with "INFOR" give more information on the problems as well as some guidelines on the solutions to the problems.

The processing rate of the program is partly related to the performance of the detailed computing systems. Figure 1 shows the typical trends of the progress of the program, where the blue line displays the trend of running the example in this subsection. From the figure, the number of elapsed seconds grows linearly with the number of processed entries. This linear pattern, rather than a quadratic pattern, is a nice feature. It guarantees the program has a high rate even in the case of processing huge samples. In this example, the program is able to process one hundred thousand events within five seconds.

2.4. Output of the program

The program gains the topology information from input data, and saves it to output files. As mentioned in Section 1, the information includes the categories of physics processes and the number of processes in each category, involved both in entire samples and in individual events. We refer to the information at the sample level as topology maps. In the topology maps, we assign an integer to each category of physics processes as its index. We term the indices of processes as well as the numbers of processes involved in each category in the individual events as topology tags.

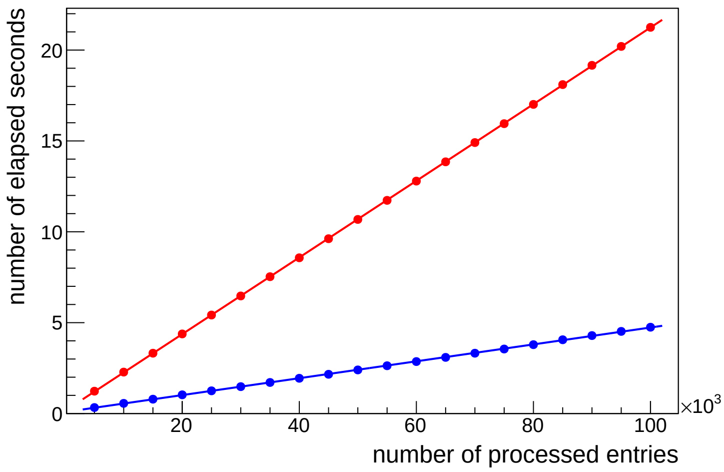

Figure 1: Typical trends of the progress of the program. The dots show the timing data from the standard output of the program, and the lines display the results of fitting linear functions to the data. The blue and red lines illustrate the trends of running the J/ψ example in Section 2.3 and the $\Upsilon(4S)$ example in Section 3.1, respectively. It takes more time in the $\Upsilon(4S)$ example than in the J/ψ example, because the decay of the $\Upsilon(4S)$ resonance is more complex than that of the J/ψ resonance.

The program outputs topology maps to three different files: one plain text file, one tex source file, and one pdf file, with the same main name specified in the card file. For instance, the three files are "jpsi_ta.txt", "jpsi_ta.tex", and "jpsi_ta.pdf" in the example. Although in different formats, the three files have the same information. The pdf file is the easiest to read. It is converted from the tex source file with the command pdflatex. The tex source file is convenient to us if we want to change the style of the pdf file to our taste and when we need to copy and paste (parts of) the topology maps to our slides, papers, and so on. For example, all of the tables displaying topology maps in this user guide are taken from associated tex source files. The plain text file has its own advantage, because the topology maps in it can be checked with text processing commands as well as text editors, and can be used on some occasions as input to the functionality items (see Sections 3 and 4 for details) of another card file.

In addition to the three files for topology maps, one or more root files are output to save topology tags. The root files only include one TTree object, which is entirely the same as that in the input root files, except for the topology tags inserted in all of its entries. The number of root files depends on the size of output data. The program switches to one new root file whenever the size of the TTree object in memory exceeds 3 GB. In the case of the size less than 3 GB, only one root file is output. While the sole or first root file has the same main name as the three files above, more possible root files are denominated with the suffix "_n" (n=1, 2, 3, and so on) appended to the main name. In the example, the first root file is "jpsi_ta.root", and more possible root files would be "jpsi_ta_1.root", "jpsi_ta_2.root", "jpsi_ta_3.root", and so on.

In the example of the previous subsection, the program conducts its basic functionality, namely the component analysis over decay trees. From the 100000 events of the input sample, the program recognizes 17424 decay trees and outputs all of them to the txt, tex, and pdf files. Table 1 shows only the top ten decay trees and their respective final states in the obtained topology map. In the table, “rowNo”, “iDcyTr”, “nEtr”, and “nCEtr” are abbreviations for the row number, index of decay tree, number of entries of decay tree, and number of the cumulative entries from the first to the current decay trees, respectively. The values of “iDcyTr” are assigned from small to large in the program but listed according to the values of “nEtr” from large to small in the table. This is the reason why they are not in natural order like the values of “rowNo”. Since J/ψ is the only root particle for the J/ψ sample, the production branch $e^+e^- \to J/\psi$ is omitted to save page space. Similar rules also apply to other samples with only one root particle. Considering π^0 has a very large production rate and approximatively 99% of it decays to $\gamma\gamma$, the program is designed to discard the decay $\pi^0 \to \gamma\gamma$ by default at the early phase of processing the input data (see Section 5.1.2 for the setting item to alter the behavior). As a result, $\pi^0 \to \gamma\gamma$ does not show itself in the table. Besides, the superscripts “f” and “F” in γ^f and γ^F indicate the final state radiation effect (see Section 5.1.3 for their difference).

Table 1: Top ten decay trees and their respective final states.

rowNo	decay tree	decay final state	iDcyTr	nEtr	nCEtr
1	$J/\psi \to \mu^+\mu^-$	$\mu^+\mu^-$	6	5269	5269
2	$J/\psi \to e^+e^-$	e^+e^-	4	4513	9782
3	$J/\psi \to \pi^0\pi^+\pi^+\pi^-\pi^-$	$\pi^0\pi^+\pi^+\pi^-\pi^-$	0	2850	12632
4	$J/\psi \to \pi^0\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-$	$\pi^0\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-$	2	1895	14527
5	$J/\psi \to \pi^0\pi^+\pi^-K^+K^-$	$\pi^0\pi^+\pi^-K^+K^-$	20	1698	16225
6	$J/\psi \to \rho^+\rho^-\omega, \rho^+ \to \pi^0\pi^+,$ $\rho^- \to \pi^0\pi^-, \omega \to \pi^0\pi^+\pi^-$	$\pi^0\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-$	19	1453	17678
7	$J/\psi \to e^+e^-\gamma^f$	$e^+e^-\gamma^f$	70	1222	18900
8	$J/\psi \to \pi^0\pi^0\pi^+\pi^+\pi^-\pi^-$	$\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-$	127	1161	20061
9	$J/\psi \to \pi^0\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-$	$\pi^0\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-$	234	836	20897
10	$J/\psi \to \pi^0\pi^0\pi^+\pi^-\gamma^F$	$\pi^0\pi^0\pi^+\pi^-\gamma^F$	43	792	21689

In the table, “iDcyTr” is the topology tag for decay trees. Thus, it is also saved in the TTree objects of the output root file, together with other quantities for physics analysis. Therefore, it can be used to pick out the entries of specific decay trees and then examine the distributions of the other quantities over the decay trees. In the example, besides the raw topology truth information, only a random variable following standardized normal distribution, namely X, is stored in the input root files and thus copied by default to the output root file. Though not a genuine variable for physics analysis, X is quite good to illustrate the usage of the topology tag. Figure 2 shows the distribution of X accumulated over the top ten decay trees. The figure is drawn with the root script

examples/in_the_user_guide/ex_for_tb_01/draw_X/v2/draw_X.C,

where, for example, a statement equivalent to

chain–>Draw(“X >>h0”, “iDcyTr==6”)

is used to import X over the decay tree $J/\psi \to \mu^+\mu^-$ from the output root file to the histogram named h0. With such a figure, we can clearly see the contribution of each decay tree. Particularly, we can get to know whether a decay tree has a peak contribution or a contribution mainly distributed in a different region. Based on these distributions, we can get a better understanding of our signals and backgrounds, and thus optimize event selection criteria by applying new requirements on the displayed quantities.

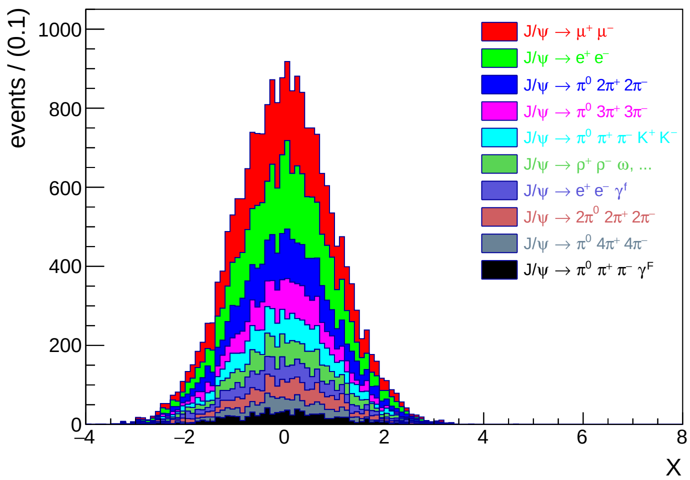

Figure 2: Distribution of X accumulated over the top ten decay trees. In the legend entry "$J/\psi \to \rho^+\rho^-\omega$, ...", the dots "..." represent the secondary decay branches: $\rho^+ \to \pi^0\pi^+$, $\rho^- \to \pi^0\pi^-$, $\omega \to \pi^0\pi^+\pi^-$.

3. Component analysis

Component analysis is the primary functionality of the program. It is performed over decay trees in the previous example. In addition, it can be carried out as follows: over decay initial-final states; with specified particles to check their decay branches, production branches, mothers, cascade decay branches, and decay final states; with specified inclusive decay branches to examine their exclusive components; and with specified intermediate-resonance-allowed (IRA) decay branches to investigate their inner structures. This section introduces the nine (five for specified particles) kinds of component analysis, with each in a subsection. For each kind of component analysis, one item is designed and implemented in the program to set related parameters. In each subsection, we take an example to demonstrate the corresponding setting item and show the resulting topology map. For easy exposition, all of the essential topology tags involved in the component analysis functionalities are presented in another separate subsection, namely the last subsection.

Similar to the case over decay trees, to perform the component analysis over decay initial-final states, we only need to input an positive option "Y" to the corresponding item. Different from the former two kinds, to carry out the latter seven kinds of component analysis, we have to explicitly specify one or more desired particles, inclusive decay branches, or IRA decay branches in the associated items. In the following examples, two particles or decay branches are set to illustrate the use of these items, but only the topology map related to one of them is shown to save space in the paper.

In addition to the indispensable parameters, two sorts of common optional parameters can be set in the items. The first sort is designed for all the nine kinds of component analysis to restrict the maximum number of components output to the txt, tex and pdf files. Without the optional parameters, all components will be output. This is fine if the number of components is not massive. In cases of too many (around ten thousand or more) components, it takes a long time for the program to output the components to the txt and tex files as well as to get the pdf file from the tex file. In such cases, it also takes up a large disk space to save these components in the output files. Considering further that the posterior components are generally unimportant and our time and energy to examine them are limited, it is better to set a maximum to the number of output components. To save space in the paper, we set the maximum number to five in the following examples.

The second sort of optional parameters are developed for the latter seven kinds of component analysis to assign meaningful aliases to the specified particles, inclusive decay branches, and IRA decay branches. By default, the indices 0, 1, 2, and so on are used to tag the particles and decay branches in the names of the TBranch objects appended in the TTree object of the output root files. This is fine, but it is significative to replace the indices with meaningful aliases, particularly in cases of many specified particles or decay branches.

3.1. *Decay trees*

Component analysis over decay trees is the basic kind of component analysis that has already been widely performed in the BESIII experiment. The following example shows the associated item with the maximum number of output components set to five. In the item, a third parameter is also filled and set to “Y”. With the setting, the decay final states in the output pdf file are put under their respective decay trees, rather than in a column next to that for decay trees. It is recommended to use this optional parameter in cases there are too many (about ten or more) particles in some final states. Here, we note that the symbol “–” can be used as a placeholder for the maximum number of output components, if only the third parameter is desired.

```
% Component analysis — decay trees
{
  Y   5   Y
}
```

Component analysis over decay trees is one kind of the most time-consuming topology analysis tasks. To verify the linear pattern further, the progress of running this example, in addition to the example in Section 2.3, is also illustrated in Fig. 1. Apparently, the similar linear pattern is also observed. However, since the decay of the $\Upsilon(4S)$ resonance is more complex than that of the J/ψ resonance, it takes more than twenty seconds for the program to process one hundred thousand events in this example. Nonetheless, the program still has a high processing rate.

Table 2 shows the decay trees. In the table, while the first five decay trees are listed exclusively in the main part, the rest decay trees are only summarized inclusively at the bottom row. In the symbolic expressions of decay initial-final states, the dashed right arrow ($\dashrightarrow$) instead of the plain right arrow ($\rightarrow$) is used, in order to reflect that the initial state does not necessarily decay to the final states in a direct way. Similarly, it is also used in the symbolic expressions of IRA decay branches, which will be introduced in Section 3.9.

Table 2: Decay trees and their respective initial-final states.

rowNo	decay tree (decay initial-final states)	iDcyTr	nEtr	nCEtr
1	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}\gamma^F, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}, D^{*-} \rightarrow \pi^-\bar{D}^0,$ $D^{*+} \rightarrow \pi^+ D^0, \bar{D}^0 \rightarrow \pi^0\pi^-K^+, D^0 \rightarrow \pi^0\pi^+K^-$ $(\Upsilon(4S) \dashrightarrow e^+\nu_e\mu^-\bar{\nu}_\mu\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-K^+K^-\gamma^F)$	20870	3	3
2	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \pi^0\pi^+\pi^+\rho^-D^-, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}, \rho^- \rightarrow \pi^0\pi^-,$ $D^- \rightarrow \pi^-\pi^-K^+, D^{*+} \rightarrow \pi^+D^0, D^0 \rightarrow K^0_L\pi^+\pi^-$ $(\Upsilon(4S) \dashrightarrow \mu^-\bar{\nu}_\mu\pi^0\pi^0K^0_L\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+)$	5295	2	5
3	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \mu^+\nu_\mu D^{*-}, \bar{B}^0 \rightarrow e^-\bar{\nu}_e D^+, D^{*-} \rightarrow \pi^-\bar{D}^0,$ $D^+ \rightarrow e^+\nu_e\bar{K}^*, \bar{D}^0 \rightarrow \pi^0\pi^+\pi^-K^0_S, \bar{K}^* \rightarrow \pi^0\bar{K}^0, K^0_S \rightarrow \pi^+\pi^-, \bar{K}^0 \rightarrow K^0_L$ $(\Upsilon(4S) \dashrightarrow e^+e^-\nu_e\bar{\nu}_e\mu^+\nu_\mu\pi^0\pi^0K^0_L\pi^+\pi^+\pi^-\pi^-\pi^-)$	11954	2	7
4	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}, \bar{B}^0 \rightarrow \pi^0\pi^-\omega D^+, D^{*-} \rightarrow \pi^-\bar{D}^0,$ $\omega \rightarrow \pi^0\pi^+\pi^-, D^+ \rightarrow e^+\nu_e\pi^+K^-, \bar{D}^0 \rightarrow \pi^0\pi^-K^+$ $(\Upsilon(4S) \dashrightarrow e^+e^+\nu_e\nu_e\pi^0\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+K^-)$	14345	2	9
5	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \mu^+\nu_\mu D^{*-}, \bar{B}^0 \rightarrow e^-\bar{\nu}_e D^{*+}\gamma^F, D^{*-} \rightarrow \pi^-\bar{D}^0,$ $D^{*+} \rightarrow \pi^0D^+, \bar{D}^0 \rightarrow \pi^-K^+, D^+ \rightarrow e^+\nu_e\bar{K}^*, \bar{K}^* \rightarrow \pi^+K^-$ $(\Upsilon(4S) \dashrightarrow e^+e^-\nu_e\bar{\nu}_e\mu^+\nu_\mu\pi^0\pi^+\pi^-\pi^-K^+K^-\gamma^F)$	15332	2	11
rest	$\Upsilon(4S) \rightarrow$ others (99980 in total) ($\Upsilon(4S) \dashrightarrow$ corresponding to others)	—	99989	100000

3.2. *Decay initial-final states*

On some occasions, we need to investigate the decay initial-final states of backgrounds for some sophisticated physics analyses. Particularly, it is necessary to differentiate the following two fundamental types of backgrounds: the one with the same initial-final state as the signal, and the other with different initial-final states from the signal. While the latter type of backgrounds needs to be suppressed as much as possible, the former type usually needs to be kept to study more physical effects, for example, the interference effect. Besides, examining the decay initial-final states of backgrounds sheds light on the misjudgement of final state particles at the level of signal candidates. Below is an example demonstrating the related item with the maximum number of output components set to five.

```
% Component analysis — decay initial-final states
{
  Y    5
}
```

The decay initial-final states are displayed in Table 3. The layout of the table is similar to that of Table 2, which shows the decay trees.

Table 3: Decay initial-final states.

rowNo	decay initial-final states	iDcyIFSts	nEtr	nCEtr
1	$\Upsilon(4S) \dashrightarrow \mu^+\nu_\mu\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+K^-$	41	18	18
2	$\Upsilon(4S) \dashrightarrow \pi^0\pi^0\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-\pi^-K^+K^-$	887	18	36
3	$\Upsilon(4S) \dashrightarrow \mu^-\bar{\nu}_\mu\pi^0\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+K^-$	3350	18	54
4	$\Upsilon(4S) \dashrightarrow \pi^0\pi^0\pi^0\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-\pi^-\pi^-K^+K^-$	1215	17	71
5	$\Upsilon(4S) \dashrightarrow \pi^0\pi^0\pi^0\pi^0\pi^0\pi^0K^0_L\pi^+\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^-$	1207	17	88
rest	$\Upsilon(4S) \dashrightarrow$ others (78208 in total)	—	99912	100000

3.3. Decay branches of particles

Invariant mass constraint is one of the most frequently used event selection requirement in high energy physics experiments. With the requirement applied to certain particle, the main backgrounds to its signal decay mode are very likely to be its other decay modes. In this case, it is significative to examine the decay branches of the particle. The following example shows the associated item with the two particles D^{*+} and J/ψ set as research objects. In the item, each row holds the information of a specified particle, and the first, second and third columns are the textual expressions, aliases, and maximum numbers of output components, respectively. As we introduce at the beginning part of this section, the aliases and maximum numbers of output components are both optional. Here, we note that the symbol "−" can be used as a placeholder for an unassigned alias, if only the maximum number of output components is desired.

```
% Component analysis — decay branches of particles
{
  D*+    Dsp    5
  J/psi  Jpsi   5
}
```

Table 4 shows the decay branches of D^{*+}. From the table, only four decay branches of D^{*+} are found in the input inclusive MC sample. Since there is likely one or more cases of D^{*+} decays in one input entry, "nCase" and "nCCase", instead of "nEtr" and "nCEtr", are used in the table in order to accurately indicate what we are counting are the numbers of D^{*+} decays, rather than the numbers of entries involving the D^{*+} decays.

Table 4: Decay branches of D^{*+}.

rowNo	decay branch of D^{*+}	iDcyBrP	nCase	nCCase
1	$D^{*+} \to \pi^+ D^0$	0	31180	31180
2	$D^{*+} \to \pi^0 D^+$	1	13978	45158
3	$D^{*+} \to D^+ \gamma$	2	700	45858
4	$D^{*+} \to \pi^+ D^0 \gamma^F$	3	28	45886

3.4. Production branches of particles

In some cases, we have interest in the production branches of certain particles. Below is an example demonstrating the related item also by taking the two particles D^{*+} and J/ψ as objects of study. The input to this item is the same as that to the above item.

```
% Component analysis — production branches of particles
{
  D*+    Dsp    5
  J/psi  Jpsi   5
}
```

The production branches of D^{*+} are displayed in Table 5. In the production branches, D^{*+} is marked in blue so as to make it noticeable. From the table, the number of production branches of D^{*+} found in the input sample is 3277, much bigger than 4, which is the number of its decay branches.

Table 5: Production branches of D^{*+}.

rowNo	production branch of D^{*+}	iProdBrP	nCase	nCCase
1	$\bar{B}^0 \to \mu^- \bar{\nu}_\mu D^{*+}$	9	4154	4154
2	$\bar{B}^0 \to e^- \bar{\nu}_e D^{*+}$	7	2886	7040
3	$\bar{B}^0 \to D^{*+} D_s^{*-}$	4	1691	8731
4	$\bar{B}^0 \to e^- \bar{\nu}_e D^{*+} \gamma^F$	10	1623	10354
5	$\bar{B}^0 \to \pi^0 \pi^+ \pi^- \pi^- D^{*+}$	40	1429	11783
rest	others (3272 in total)	—	34103	45886

3.5. *Mothers of particles*

Occasionally, we may want to check the mothers of certain particles. The following example shows the associated item also with the two particles D^{*+} and J/ψ set as research objects. The input to this item is identical to those to the two items above.

```
% Component analysis — mothers of particles
{
  D*+    Dsp    5
  J/psi  Jpsi   5
}
```

Table 6 shows the mothers of D^{*+}. Notably, the PDG codes of the mother particles, instead of additional indices, are listed in the table, since they are sufficient to tag the mother particles. From the table, six sources of D^{*+} are found in the input sample and the dominant one is the $\bar{B}^0$ decay.

Table 6: Mothers of D^{*+}.

rowNo	mother of D^{*+}	PDGMoth	nCase	nCCase
1	$\bar{B}^0$	−511	41751	41751
2	B^0	511	2983	44734
3	$D_1'^+$	20413	455	45189
4	D_1^+	10413	368	45557
5	D_2^{*+}	415	247	45804
rest	others (1 in total)	—	82	45886

3.6. *Cascade decay branches of particles*

When the invariant mass constraint is applied to certain particle and the signal process is its cascade decay mode, it is meaningful to investigate its cascade decay branches, rather than its first decay branches, so as to analyze the backgrounds effectively. Below is an example demonstrating the related item by taking the two particles B^0 and D^0 as objects of study. While the first three columns of the input to this item have the same meanings as those to the three items above, the additional fourth column sets the maximum hierarchy of decay branches to be examined. Here, the hierarchy reflects the rank of a decay branch in a cascade decay branch of one specific particle. For instance, in the following cascade decay branch of B^0: $B^0 \to \pi^0\pi^0\rho^0\pi^+D^{*-}$, $\rho^0 \to \pi^+\pi^-$, $D^{*-} \to \pi^-\bar{D}^0$, $\bar{D}^0 \to \eta\eta'$, $\eta \to \pi^0\pi^0\pi^0$, $\eta' \to \pi^0\pi^0\eta$, $\eta \to \gamma\gamma$, the hierarchies of the seven individual decay branches are 1, 2, 2, 3, 4, 4, and 5, respectively. In the example item, the maximum hierarchy of decay branches is set to two for both B^0 and D^0, and hence only the first two hierarchies of branches in their cascade decays will be investigated. Without such settings, all the branches in their cascade decays will be examined.

```
% Component analysis — cascade decay branches of particles
{
   B0   B0   5   2
   D0   D0   5   2
}
```

The cascade decay branches of B^0 are displayed in Table 7.

Table 7: Cascade decay branches of B^0 (only the first two hierarchies are involved).

rowNo	cascade decay branch of B^0	iCascDcyBrsP	nCase	nCCase
1	$B^0 \to \mu^+\nu_\mu D^{*-}, D^{*-} \to \pi^-\bar{D}^0$	12	2912	2912
2	$B^0 \to e^+\nu_e D^{*-}, D^{*-} \to \pi^-\bar{D}^0$	6	1991	4903
3	$B^0 \to \mu^+\nu_\mu D^{*-}, D^{*-} \to \pi^0 D^-$	70	1283	6186
4	$B^0 \to e^+\nu_e D^{*-}\gamma^F, D^{*-} \to \pi^-\bar{D}^0$	18	1132	7318
5	$B^0 \to D^{*-}D_s^{*+}, D^{*-} \to \pi^-\bar{D}^0, D_s^{*+} \to D_s^+\gamma$	20	1119	8437
rest	$B^0 \to$ others (42074 in total)	—	91594	100031

3.7. *Decay final states of particles*

When the invariant mass constraint is applied to certain particle reconstructed directly from some final state particles, it is significative to examine its decay final states, rather than its first or cascade decay branches, at the truth level in order to analyze the backgrounds effectively. The following example shows the associated item also with the two particles B^0 and D^0 set as research objects. The format of the input to the item is the same as that to the above item, but the fourth parameters here are designed to restrict the numbers of final state particles. Without the fourth parameters, all the decay final states of the specified particles will be investigated. In the example, the parameters are set to three for both B^0 and D^0, and thus only the three-body decay final states of them will be examined.

```
% Component analysis — decay final states of particles
{
   B0   B0   5   3
   D0   D0   5   3
}
```

Table 8 shows the three-body decay final states of D^0. In the table, π^0 only decays to $\gamma\gamma$; otherwise, it will be replaced with its decay products, resulting in different decay final states of D^0.

Table 8: Decay final states of D^0 (only three-body final states are involved).

rowNo	decay final state of D^0	iDcyFStP	nCase	nCCase
1	$D^0 \dashrightarrow \pi^0\pi^+K^-$	2	6258	6258
2	$D^0 \dashrightarrow \mu^+\nu_\mu K^-$	5	1487	7745
3	$D^0 \dashrightarrow \pi^0\pi^+\pi^-$	1	1162	8907
4	$D^0 \dashrightarrow K_L^0\pi^+\pi^-$	3	1158	10065
5	$D^0 \dashrightarrow e^+\nu_e K^-$	11	1148	11213
rest	$D^0 \dashrightarrow$ others (24 in total)	—	2407	13620

3.8. *Inclusive decay branches*

In some cases, we are interested in the exclusive components of certain inclusive decay branches. Below is an example demonstrating the related item by taking the two inclusive decay branches $\bar{B}^0 \rightarrow D^{*+} + anything$ and $B^0 \rightarrow K_S^0 + anything$ as objects of study. In the item, each row holds the information of a inclusive decay branch, and the first, second, and third columns separated with the symbol "&" are the textual expressions, aliases, and maximum numbers of output components, respectively. As we introduce at the beginning part of this section, the aliases and maximum numbers of output components are both optional. Here, we note that the symbol "−" can be used as a placeholder for an unassigned alias, if only the maximum number of output components is desired.

```
% Component analysis — inclusive decay branches
{
  B0 −−> D*+   &   B2Dsp   &   5
  B0 −−> K_S0   &   B2Ks   &   5
}
```

The exclusive components of $B^0 \rightarrow K_S^0 + anything$ are displayed in Table 9. From the table, ten exclusive components of the inclusive decay branch are found in the input sample, and the particles denoted with *anything* are mainly the traditional charmonium states.

Table 9: Exclusive components of $B^0 \rightarrow K_S^0 + anything$.

rowNo	exclusive component of $B^0 \rightarrow K_S^0 + anything$	iDcyBrIncDcyBr	nCase	nCCase
1	$B^0 \rightarrow K_S^0 J/\psi$	0	45	45
2	$B^0 \rightarrow K_S^0 \eta_c$	1	40	85
3	$B^0 \rightarrow K_S^0 \psi'$	3	33	118
4	$B^0 \rightarrow K_S^0 \chi_{c1}$	2	20	138
5	$B^0 \rightarrow K_S^0 \chi_{c0}$	4	6	144
rest	$B^0 \rightarrow K_S^0$ + others (5 in total)	—	9	153

3.9. *Intermediate-resonance-allowed decay branches*

Table 10: Exclusive components of $D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$.

rowNo	exclusive component of $D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$	iDcyBrIRADcyBr	nCase	nCCase
1	$D^{*+} \rightarrow \pi^+ D^0, D^0 \rightarrow \pi^0\pi^+K^-$	0	3869	3869
2	$D^{*+} \rightarrow \pi^0 D^+, D^+ \rightarrow \pi^+\pi^+K^-$	1	1102	4971

Occasionally, we may want to investigate the inner structures of certain IRA decay branches. The following example shows the associated item with the two IRA decay branches $D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$ and $J/\psi \dashrightarrow \pi^0\pi^+\pi^-$ set as research objects. Since IRA decay branches look like inclusive decay branches, the format of the input to the item for IRA decay branches is identical to that for inclusive decay branches, which is introduced in the previous subsection.

```
% Component analysis — intermediate-resonance-allowed decay branches
{
  D*+ −−> K− pi+ pi+ pi0   &   Dsp2K3Pi   &   5
  J/psi −−> pi+ pi− pi0   &   Jpsi23Pi   &   5
}
```

Table 10 shows the exclusive components of $D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$. From the table, two intermediate particles D^0 and D^+ are found in the IRA decay branch, and they decay to $\pi^0\pi^+K^-$ and $\pi^+\pi^+K^-$, respectively.

3.10. Essential topology tags

Table 11: Essential topology tags involved in each kind of component analysis.

Component analysis kind	Topology tag	Interpretation
Decay trees	iDcyTr	index of decay tree
Decay initial-final states	iDcyIFSts	index of decay initial-final states
Decay branches of particles	nPDcyBr_i	number of particle$_\mathrm{i}$s (or its decay branches)
	iDcyBrP_i_j	index of decay branch of the j$^\mathrm{th}$ particle$_\mathrm{i}$
Production branches of particles	nPProdBr_i	number of particle$_\mathrm{i}$s (or its production branches)
	iProdBrP_i_j	index of production branch of the j$^\mathrm{th}$ particle$_\mathrm{i}$
Mothers of particles	nPMoth_i	number of particle$_\mathrm{i}$s (or its mothers)
	PDGMothP_i_j	PDG code of mother of the j$^\mathrm{th}$ particle$_\mathrm{i}$
Cascade decay branches of particles	nPCascDcyBr_i	number of particle$_\mathrm{i}$s (or its cascade decay branches)
	iCascDcyBrP_i_j	index of cascade decay branch of the j$^\mathrm{th}$ particle$_\mathrm{i}$
Decay final states of particles	nPDcyFSt_i	number of particle$_\mathrm{i}$s (or its decay final states)
	iDcyFStP_i_j	index of decay final state of the j$^\mathrm{th}$ particle$_\mathrm{i}$
Inclusive decay branches	nIncDcyBr_i	number of inclusive decay branch$_\mathrm{i}$es
	iDcyBrIncDcyBr_i_j	index of decay branch of the j$^\mathrm{th}$ inclusive decay branch$_\mathrm{i}$
IRA decay branches	nIRADcyBr_i	number of IRA decay branch$_\mathrm{i}$es
	iDcyBrIRADcyBr_i_j	index of decay branch of the j$^\mathrm{th}$ IRA decay branch$_\mathrm{i}$

Table 11 lists and interprets all of the essential topology tags involved in the component analysis functionalities. The topology tag for the component analysis over decay initial-final states is iDcyIFSts. It has the similar interpretation as iDcyTr and is shown in the third column of Table 3. For the latter seven kinds of component analysis, there are two sorts of topology tags. The first sort, such as nPDcyBr_i, records the number of the specified particles or decay branches found in each entry. The second sort, for example iDcyBrP_i_j, keeps the corresponding index of each instance of one specified particle or decay branch found in each entry. The indices are also listed in the third columns of Tables 4 – 10.

In the topology tags, "i" in "_i" is the default index of the specified particle or decay branch, and it ranges from 0 (included) to the number of specified particles or decay branches (excluded). If the alias of the particle or decay branch is also specified, the index "i" will be replaced with the alias. For example, in the component analysis over decay branches of D^{*+} and J/ψ, since "Dsp" and "Jpsi" are set as their aliases, the specialised topology tags nPDcyBr_Dsp and nPDcyBr_Jpsi, instead of the default ones nPDcyBr_0 and nPDcyBr_1, are used to store the numbers of D^{*+} and J/ψ (or their decay branches) found in each entry.

In addition, "j" in "_j" is the default index of the particle or decay branch found in an entry, and it ranges from 0 (included) to the sample-level maximum of the number of the particles or decay branches found in each entry (excluded). For example, in the component analysis over decay branches of D^{*+}, the sample-level maximum of the number of D^{*+} (or its decay branches) found in each entry is two, and thus the indices of the D^{*+} decay branches are stored in the topology tags iDcyBrP_Dsp_0 and iDcyBrP_Dsp_1. The indices range from 0 (include) to the number of the categories of the D^{*+} decay branches found in the samples. In the entries with only one D^{*+}, iDcyBrP_Dsp_1 is assigned with the default value −1; in the entries which have no D^{*+}, the default value −1 is assigned to both iDcyBrP_Dsp_0 and iDcyBrP_Dsp_1. We note that different from all other indices, PDGMoth_i_j has the default value 0, instead of −1.

4. Signal identification

Signal identification is the other functionality of the program. Though it is a relatively simple functionality, it can help us identify the signals we desire directly, quickly, and easily. At present, the following eight kinds of signals can be identified with the program: (1) decay trees, (2) decay initial-final states, (3) particles, (4) (regular) decay branches, (5) cascade decay branches, (6) inclusive decay branches, (7) inclusive cascade decay branches, and (8) IRA decay branches. For each kind of signals, one item is developed to specify related parameters. This section introduces the eight kinds of signal identification, with each in a subsection. In each subsection, we take an example to demonstrate the related setting item and show the obtained topology map. For easy exposition, all of the essential topology tags involved in the signal identification functionalities are presented in another separate subsection, that is, the last subsection.

Similar to the cases of the latter seven kinds of component analysis, one or more signals can be specified in each of the signal identification items, and two signals are set in the following examples to illustrate the use of the items. Besides, meaning aliases can also be optionally assigned to the specified signals so as to better tag them in the names of the TBranch objects appended in the TTree object of the output root files.

4.1. Decay trees

Sometimes, we need to identify certain decay trees. The following example shows the associated item with the first two decay trees listed in Table 2 set as signals. In the item, each row holds a decay branch in the decay trees, and the first, second, and third columns separated with the symbol "&" are the indices, textual expressions, and mother indices of the decay branches, respectively. In addition, the decay branches with index 0 indicate the beginning of new decay trees, and their mother indices are equal to −1, suggesting they have no mother branches because they are the first decay branches of the decay trees. Besides, a name of each decay tree can be optionally filled in the fourth column of its first decay branch. Similar to the third parameter in the item for the component analysis over decay trees (see Section 3.1), a "Y" can be optionally filled in the fifth column of the first decay branch of the first decay tree, to adjust the positions of decay final states in the output pdf file.

```
% Signal identification — decay trees
{
   0  &  Upsilon(4S) --> B0 anti-B0  &  -1  &  1stDcyTrInTb2  &  Y
   1  &  B0 --> e+ nu_e D*- gamma  &  0
   2  &  anti-B0 --> mu- anti-nu_mu D*+  &  0
   3  &  D*- --> pi- anti-D0  &  1
   4  &  D*+ --> pi+ D0  &  2
   5  &  anti-D0 --> pi0 pi- K+  &  3
   6  &  D0 --> pi0 pi+ K-  &  4

   0  &  Upsilon(4S) --> B0 anti-B0  &  -1  &  2ndDcyTrInTb2
   1  &  B0 --> pi0 pi+ pi- rho- D-  &  0
   2  &  anti-B0 --> mu- anti-nu_mu D*+  &  0
   3  &  rho- --> pi0 pi-  &  1
   4  &  D- --> pi- pi- K+  &  1
   5  &  D*+ --> pi+ D0  &  2
   6  &  D0 --> K_L0 pi+ pi-  &  5
```

```
}
```

Table 12 shows the resulting topology map. The results are the same as those displayed in the first two rows of Table 2.

Table 12: Signal decay trees and their respective initial-final states.

rowNo	signal decay tree (signal decay initial-final states)	iSigDcyTr	nEtr	nCEtr
1	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}\gamma^F, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}, D^{*-} \rightarrow \pi^-\bar{D}^0,$ $D^{*+} \rightarrow \pi^+ D^0, \bar{D}^0 \rightarrow \pi^0\pi^-K^+, D^0 \rightarrow \pi^0\pi^+K^-$ $(\Upsilon(4S) \dashrightarrow e^+\nu_e\mu^-\bar{\nu}_\mu\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-K^+K^-\gamma^F)$	0	3	3
2	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \pi^0\pi^+\pi^+\rho^-D^-, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}, \rho^- \rightarrow \pi^0\pi^-,$ $D^- \rightarrow \pi^-\pi^-K^+, D^{*+} \rightarrow \pi^+D^0, D^0 \rightarrow K_L^0\pi^+\pi^-$ $(\Upsilon(4S) \dashrightarrow \mu^-\bar{\nu}_\mu\pi^0\pi^0K_L^0\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+)$	1	2	5

4.2. Decay initial-final states

In a few cases, we have interest in some decay initial-final states. Below is an example demonstrating the related item by taking the first two decay initial-final states listed in Table 3 as signals. Similar to IRA decay branches, decay initial-final states look like inclusive decay branches. Hence, except that only two columns are involved in the item, the format of the input to the item for decay initial-final states is identical to that for the component analysis over inclusive decay branches, which is introduced in Section 3.8. As we can see from the example, the numbers of identical particles are supported to be written in front of their textual names in order to simplify the textual expressions of the final states.

```
% Signal identification — decay initial-final states
{
  Y(4S) --> mu+ nu_mu 3 pi0 3 pi+ 4 pi- K+ K-  &  2ndDcyIFStsInTb3
  Y(4S) --> 5 pi0 5 pi+ 5 pi- K+ K-  &  2ndDcyIFStsInTb3
}
```

The obtained topology map is displayed in Table 13. The results are identical to those shown in the first two rows of Table 3.

Table 13: Signal decay initial-final states.

rowNo	signal decay initial-final states	iSigDcyIFSts2	nEtr	nCEtr
1	$\Upsilon(4S) \dashrightarrow \mu^+\nu_\mu\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+K^-$	0	18	18
2	$\Upsilon(4S) \dashrightarrow \pi^0\pi^0\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-\pi^-K^+K^-$	1	18	36

4.3. Particles

Occasionally, we may want to identify some particles. The following example shows the associated item with the two particles D^{*+} and J/ψ set as signals. Except that only two columns are involved in the item, the format of the input to the item is identical to that for the component analysis over decay branches of particles, which is introduced in Section 3.3.

```
% Signal identification — particles
{
  D*+   Dsp
  J/psi  Jpsi
}
```

Table 14 shows the resulting topology map. As a cross-check, the number of D^{*+}s in the table equals those in Tables 4, 5, and 6.

Table 14: Signal particles.

rowNo	signal particle	iSigP	nCase	nCCase
1	D^{*+}	0	45886	45886
2	J/ψ	1	2654	48540

4.4. Decay branches

On some occasions, we have to identify certain regular decay branches. Below is an example demonstrating the related item by taking the two decay branches $\bar{B}^0 \to \mu^-\bar{\nu}_\mu D^{*+}$ and $B^0 \to K_S^0 J/\psi$ as signals. Since regular decay branches also look like inclusive decay branches, except that only two columns are involved in the item, the format of the input to the item for regular decay branches is identical to that for the component analysis over inclusive decay branches, which is introduced in Section 3.8.

```
% Signal identification — decay branches
{
  B0 --> mu- anti-nu_mu D*+   &   B2munuDsp
  B0 --> K_S0 J/psi   &   B2KsJpsi
}
```

The obtained topology map is displayed Table 15. For the purpose of cross-checks, we note that the number of $\bar{B}^0 \to \mu^-\bar{\nu}_\mu D^{*+}$ ($B^0 \to K_S^0 J/\psi$) in the table is equal to that in the first row of Table 5 (9).

Table 15: Signal decay branches.

rowNo	signal decay branch	iSigDcyBr	nCase	nCCase
1	$\bar{B}^0 \to \mu^-\bar{\nu}_\mu D^{*+}$	0	4154	4154
2	$B^0 \to K_S^0 J/\psi$	1	45	4199

4.5. Cascade decay branches

Sometimes, we are interested in certain cascade decay branches. The following example shows the associated item with the two cascade decay branches $B^0 \to D^{*-}D_s^{*+}$, $D^{*-} \to \pi^-\bar{D}^0$, $D_s^{*+} \to D_s^+\gamma$ and $B^0 \to D^{*-}D_s^{*+}$, $D^{*-} \to \pi^-\bar{D}^0$ set as signals. While the first cascade decay branch is identical to the fifth one in Table 7, the second is only part of it, which demonstrates that the cascade decay branches supported in the item are not necessarily fully specified at the level of certain hierarchy. Similar to decay trees, cascade decay branches are made up of regular decay branches. Hence, the format of the input to the item for cascade decay branches is identical to that for decay trees, which is introduced in Section 4.1.

```
% Signal identification — cascade decay branches
{
  0  &  B0 --> D*- D_s*+   &  -1
  1  &  D*- --> pi- anti-D0   &  0
  2  &  D_s*+ --> D_s+ gamma   &  0

  0  &  B0 --> D*- D_s*+   &  -1
```

```
    1   &   D*- --> pi- anti-D0   &   0
}
```

Table 16 shows the resulting topology map. As a cross-check, the number of cases of the first cascade decay branch in the table equals that of the fifth cascade decay branch in Table 7.

Table 16: Signal cascade decay branches.

rowNo	signal cascade decay branch	iSigCascDcyBrs	nCase	nCCase
1	$B^0 \to D^{*-}D_s^{*+}, D^{*-} \to \pi^-\bar{D}^0, D_s^{*+} \to D_s^+\gamma$	0	1119	1119
2	$B^0 \to D^{*-}D_s^{*+}, D^{*-} \to \pi^-\bar{D}^0$	1	1180	2299

4.6. Inclusive decay branches

In a few cases, we have to identify some inclusive decay branches. Below is an example demonstrating the related item by taking the two inclusive decay branches $\bar{B}^0 \to D^{*+} + anything$ and $B^0 \to K_S^0 + anything$ as signals. Except that only two columns are involved in the item, the format of the input to the item is identical to that for the component analysis over inclusive decay branches, which is introduced in Section 3.8.

```
% Signal identification — inclusive decay branches
{
  anti−B0 −−> D*+   &   B2Dsp
  B0 −−> K_S0   &   B2Ks
}
```

The obtained topology map is displayed in Table 17. As a cross-check, the number of $B^0 \to K_S^0 + anything$ in the table equals that in Table 9.

Table 17: Signal inclusive decay branches.

rowNo	signal inclusive decay branch	iSigIncDcyBr	nCase	nCCase
1	$\bar{B}^0 \to D^{*+} + anything$	0	41751	41751
2	$B^0 \to K_S^0 + anything$	1	153	41904

4.7. Inclusive cascade decay branches

Occasionally, we may have interest in certain inclusive cascade decay branches. The following example shows the associated item with the two inclusive cascade decay branches $\bar{B}^0 \to D^{*+} + anything$, $D^{*+} \to \pi^+D^0$ and $B^0 \to K_S^0 J/\psi$, $K_S^0 \to \pi^+\pi^-$, $J/\psi \to \mu^+ + anything$ set as signals. Similar to decay trees and cascade decay branches, inclusive cascade decay branches are made up of regular decay branches. Hence, the format of the input to the item for inclusive cascade decay branches is also identical to that for decay trees, which is introduced in Section 4.1. and the independent textual name "*" denotes anything.

```
% Signal identification — inclusive cascade decay branches
{
  0   &   anti-B0 --> D*+ *   &   −1
  1   &   D*+ --> pi+ D0   &   0

  0   &   B0 --> K_S0 J/psi   &   −1
  1   &   K_S0 --> pi+ pi−   &   0
  2   &   J/psi --> mu+ *   &   0
```

```
}
```

Table 18 shows the resulting topology map.

Table 18: Signal inclusive cascade decay branches.

rowNo	signal inclusive cascade decay branch	iSigIncCascDcyBrs	nCase	nCCase
1	$\bar{B}^0 \to D^{*+} + anything, D^{*+} \to \pi^+ D^0$	0	28367	28367
2	$B^0 \to K_S^0 J/\psi, K_S^0 \to \pi^+\pi^-, J/\psi \to \mu^+ + anything$	1	1	28368

4.8. *Intermediate-resonance-allowed decay branches*

On some occasions, we need to identify certain IRA decay branches. Below is an example demonstrating the related item by taking the two IRA decay branches $D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$ and $J/\psi \dashrightarrow \pi^0\pi^+\pi^-$ as signals. Except that only two columns are involved in the item, the format of the input to the item is identical to that for the component analysis over IRA decay branches, which is introduced in Section 3.9.

```
% Signal identification — intermediate-resonance-allowed decay branches
{
  D*+ --> K- pi+ pi+ pi0    &    Dsp2K3Pi
  J/psi --> pi+ pi- pi0    &    Jpsi23Pi
}
```

The obtained topology map is displayed in Table 19. For the purpose of cross-checks, we note that the number of $D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$ in the table is equal to that in Table 10.

Table 19: Signal IRA decay branches.

rowNo	signal IRA decay branch	iSigIRADcyBr	nCase	nCCase
1	$D^{*+} \dashrightarrow \pi^0\pi^+\pi^+K^-$	0	4971	4971
2	$J/\psi \dashrightarrow \pi^0\pi^+\pi^-$	1	59	5030

4.9. *Essential topology tags*

Table 20 summarizes and explains all of the essential topology tags involved in the signal identification functionalities. For signal decay trees and signal decay initial-final states, there are two sorts of topology tags. The first sort of tags, iSigDcyTr and iSigDcyIFSts, record the default indices of the specified signal decay trees and signal decay initial-final states. They have the similar interpretation as iDcyTr and iDcyIFSts, and are shown in the third columns of Tables 12 and 13. The second sort of tags, nameSigDcyTr and nameSigDcyIFSts, save the specified aliases of the signal decay trees and signal decay initial-final states. In cases the aliases are not specified, empty strings will be stored.

For the latter six kinds of signal identification, there are only one sort of topology tags, which record the number of the specified particles or decay branches found in each entry. Similar to the cases in the latter seven kinds of component analysis, in the topology tags, "i" in "_i" is the default index of the specified particle or decay branch, and it ranges from 0 (included) to the number of specified particles or decay branches (excluded). If the alias of the particle or decay branch is also specified, the index "i" will be replaced with the alias.

Table 20: Essential topology tags involved in each kind of signal identification.

Signal identification kind	Topology tag	Interpretation
Decay trees	iSigDcyTr	index of signal decay tree
	nameSigDcyTr	name of signal decay tree
Decay initial-final states	iSigDcyIFSts	index of signal decay initial-final states
	nameSigDcyIFSts	name of signal decay initial-final states
Particles	nSigP_i	number of signal particle$_i$s
Decay branches	nSigDcyBr_i	number of signal decay branch$_i$es
Cascade decay branches	nSigCascDcyBr_i	number of signal cascade decay branch$_i$es
Inclusive decay branches	nSigIncDcyBr_i	number of signal inclusive decay branch$_i$es
Inclusive cascade decay branches	nSigIncCascDcyBr_i	number of signal inclusive cascade decay branch$_i$es
IRA decay branches	nSigIRADcyBr_i	number of signal IRA decay branch$_i$es

5. Common settings

From Sections 3 and 4, the optional parameters of the functionality items give us more choices and thus help us do our jobs quicker and better. In addition to these parameters, many optional items are designed and implemented to control the execution of the program in order to meet practical needs. Unlike the optional parameters, which only affect the individual functionalities to which they belong, the optional items have impact on all of the functionalities, or at least most of the functionalities. The current version of the program contains 24 commonly used items, which can be divided into the following three groups: items on the input of the program, items on the functionalities of the program, and items on the output of the program. This section introduces these items in the three groups, with each group in one subsection.

5.1. Settings on the input of the program

5.1.1. Input entries

The program normally processes all of the entries in the input samples, but sometimes only a part of the entries are needed to be (first) processed. Running the program over a big sample usually takes a long time. In such a case, it is a good habit to run the program first over a small part of the sample to check possible exceptions, and then over the whole sample if no exceptions are found or after the found exceptions are handled. Besides, a small number of entries is usually sufficient to do tests in the developing of the program. For these reasons, an item is developed to set up the maximum number of entries to be processed. Below is an example showing the item with the maximum number set at two thousand.

```
% Maximum number of entries to be processed
{
   2000
}
```

On some occasions, especially in the course of optimizing selection criteria, we need to run the program only over entries satisfying certain requirements. For this purpose, an item is developed to select entries. The following example shows the item with X set in the range $(-1, 1)$.

```
% Cut to select entries
{
   (X >−1) && (X <1)
}
```

Notably, only a single-line selection requirement is supported in the item, like the cases in the methods Draw() and GetEntries() of the class TTree. In spite of this, such a requirement is able to express any requirement with the help of the parentheses "()" as well as the logical symbols "&&", "||", and "!".

Occasionally, array variables are involved in the requirement. Under the circumstances, users have to tell the program how to determine the total logical value with the individual logical values. At present, two criteria are provided: (1) the total result is true as long as the result for one instance is true; (2) the total result is false as long as the result for one instance is false. By default, the second criterion is used in the program. One can alter it to the first one with the following item.

```
% Method to apply cut to array variables (Two options: T and F. Default: F)
{
  T
}
```

In the item, "T" and "F" stand for the first and second criteria, respectively.

5.1.2. *Input decay branches*

Normally, the program deals with all of the decay branches in every decay tree. However, examining all the branches is not always required in practice. Sometimes, we only concern the first n hierarchies of the branches. Similar to that in cascade decay branches of particles (as we introduce in Section 3.6), the hierarchy here reflects the rank of a decay branch in a decay tree. For example, in the decay tree $\Upsilon(4S) \rightarrow B^0\bar{B}^0$, $B^0 \rightarrow e^+\nu_e D^{*-}\gamma^F$, $\bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}$, $D^{*-} \rightarrow \pi^-\bar{D}^0$, $D^{*+} \rightarrow \pi^+ D^0$, $\bar{D}^0 \rightarrow \pi^0\pi^-K^+$, $D^0 \rightarrow \pi^0\pi^+K^-$, the hierarchies of the seven individual branches are 1, 2, 2, 3, 3, 4, and 4, respectively. The program provides an item to set the maximum hierarchy. Below is an example showing the item with the maximum hierarchy set at one.

```
% Maximum hierarchy of heading decay branches to be processed in each event
{
  1
}
```

With the setting, the decay branches with hierarchy larger than one will be ignored by the program. For the component analysis over the decay trees of the $\Upsilon(4S)$ sample, only the first hierarchy of $\Upsilon(4S)$ decay branches are analyzed, and the result is shown in Table 21. From the table, not only $\Upsilon(4S) \rightarrow B^0\bar{B}^0$ but also $\Upsilon(4S) \rightarrow B^0B^0$ and $\Upsilon(4S) \rightarrow \bar{B}^0\bar{B}^0$ are seen because of B^0-$\bar{B}^0$ mixing.

Table 21: Decay trees and their respective initial-final states.

rowNo	decay tree (decay initial-final states)	iDcyTr	nEtr	nCEtr
1	$\Upsilon(4S) \rightarrow B^0\bar{B}^0$ ($\Upsilon(4S) \dashrightarrow B^0\bar{B}^0$)	0	81057	81057
2	$\Upsilon(4S) \rightarrow B^0B^0$ ($\Upsilon(4S) \dashrightarrow B^0B^0$)	1	9487	90544
3	$\Upsilon(4S) \rightarrow \bar{B}^0\bar{B}^0$ ($\Upsilon(4S) \dashrightarrow \bar{B}^0\bar{B}^0$)	2	9456	100000

Similarly, in the case of the maximum hierarchy set at two, we could get the result of the component analysis over the first two hierarchies of $\Upsilon(4S)$ decay branches, as displayed in Table 22.

Table 22: Decay trees and their respective initial-final states.

rowNo	decay tree (decay initial-final states)	iDcyTr	nEtr	nCEtr
1	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \mu^+\nu_\mu D^{*-}, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}$ $(\Upsilon(4S) \dashrightarrow \mu^+\mu^-\nu_\mu\bar{\nu}_\mu D^{*+}D^{*-})$	936	136	136
2	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}$ $(\Upsilon(4S) \dashrightarrow e^+\nu_e\mu^-\bar{\nu}_\mu D^{*+}D^{*-})$	1188	112	248
3	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \mu^+\nu_\mu D^{*-}, \bar{B}^0 \rightarrow e^-\bar{\nu}_e D^{*+}$ $(\Upsilon(4S) \dashrightarrow e^-\bar{\nu}_e\mu^+\nu_\mu D^{*+}D^{*-})$	268	110	358
4	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow D^{*-}D_s^{*+}, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}$ $(\Upsilon(4S) \dashrightarrow \mu^-\bar{\nu}_\mu D^{*+}D^{*-}D_s^{*+})$	2063	72	430
5	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}, \bar{B}^0 \rightarrow e^-\bar{\nu}_e D^{*+}$ $(\Upsilon(4S) \dashrightarrow e^+e^-\nu_e\bar{\nu}_e D^{*+}D^{*-})$	95	71	501
rest	$\Upsilon(4S) \rightarrow$ others (81609 in total) $(\Upsilon(4S) \dashrightarrow$ corresponding to others)	—	99499	100000

Sometimes, we do not care about the decay of some particles. One can make the program ignore their decay branches with the following item. With the setting in the example, the decay of B^0 and $\bar{B}^0$ will be ignored by the program.

```
% Ignore the decay of the following particles
{
   B0
   anti-B0
}
```

At some other times, we have interest in the decay of some particles but not in the decay of their daughters. To handle this case, the following item is developed to make the program ignore the decay of their daughters. In the following example, the decay of the daughters of B^0 and $\bar{B}^0$ will be ignored by the program.

```
% Ignore the decay of the daughters of the following particles
{
   B0
   anti-B0
}
```

The two settings above have the same effects as those in the previous paragraph which set the maximum hierarchy at one and two, and hence the corresponding results are identical to those shown in Tables 21 and 22.

As mentioned in Section 2.4, the decay $\pi^0 \rightarrow \gamma\gamma$ is ignored by default. On the occasions when we need to identify the signals involving the decay, we can make the program retain the decay with the item below set to "Y".

```
% Retain the decay of pi0 to gamma gamma (Two options: Y and N. Default: N)
{
   Y
}
```

Besides, if needed, one can make the program ignore other final decay branches, such as $\eta \rightarrow \gamma\gamma$ and $K_S^0 \rightarrow \pi^+\pi^-$, with the following item.

```
% Ignore the following final decay branches
{
```

```
    eta --> gamma gamma
    K_S0 --> pi+ pi-
}
```

5.1.3. Initial and final state radiation photons

Initial state radiation (ISR) and final state radiation (FSR) are inevitable physical effects in e^+e^- colliding experiments. Therefore, ISR and FSR photons are often involved in the inclusive MC samples. The program processes them together with other particles in the default case. To distinguish them from other photons, the program tries to label them in the output txt, tex and pdf files. Sometimes, these photons are marked out beforehand with special PDG codes according to particle status information from generators. One can inform the program of these PDG codes by the following two items.

```
% PDG code of ISR photons (Default: 222222222)
{
    222222222
}


% PDG code of FSR photons (Default: -22)
{
    -22
}
```

In this case, the program is able to label the ISR and FSR photons as γ^i (gammai) and γ^f (gammaf) in the output pdf (txt) files, respectively.

On other occasions, ISR and FSR photons are not marked out in advance due to some reasons. In such cases, the program have to identify them by itself according to the following rules: photons which have no mothers recorded in the arrays of the PDG codes and mother indices are considered as generalized ISR photons, while other photons which have at least one $e^\pm$, $\mu^\pm$, $\pi^\pm$, $K^\pm$, p, or $\bar{p}$ sister are taken as generalized FSR photons. Here, the modifier "generalized" is used because the rules can not determine the types of the photons in absolute accuracy. For example, photons from radiative decays might be mistaken as ISR and FSR photons. Despite this, generalized ISR and FSR photons are good concepts, particularly in cases where the sources of the photons are not required to be distinguished clearly. The program will label the generalized ISR and FSR photons as γ^I (gammaI) and γ^F (gammaF) in the output pdf (txt) files, respectively.

Notably, we are not concerned about these ISR and FSR photons in many cases. If they have already been marked out beforehand, one can make the program ignore them accurately by setting the following two items to "Ys".

```
% Ignore ISR photons (Three options: Ys, Yg and N. Default: N)
{
    Ys
}


% Ignore FSR photons (Three options: Ys, Yg and N. Default: N)
{
    Ys
}
```

In cases that these photons are not marked in advance, the option "Yg" can be used to ignore the generalized ISR and FSR photons. In "Ys" and "Yg", "s" and "g" are the initials of the words "strict" and "generalized", respectively.

5.2. Settings on the functionalities of the program

5.2.1. Candidate based analysis

According to the number of signal candidates in an event that are selected and retained to extract physics results, data analysis in high energy experiments can be divided into the following two categories: event based analysis and candidate based analysis. While at most one candidate in an event is kept in event based analysis, one or more candidates in an event can be retained in candidate based analysis. Generally, the quantities related to a candidate are stored in an entry of the TTree objects in the root files. Thus, one or more entries relate to an event in candidate based analysis, while only one entry corresponds to an event in event based analysis. Normally, the indices of candidates within an event are stored in the corresponding entries in candidate based analysis.

By default, the program analyzes the input entries one by one. In this case, the events with multiple candidates will be processed repeatedly. Particularly, the number of physics processes at the sample level will be over counted. One can make the program avoid the problem by inputting “Y” to the following item.

```
% Avoid over counting for candidate based analysis (Two options: Y and N. Default: N)
{
  Y
}
```

Also, the indices of candidates within an event are required. We can tell the program the related TBranch name with the following item.

```
% TBranch name of the indices of candidates in an event (Default: __candidate__)
{
  iCandidate
}
```

With the settings, the program will process the first entry of each event in a normal way, including obtaining and storing the topology tags; it will not analyze the other entries of the same event, but only store the same topology tags to them.

5.2.2. Charge conjugation

Charge conjugation is an important concept in high energy physics. By default, charge conjugate objects (particles and decays) are processed separately in the program. However, we need to handle them together in many physics studies because of the sameness between them. One can have the program process them together with the item below set to “Y”.

```
% Process charge conjugate objects together (Two options: Y and N. Default: N)
{
  Y
}
```

Performing topology analysis with the setting inserts new topology tags in the output root files and adds new counters to topology maps in the output txt, tex, and pdf files. Tables 23 and 24 list and interpret all of the topology tags related to charge conjugation involved in the component analysis and signal identification functionalities, respectively.

As an example, we perform the component analysis over decay trees with the charge conjugate item. Table 25 shows the obtained topology map. Besides the columns in Table 2, two additional columns with the headers “nCcEtr” and “nAllEtr” are inserted in the table. Here, “nCcEtr” represents the number of entries involving the charge conjugate decay trees, and “nAllEtr”

Table 23: Topology tags related to charge conjugation involved in each kind of component analysis. For the latter seven kinds of component analysis, the topology tags in the 1) and 2) groups are only designed for the self-charge-conjugate and non-self-charge-conjugate particles and decay branches, respectively. The acronyms "cc" and $\mathrm{index_{cc}}$ are short for "charge conjugate" and "charge conjugate index", respectively.

Component analysis kind	Topology tag	Interpretation
Decay trees	iCcDcyTr	$\mathrm{index_{cc}}$ of decay tree
Decay initial-final states	iCcDcyIFSts	$\mathrm{index_{cc}}$ of decay initial-final states
Decay branches of particles	iCcPDcyBr_i	$\mathrm{index_{cc}}$ of $\mathrm{particle_i}$
	1) iCcDcyBrP_i_j	$\mathrm{index_{cc}}$ of decay branch of the $\mathrm{j^{th}}$ $\mathrm{particle_i}$
	2) nCcPDcyBr_i	number of cc $\mathrm{particle_i}$s (decay branches)
	2) iDcyBrCcP_i_j	index of decay branch of the $\mathrm{j^{th}}$ cc $\mathrm{particle_i}$
	2) nAllPDcyBr_i	number of all $\mathrm{particle_i}$s (decay branches)
Production branches of particles	iCcPProdBr_i	$\mathrm{index_{cc}}$ of $\mathrm{particle_i}$
	1) iCcProdBrP_i_j	$\mathrm{index_{cc}}$ of production branch of the $\mathrm{j^{th}}$ $\mathrm{particle_i}$
	2) nCcPProdBr_i	number of cc $\mathrm{particle_i}$s (production branches)
	2) iProdBrCcP_i_j	index of production branch of the $\mathrm{j^{th}}$ cc $\mathrm{particle_i}$
	2) nAllPProdBr_i	number of all $\mathrm{particle_i}$s (production branches)
Mothers of particles	iCcPMoth_i	$\mathrm{index_{cc}}$ of $\mathrm{particle_i}$
	1) iCcMothP_i_j	$\mathrm{index_{cc}}$ of mother of the $\mathrm{j^{th}}$ $\mathrm{particle_i}$
	2) nCcPMoth_i	number of cc $\mathrm{particle_i}$s (mothers)
	2) PDGMothCcP_i_j	PDG code of mother of the $\mathrm{j^{th}}$ cc $\mathrm{particle_i}$
	2) nAllPMoth_i	number of all $\mathrm{particle_i}$s (mothers)
Cascade decay branches of particles	iCcPCascDcyBr_i	$\mathrm{index_{cc}}$ of $\mathrm{particle_i}$
	1) iCcCascDcyBrP_i_j	$\mathrm{index_{cc}}$ of cascade decay branch of the $\mathrm{j^{th}}$ $\mathrm{particle_i}$
	2) nCcPCascDcyBr_i	number of cc $\mathrm{particle_i}$s (cascade decay branches)
	2) iCascDcyBrCcP_i_j	index of cascade decay branch of the $\mathrm{j^{th}}$ cc $\mathrm{particle_i}$
	2) nAllPCascDcyBr_i	number of all $\mathrm{particle_i}$s (cascade decay branches)
Decay final states of particles	iCcPDcyFSt_i	$\mathrm{index_{cc}}$ of $\mathrm{particle_i}$
	1) iCcDcyFStP_i_j	$\mathrm{index_{cc}}$ of decay final state of the $\mathrm{j^{th}}$ $\mathrm{particle_i}$
	2) nCcPDcyFSt_i	number of cc $\mathrm{particle_i}$s (decay final states)
	2) iDcyFStCcP_i_j	index of decay final state of the $\mathrm{j^{th}}$ cc $\mathrm{particle_i}$
	2) nAllPDcyFSt_i	number of all $\mathrm{particle_i}$s (decay final states)
Inclusive decay branches	iCcIncDcyBr_i	$\mathrm{index_{cc}}$ of inclusive decay $\mathrm{branch_i}$
	1) iCcDcyBrIncDcyBr_i_j	$\mathrm{index_{cc}}$ of decay branch of the $\mathrm{j^{th}}$ inclusive decay $\mathrm{branch_i}$
	2) nCcIncDcyBr_i	number of cc inclusive decay $\mathrm{branch_i}$es
	2) iDcyBrCcIncDcyBr_i_j	index of decay branch of the $\mathrm{j^{th}}$ cc inclusive decay $\mathrm{branch_i}$
	2) nAllIncDcyBr_i	number of all inclusive decay $\mathrm{branch_i}$es
IRA decay branches	iCcIRADcyBr_i	$\mathrm{index_{cc}}$ of IRA decay $\mathrm{branch_i}$
	1) iCcDcyBrIRADcyBr_i_j	$\mathrm{index_{cc}}$ of decay branch of the $\mathrm{j^{th}}$ IRA decay $\mathrm{branch_i}$
	2) nCcIRADcyBr_i	number of cc IRA decay $\mathrm{branch_i}$es
	2) iDcyBrCcIRADcyBr_i_j	index of decay branch of the $\mathrm{j^{th}}$ cc IRA decay $\mathrm{branch_i}$
	2) nAllIRADcyBr_i	number of all IRA decay $\mathrm{branch_i}$es

Table 24: Topology tags related to charge conjugation involved in each kind of signal identification. For the latter six kinds of signal identification, the topology tags in the *) groups are only designed for the non-self-charge-conjugate particles and decay branches. The acronyms "cc" and index$_{\text{cc}}$ are short for "charge conjugate" and "charge conjugate index", respectively.

Signal identification kind	Topology tag	Interpretation
Decay trees	iCcSigDcyTr	index$_{\text{cc}}$ of signal decay tree
Decay initial-final states	iCcSigDcyIFSts	index$_{\text{cc}}$ of signal decay initial-final states
Particles	iCcSigP_i	index$_{\text{cc}}$ of signal particle$_{\text{i}}$
	*) nCcSigP_i	number of cc signal particle$_{\text{i}}$s
	*) nAllSigP_i	number of all signal particle$_{\text{i}}$s
Decay branches	iCcSigDcyBr_i	index$_{\text{cc}}$ of signal decay branch$_{\text{i}}$
	*) nCcSigDcyBr_i	number of cc signal decay branch$_{\text{i}}$es
	*) nAllSigDcyBr_i	number of all signal decay branch$_{\text{i}}$es
Cascade decay branches	iCcSigCascDcyBr_i	index$_{\text{cc}}$ of signal cascade decay branch$_{\text{i}}$
	*) nCcSigCascDcyBr_i	number of cc signal cascade decay branch$_{\text{i}}$es
	*) nAllSigCascDcyBr_i	number of all signal cascade decay branch$_{\text{i}}$es
Inclusive decay branches	iCcSigIncDcyBr_i	index$_{\text{cc}}$ of signal inclusive decay branch$_{\text{i}}$
	*) nCcSigIncDcyBr_i	number of cc signal inclusive decay branch$_{\text{i}}$es
	*) nAllSigIncDcyBr_i	number of all signal inclusive decay branch$_{\text{i}}$es
Inclusive cascade decay branches	iCcSigIncCascDcyBr_i	index$_{\text{cc}}$ of signal inclusive cascade decay branch$_{\text{i}}$
	*) nCcSigIncCascDcyBr_i	number of cc signal inclusive cascade decay branch$_{\text{i}}$es
	*) nAllSigIncCascDcyBr_i	number of all signal inclusive cascade decay branch$_{\text{i}}$es
IRA decay branches	iCcSigIRADcyBr_i	index$_{\text{cc}}$ of signal IRA decay branch$_{\text{i}}$
	*) nCcSigIRADcyBr_i	number of cc signal IRA decay branch$_{\text{i}}$es
	*) nAllSigIRADcyBr_i	number of all signal IRA decay branch$_{\text{i}}$es

is the sum of "nEtr" and "nCcEtr". In addition to "iDcyTr", "iCcDcyTr" is also inserted in the output root files as a topology tag. It is short for charge conjugate index of decay tree. For self-charge-conjugate decay trees, it has the value 0; for non-self-charge-conjugate decay trees, it has the value 1 or -1: while 1 tags the decay trees listed in the topology maps, -1 indicates their charge conjugate decay trees. Whereas the values of "iDcyTr" for each decay tree and its charge conjugate decay tree are equal in order to indicate their sameness, the values of "iCcDcyTr" for them are opposite so as to reflect their difference.

As another example, we carry out the component analysis over the decay branches of D^{*+}. The resulting topology map of D^{*+} is displayed in Table 26. Compared with Table 4, two new columns are added to the table, and their headers "nCcCase" and "nAllCase" have the similar meanings as "nCcEtr" and "nAllEtr" in Table 25. For a specified particle, what we want to further record with topology tags are as follows: (1) whether it is self-charge-conjugate; (2) whether its decay branches are self-charge-conjugate, if it is self-charge-conjugate; (3) the number and the indices of the decay branches of its charge-conjugate particle, if it is not self-charge-conjugate. Hence, in addition to "nPDcyBr_i" and "iDcyBrP_i_j", the following topology tags are also inserted in the output root files: "iCcPDcyBr_i" for all specified particles; "iCcDcyBrP_i_j" for self-charge-conjugate particles only; and "nCcPDcyBr_i", "iDcyBrCcP_i_j", and "nAllPDcyBr_i" for non-self-charge-conjugate particles only. Here, "iCcPDcyBr_i" is short for charge conjugate index of the i$^{\text{th}}$ particle specified for its decay branches. For self-charge-conjugate particles, it has the value 0; for non-self-charge-conjugate particles, it has the value 1.

Table 25: Decay trees and their respective initial-final states.

rowNo	decay tree (decay initial-final states)	iDcyTr	nEtr	nCcEtr	nAllEtr	nCEtr
1	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}\gamma^F, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}, D^{*-} \rightarrow \pi^-\bar{D}^0,$ $D^{*+} \rightarrow \pi^+ D^0, \bar{D}^0 \rightarrow \pi^0\pi^-K^+, D^0 \rightarrow \pi^0\pi^+K^-$ $(\Upsilon(4S) \dashrightarrow e^+\nu_e\mu^-\bar{\nu}_\mu\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-K^+K^-\gamma^F)$	20870	3	0	3	3
2	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \mu^+\nu_\mu D^-, \bar{B}^0 \rightarrow e^-\bar{\nu}_e D^{*+}, D^- \rightarrow e^-\bar{\nu}_e\pi^-K^+,$ $D^{*+} \rightarrow \pi^+ D^0, D^0 \rightarrow \pi^0\pi^+K^-$ $(\Upsilon(4S) \dashrightarrow e^-e^-\bar{\nu}_e\bar{\nu}_e\mu^+\nu_\mu\pi^0\pi^+\pi^+\pi^-K^+K^-)$	3722	1	1	2	5
3	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow \pi^0\pi^+\pi^+\rho^-D^-, \bar{B}^0 \rightarrow \mu^-\bar{\nu}_\mu D^{*+}, \rho^- \rightarrow \pi^0\pi^-,$ $D^- \rightarrow \pi^-\pi^-K^+, D^{*+} \rightarrow \pi^+D^0, D^0 \rightarrow K^0_L\pi^+\pi^-$ $(\Upsilon(4S) \dashrightarrow \mu^-\bar{\nu}_\mu\pi^0\pi^0K^0_L\pi^+\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+)$	5295	2	0	2	7
4	$\Upsilon(4S) \rightarrow B^0\bar{B}^0, B^0 \rightarrow e^+\nu_e D^{*-}\gamma^F, \bar{B}^0 \rightarrow \pi^0\pi^+\pi^-\pi^-D^{*+},$ $D^{*-} \rightarrow \pi^0 D^-, D^{*+} \rightarrow \pi^+D^0, D^- \rightarrow \pi^-\pi^-K^+, D^0 \rightarrow \pi^0\pi^+K^-$ $(\Upsilon(4S) \dashrightarrow e^+\nu_e\pi^0\pi^0\pi^0\pi^+\pi^+\pi^+\pi^-\pi^-\pi^-\pi^-K^+K^-\gamma^F)$	10206	1	1	2	9
5	$\Upsilon(4S) \rightarrow B^0B^0, B^0 \rightarrow \mu^+\nu_\mu D^{*-}, B^0 \rightarrow \mu^+\nu_\mu D^{*-}, D^{*-} \rightarrow \pi^0D^-,$ $D^{*-} \rightarrow \pi^-\bar{D}^0, D^- \rightarrow \pi^0\pi^-K^0_S, \bar{D}^0 \rightarrow \pi^0\pi^-K^+, K^0_S \rightarrow \pi^+\pi^-$ $(\Upsilon(4S) \dashrightarrow \mu^+\mu^+\nu_\mu\nu_\mu\pi^0\pi^0\pi^0\pi^+\pi^-\pi^-\pi^-\pi^-K^+)$	11916	1	1	2	11
rest	$\Upsilon(4S) \rightarrow$ others (99969 in total) $(\Upsilon(4S) \dashrightarrow$ corresponding to others)	—	—	—	99989	100000

The topology tag “iCcDcyBrP_i_j” denotes charge conjugate index of decay branch of the j[th] instance of the i[th] particle. It is to “iDcyBrP_i_j” what “iCcDcyTr” is to “iDcyTr”. The topology tag “iDcyBrCcP_i_j” has the similar meaning as “iDcyBrP_i_j”, but it is designed for the charge conjugate particle of the i[th] particle. Particularly, it ranges from 0 (included) to the number of the categories of decay branches of the i[th] particle found in the sample (excluded). The topology tag “nCcPDcyBr_i” stands for the number of the charge conjugate i[th] particles (or their decay branches) found in each entry, and “nAllPDcyBr_i” is the sum of “nPDcyBr_i” and “nCcPDcyBr_i”.

Table 26: Decay branches of D^{*+}.

rowNo	decay branch of D^{*+}	iDcyBrP	nCase	nCcCase	nAllCase	nCCase
1	$D^{*+} \rightarrow \pi^+D^0$	0	31180	31291	62471	62471
2	$D^{*+} \rightarrow \pi^0D^+$	1	13978	14166	28144	90615
3	$D^{*+} \rightarrow D^+\gamma$	2	700	721	1421	92036
4	$D^{*+} \rightarrow \pi^+D^0\gamma^F$	3	28	36	64	92100
5	$D^{*+} \rightarrow \pi^0D^+\gamma$	4	0	1	1	92101

5.2.3. *Settings only on signal identification*

Normally, the signals specified in the signal identification functionality items are both tagged and counted by executing the program one time. In the case of a huge sample that will take a long time, it is a good idea to first tag the signals with multiple jobs each running on one machine, and then count the tagged signals together. One can make the program carry out the idea by setting the following item to “T” and “C” in the first and second steps, respectively. Here, “T” and “C” stand for tagging and counting, respectively.

```
% Analysis tasks for signal identifications (Three options: TC, T and C. Default: TC)
{
  T
}
```

By default, the signals set in the signal identification functionality items are listed in the output txt, tex, and pdf files in the sequence they are specified. In cases of plenty of signals, there is probably a need to sort them according to the number of cases found in the input samples. One can have the program do the sorting by inputting “Y” to the item below.

```
% Sort the signals in the topology maps related to signal identifications (Two options: Y and N. Default: N)
{
  Y
}
```

5.3. Settings on the output of the program

By default, decay objects (trees, initial-final states, and branches) are left-aligned in the output pdf files. If one likes it, he/she can request the program to center them by setting the following item to “Y”.

```
% Center decay objects in output pdf files (Two options: Y and N. Default: N)
{
  Y
}
```

As mentioned in Section 2.4, after the execution of the program, one or more root files will be output to save topology tags. By default, the program switches to a new output file whenever the size of the TTree object in memory exceeds 3 GB. In addition to this, the program provides an item to control the switch of output files by setting the maximum number of entries to be saved in a single output file. The following example shows the item with the maximum number set to 1 million.

```
% Maximum number of entries to be saved in a single output root file
{
  1000000
}
```

Besides, one can have the program generate one output file by one input file with the following item set to “Y”.

```
% One output root file by one input root file (Two options: Y and N. Default: N)
{
  Y
}
```

In default cases, flat TBranch objects are used to store topology tags in the output root files. This is necessary for the Belle II experiment, as array TBranch objects are not recommended to use in physics analyses in order to use other tools such as NumPy [11] and pandas [12]. However, since array TBranch objects are elegant and efficient in organizing and storing homogeneous data, sometimes it is better to use them than flat TBranch objects in other experiments, such as the BESIII experiment. One can make the program use array TBranch objects to store topology tags by inputting “Y” to the item below.

```
% Use array tbranches to store topology tags in output root files when possible (Two options: Y and N. Default: N)
{
  Y
}
```

By default, to facilitate the validation of topology analysis results, the input TBranch objects are copied to the output root files along with other TBranch objects for physics analyses. However, they often occupy too much disk space and are useless for following physics analyses. In the case of being flat, a massive amount of these TBranch objects also looks awkward. Thus, after the validation with a small sample, it would be better to remove these TBranch objects from the output root files. One can request the program to perform this removal operation before it terminates by setting the following item to “Y”.

```
% Remove the input tbranches from output root files (Two options: Y and N. Default: N)
{
  Y
}
```

In all of the previous examples, the program is applied to the inclusive MC samples in e^+e^- colliding experiments. Besides, the program can also be used in other types of high energy experiments, for example, the PANDA experiment [15], a $p\bar{p}$ annihilation experiment under construction at Darmstadt, Germany. On these occasions, we have to specify the right initial state particles with the following item to obtain the proper topology maps.

```
% Initial state particles (Default: e− e+)
{
  anti-p−    p+
}
```

With the setting, the default initial state e^+e^- is replaced by $p\bar{p}$ in Table 27.

Table 27: Decay trees and their respective initial-final states ($p\bar{p}$ annihilation).

rowNo	decay tree	decay final state	iDcyTr	nEtr	nCEtr
1	$p\bar{p} \to p\bar{p}$	$p\bar{p}$	1	232	232
2	$p\bar{p} \to \pi^+\pi^- p\bar{p}$	$\pi^+\pi^- p\bar{p}$	24	53	285
3	$p\bar{p} \to \pi^0 p\bar{p}$	$\pi^0 p\bar{p}$	5	35	320
4	$p\bar{p} \to \pi^0\pi^+\pi^- p\bar{p}$	$\pi^0\pi^+\pi^- p\bar{p}$	0	33	353
5	$p\bar{p} \to \pi^0\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-$	$\pi^0\pi^0\pi^0\pi^+\pi^+\pi^-\pi^-$	39	31	384
rest	$p\bar{p} \to$ others (184 in total)	corresponding to others	—	616	1000

6. Auxiliary facilities

This section introduces some auxiliary facilities for the use of the program, including a card file to preset frequently used items and two commands implemented in tex source files. Different from that presented in the previous four sections, the content presented in this section is not the essential part of the program. However, with these auxiliary facilities, we can make the program do our jobs better and quicker on some occasions.

6.1. The underlying card file

A card file, namely “underlying_topoana.card” under the directory “share”, to preset frequently used items is developed to assist the card file specified by the first argument of the command “topoana.exe”. Here, we refer to the former and latter card files as underlying and primary, respectively. In general, the primary card file is sufficient to set items for the execution of the program. However, considering some items are frequently used with constant inputs by a user or a group of users, it is better to move the items from the primary card file to the underlying card file, in order to make the primary card file more concise and make us more focused on the items specially set for the dedicated topology analysis.

One can decide whether to set an item in the underlying card file according to his/her own needs. Here, we introduce some frequently used items that are suitable to be put in the underlying card file as follows. As mentioned in Section 2.3, the items related to the storage type and TBranches names of the input data are usually fixed for a user or a group of users. Thus, it is quite appropriate to move them to the underlying card file. We have to process charge conjugation particles and decays together in many physics studies. In such studies, it is also a good practice to put the item on charge conjugation in the underlying card file.

The program first reads the items in the underlying card file and then reads those in the primary card file. The items set in the underlying card file can be reset in the primary card file. In such a case, the inputs in the underlying card file will be replaced by their counterparts in the primary card file.

6.2. Commands implemented in tex source files

The output pdf files can be checked after the execution of the program. If their styles are not to our taste, we can edit the corresponding tex source files to get the desired styles, according to the regular LaTeX rules. Besides the rules, two commands are implemented in the tex source files to help us edit the files quickly and easily for two common desired styles.

By default, topology tags are listed along with topology maps in the output txt, tex, and pdf files. However, only the topology maps are needed on some occasions, especially in presentations. In such cases, one can suppress the topology tags in the output tex and pdf files by simply changing the definition of the cmtTopoTags command from the nominal one

```
\newcommand{\topoTags}[1]{#1}
```

to the alternative one

```
\newcommand{\topoTags}[1]{}
```

in the preamble of the text source files. Here, "#1" is the formal parameter of the string for the topology tags. With the nominal definition, "\topoTags{#1}" returns the string exactly, while with the alternative definition it only returns an empty string. That is why the definition below is able to suppress the topology tags.

After the revision of the tex source files, one can re-compile them with the pdflatex command. Usually, the pdflatex command has to be executed two or three times for a fully compiled pdf file, and many undesired files in other formats are generated during the compilation. To execute the pdflatex command and remove the undesired files at one stroke, we develop a bash script, namely "getPdfFromTex.sh" under the directory "utilities". The script should be executed with the following command line: getPdfFlFromTexFl.sh texFileName. Compiling the tex source files with the script is recommended.

7. Summary

We develop a program, namely TopoAna, with C++, ROOT, and LaTeX for the topology analysis of inclusive MC samples in high energy physics experiments. This user guide provides a detailed description of the program, including a basic introduction to it, two sorts of its functionalities — component analysis and signal identification, and some common settings and auxiliary facilities for its execution. The program has rich functionalities and aims to solve all kinds of topology analysis tasks. Meanwhile, it has a high processing rate and is easy to use. These features make the program a power tool for analysts to investigate the signals and backgrounds involved in their works.

Since it does not rely on any specific software frameworks, the program applies to many high energy physics experiments. Up to now, it has been put into use in three experiments at e^+e^- colliders: the BESIII, Belle, and Belle II experiments. Besides these experiments, it can also be used in other types of experiments, such as the PANDA experiment. In addition, the program is also applicable to the future e^+e^- colliding experiments under research and development, such as the circular electron positron collider (CEPC) [16, 17] experiment in China, the super Charm-τ factory (SCTF) experiment [18] in Russia, and the super τ-Charm factory (STCF) experiment [19] in China. These experiments offer a wide range of potential uses of the program. With more user needs coming out in the future, we will further extend and perfect it to make it more powerful and well-rounded.

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