

Representation learning

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Bucharest CV – Reading group #3

Overview

Introduction to representation learning

Uses of representations

Types of representations learnt by deep learning

Learning good representations

Introduction

- ▶ Learning representations: the distinctive feature of deep learning

Introduction

Numeral systems

0123456789

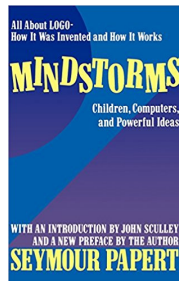
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I II III IV V VI VII VIII IX X

- ▶ Learning representations: the distinctive feature of deep learning
- ▶ Representations for humans:
 - ▶ Roman versus Arabic numerals

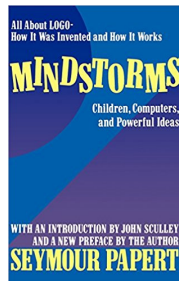
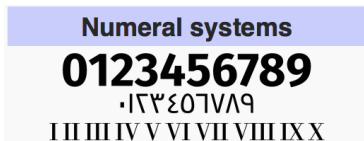
Introduction

Numeral systems									
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	٠	١	٢	٣	٤	٥	٦	٧	٨٩
I	II	III	IV	V	VI	VII	VIII	IX	X



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- ▶ Representations for humans:
 - ▶ Roman versus Arabic numerals
 - ▶ Models to assimilate knowledge

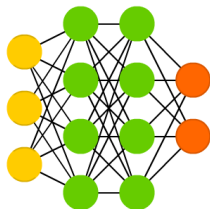
Introduction



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 - ▶ Models to assimilate knowledge
 - ▶ Ability to learn from very few examples

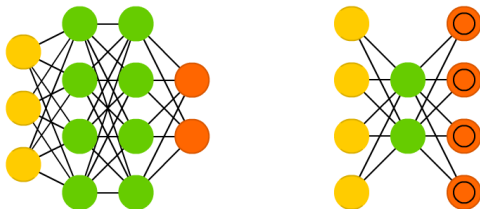
Examples of representations in neural networks

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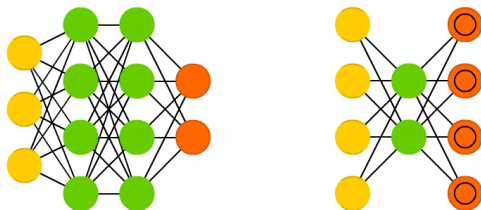
- ▶ Supervised learning – implicit representations

Examples of representations in neural networks



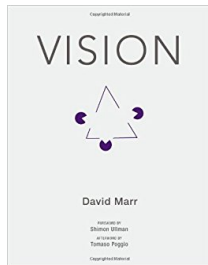
- ▶ Supervised learning – implicit representations
- ▶ Unsupervised learning – explicit representations

Examples of representations in neural networks



- ▶ Supervised learning – implicit representations
- ▶ Unsupervised learning – explicit representations
- ▶ Representations: high-level, many-to-one mapping of the input

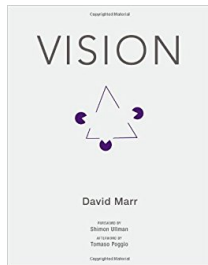
Representation learning: A definition



A representation is a formal system which makes explicit certain entities or types of information, together with a specification of how the system does this.

(Marr, 1982)

Representation learning: A definition



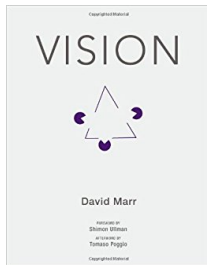
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- representations are operated by an algorithm
- set of symbols with rules of putting them together

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- ▶ *formal*
 - ▶ representations are operated by an algorithm
 - ▶ set of symbols with rules of putting them together
 - ▶ *makes explicit certain types of information*
 - ▶ usually a trade-off
 - ▶ representations are tied to a given task

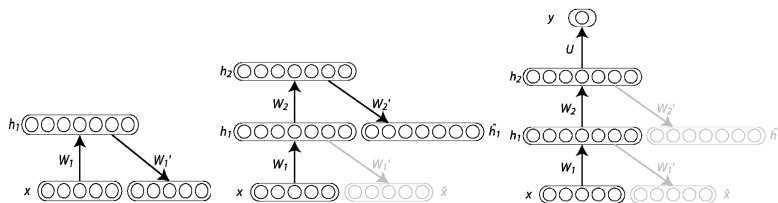
Introduction to representation learning

Uses of representations

Types of representations learnt by deep learning

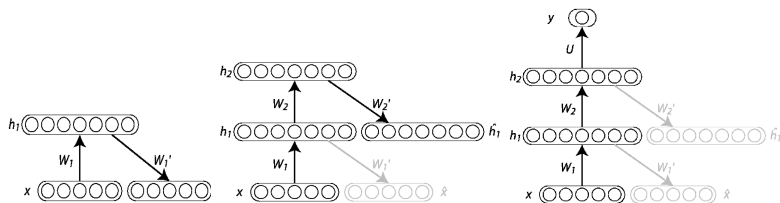
Learning good representations

Uses of representations: Unsupervised pre-training



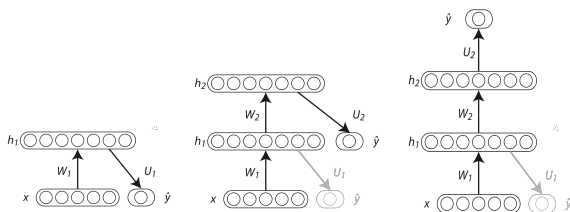
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Uses of representations: Unsupervised pre-training



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- ▶ Not that popular nowadays (except for NLP)

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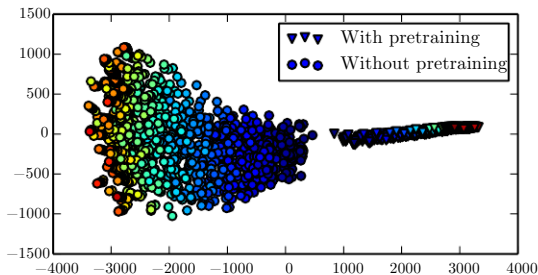
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2. Initial parameters help optimization

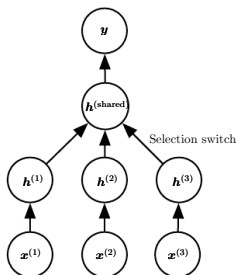
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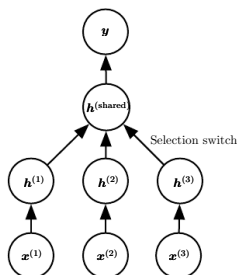
- Pre-training reduces the variance of the estimation process

More uses of representations



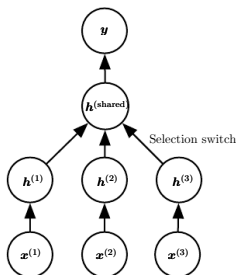
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 - ▶ Variations in one task are relevant with variations in the other one
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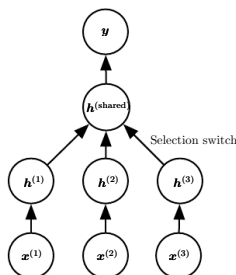
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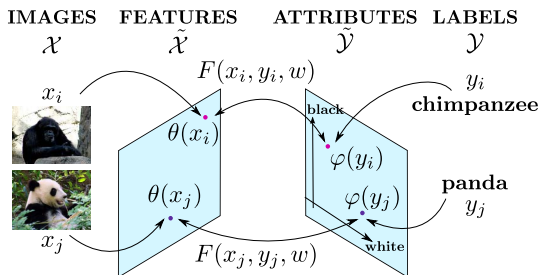
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 - ▶ Zero-shot learning: output representations to link classes

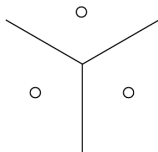
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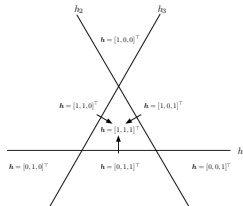
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Distributed representations



Non-distributed representations

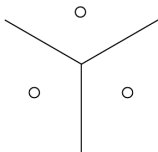
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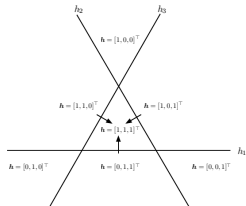
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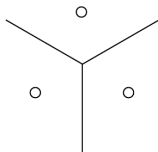
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Distribution representations

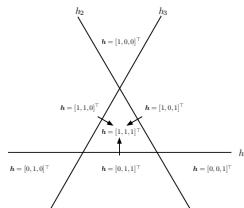
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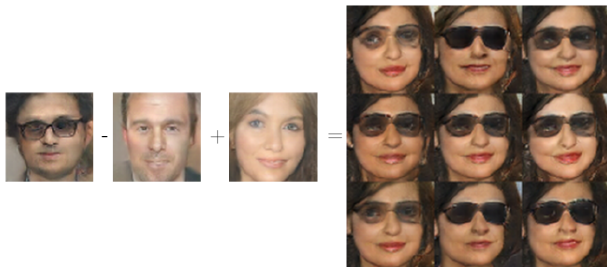
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Distributed representations



- ▶ Directions in representations space capture factors of variations
- ▶ Allows generalization to new configurations of features

Hierarchical representations

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- ▶ Deep learning offers statistical efficiency: some functions compactly represented with k layers may require exponential size with $k - 1$ layers
- ▶ Intuitively hierarchal representations allow reuse

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 - ▶ Shared factors across tasks
 - ▶ Sparsity: not all features are relevant to describing the input

Further resources

- ▶ Y. Bengio's talks and tutorials
<http://www.iro.umontreal.ca/~bengioy/talks/deep-learning-gss2012.html>
- ▶ Y. Bengio. Learning Deep Architectures for AI (Bengio, 2009)
- ▶ Y. Bengio. Representation learning: A review and new perspectives (Bengio et al., 2013)
- ▶ Representation Learning workshop (27/03 – 31/03, 2017)
<https://simons.berkeley.edu/workshops/schedule/3750>

References

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