

System Identification:-



$$y = \frac{ku}{s+a}$$

$$\Rightarrow \dot{y} + ay = ku$$

$$\Rightarrow \underbrace{\frac{y(t+1) - y(t)}{\Delta t}}_{\text{Euler's approximation}} = -ay + ku$$

$$\Rightarrow y(t+1) = \underbrace{(1 - a\Delta t)}_{\tilde{a}} y + \underbrace{k\Delta t}_{\tilde{b}} u$$

$$\underbrace{\begin{bmatrix} y & u \end{bmatrix}}_{\mathbf{Z}} \begin{bmatrix} \tilde{a} \\ \tilde{b} \end{bmatrix} = \underbrace{\text{shifted } y}_{y(t+1)}$$

$$\text{Use least square: } \begin{bmatrix} \tilde{a} \\ \tilde{b} \end{bmatrix} = \mathbf{Z} \backslash y(t+1)$$