

# **2D Feature Model - Mechanisms and Algorithms**

**Langmuir Project Documents**

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# Contents

<b>Introduction</b>	<b>3</b>
<b>Feature Model 2D - Code Structure</b>	<b>4</b>
<b>Feature Model 2D - Mesh Construction</b>	<b>6</b>
<b>Feature Model 2D - Particle</b>	<b>8</b>
<b>Feature Model 2D - Particle Tracing</b>	<b>10</b>
<b>Feature Model 2D - Reflection</b>	<b>16</b>
<b>Feature Model 2D - Drop</b>	<b>22</b>

# **Introduction**

This document introduces and discusses the mechanisms and algorithms for 2-D feature model.

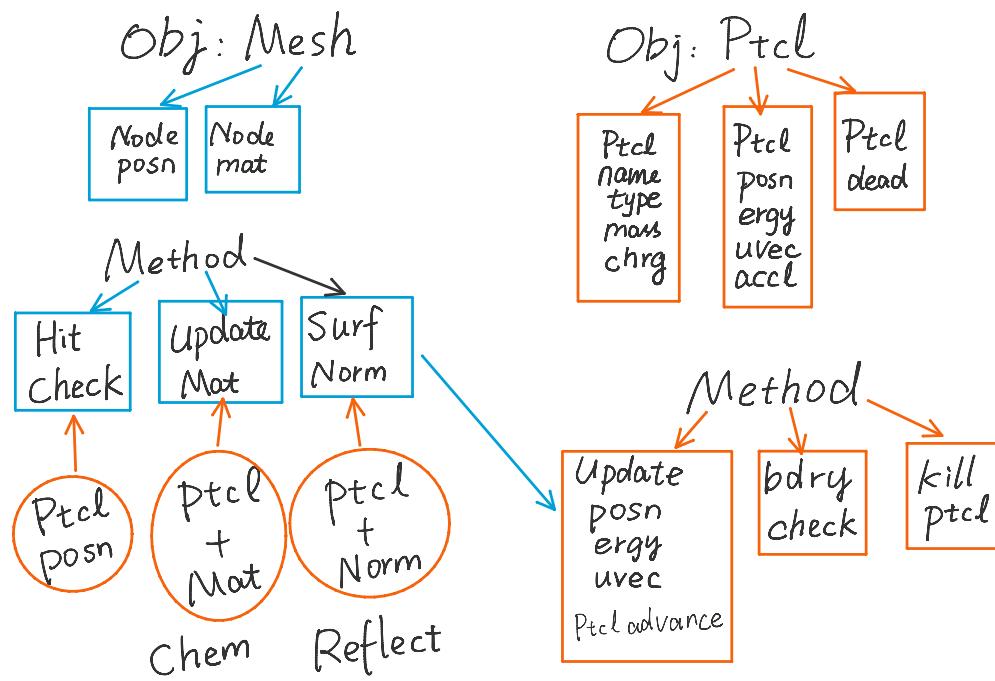
## **Feature Model 2D - Code Strucure**

The feature model is designed following by an objective oriented programming. Four major objects are created: 1. Mesh 2. Particle 3. Reflect 4. React

# Code Structure

Wednesday, September 2, 2020 3:25 PM

# CODE STRUCTURE



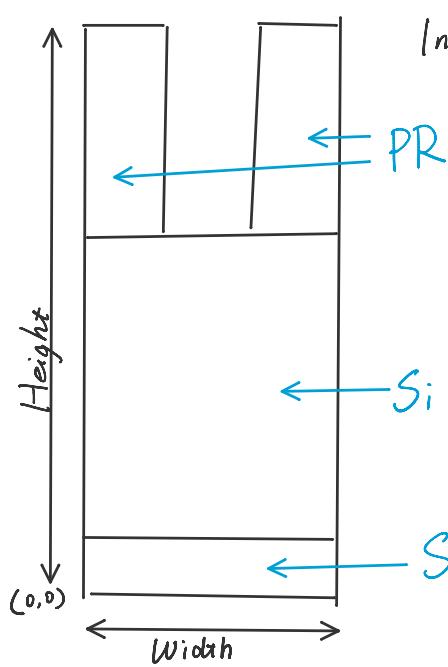
**CHEM** will be designed later  
**REFLECT**

## **Feature Model 2D - Mesh Construction**

The mesh is created by using voxel/cell structure. The voxel or cell center is defined and each represented a rectangular/square shape.

# Mesh construction

Sunday, September 13, 2020 9:44 AM



Input Mesh file :

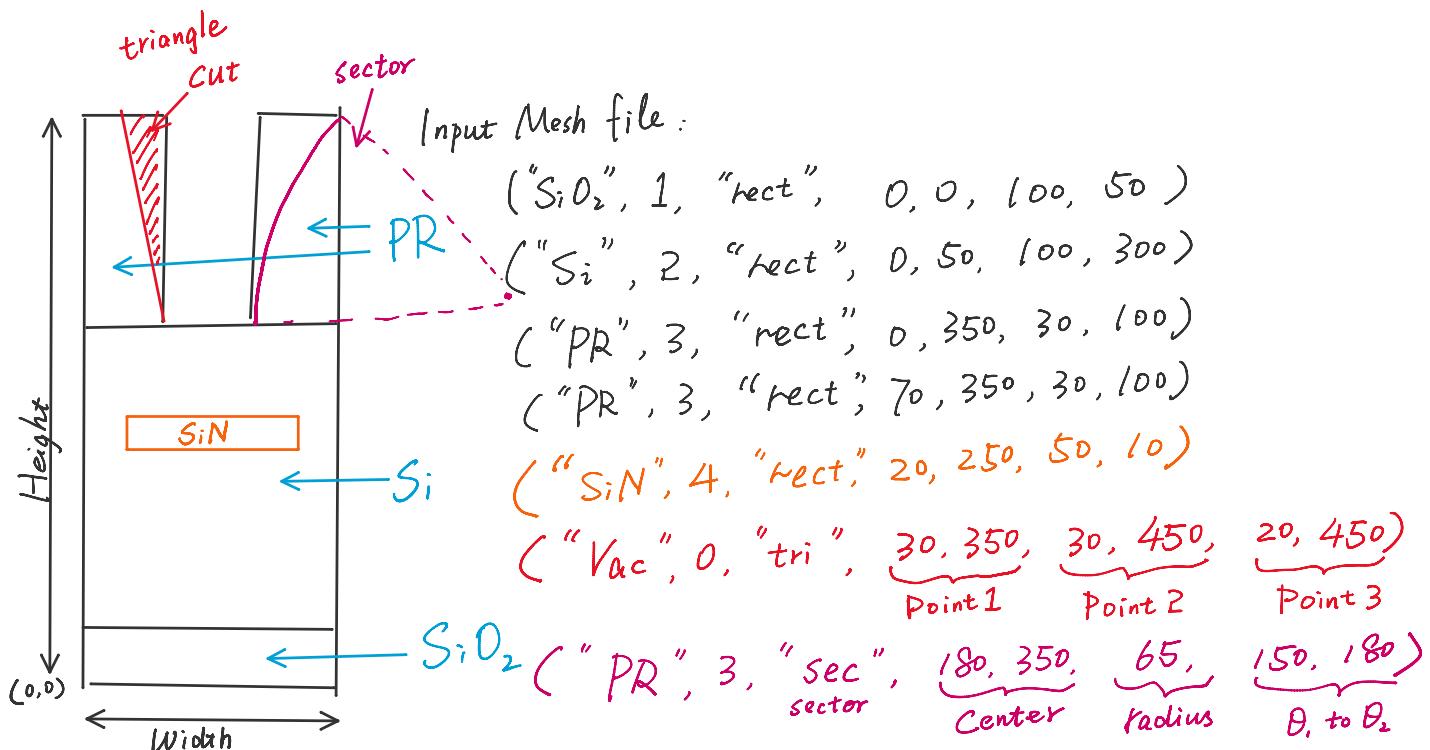
( "SiO<sub>2</sub>", 1, "rect", 0, 0, 100, 50 )

( "Si", 2, "rect", 0, 50, 100, 300 )

( "PR", 3, "rect", 0, 350, 30, 100 )

( "PR", 3, "rect", 70, 350, 30, 100 )

- i) Utilize basic shapes to construct complex feature/geometry/mesh
- ii) latter block/shape overwrites former
- iii) "Vac" default as "0", used as "CUT"



Input Mesh file :

( "SiO<sub>2</sub>", 1, "rect", 0, 0, 100, 50 )

( "Si", 2, "rect", 0, 50, 100, 300 )

( "PR", 3, "rect", 0, 350, 30, 100 )

( "PR", 3, "rect", 70, 350, 30, 100 )

( "SiN", 4, "rect", 20, 250, 50, 10 )

( "Vac", 0, "tri", 30, 350, 30, 450, 20, 450 )

Point 1 Point 2 Point 3

( "PR", 3, "sec", 180, 350, 65, 150, 180 )

Center Radius θ<sub>1</sub> to θ<sub>2</sub>

## **Feature Model 2D - Particle**

Particles are created as an object, containing information consisting of constants and variables.

# Particle

Sunday, September 13, 2020 10:21 AM

Particle	Name	Type	Mass(AMU)	Charge		Position	Energy(eV)	Direction	Dead
Arp	'Ar+'	Ion	40	+1		(0,0)	100	(-sin( $\alpha$ ), cos( $\alpha$ ))	0
O	'O'	Radical	16	0		var	var	var	var
E	'E'	Electron		-1		var	var	var	var

Constants

Variables

The Particle position is computed to as the particle advances

Position\_2 = position\_1 + speed \* direction \* dt

Step = Speed \* dt is fixed regardless of speed

The direction is a unit vector

The speed is not used. Instead the energy is used for reflection and reaction.

When reflection occurs, the direction and energy are updated

‘Dead’ is a tag to indicate whether the particle is alive or not

Dead = 0, continue to track the particle

Dead = 1, stop tracking the particle

Once a particle is created, the memory of the particle is created and I will never be erased.

Two method:

1. Only a single particle memory is created, A new particle will use the same memory with updating all the constants and the variables
2. Since there are only a limit number of kinds of particles, multiple particle memories are created with updating only the variables

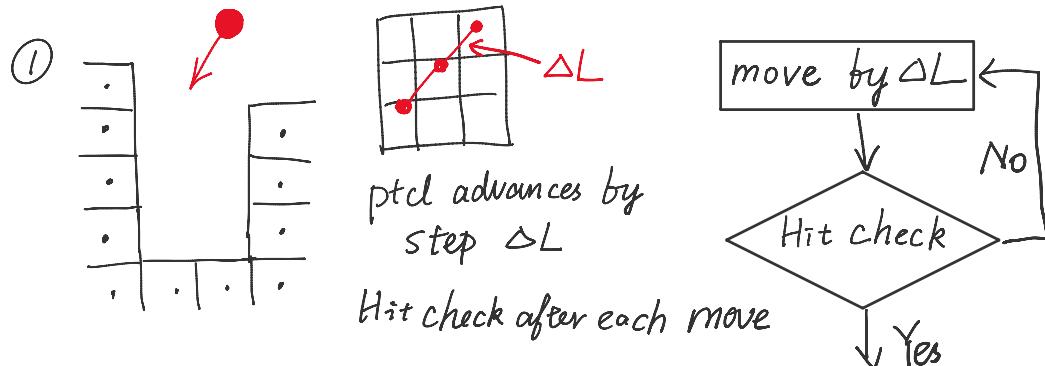
## **Feature Model 2D - Particle Tracing**

Particles are either moved by step advancing or tracked by ray tracing.  
Boundary conditions are set to be either periodic or reflective.

# Step Advance

Wednesday, September 2, 2020 3:18 PM

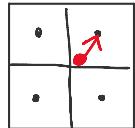
## STPE ADVANCE INFINITE SMALL PTCL



Computational Load depends on Mesh Domain

ptcl is always mapped to grids

Vac/Mat. ptcl  $(x_i, y_i)$

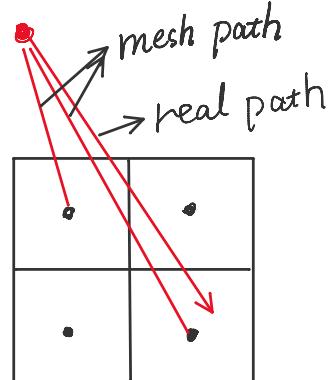


$$i = \text{round} \left( \frac{x_i}{\Delta x} \right)$$

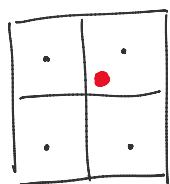
$$j = \text{round} \left( \frac{y_i}{\Delta y} \right)$$

ptcl hits cell  $(i, j)$

check cell to be Vac. or Mat.

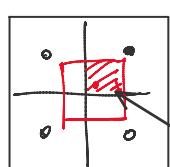


Two views:



i) assume the ptcl is infinite small

ptcl hits the cell when it enters inside a cell



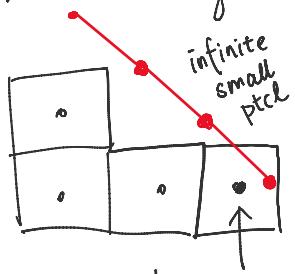
ii) assume ptcl has a volume



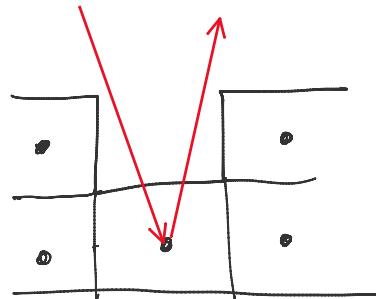
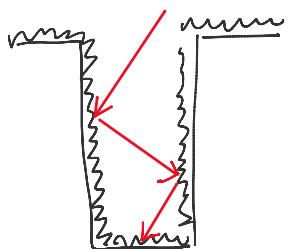
ptcl hits the cell with max volume overlap

Max overlap

Possible questions:



good  
for  
rough  
surf

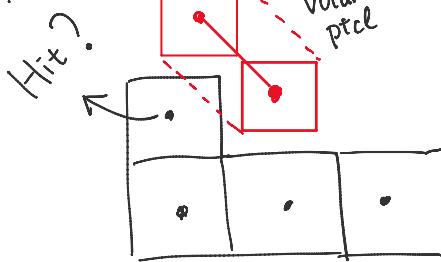
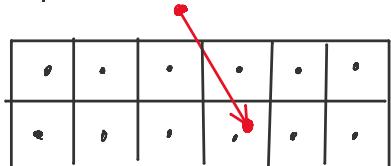


good  
for  
penetrating

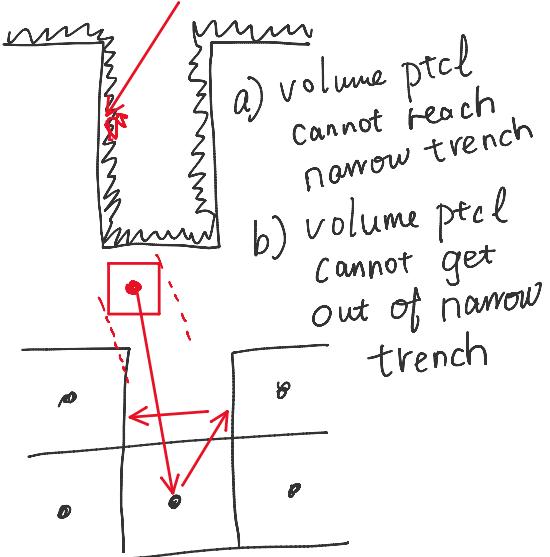
$$\Delta L = \Delta L(\varepsilon)$$

when use larger  $\Delta L$   
e.g.  $\Delta L \approx 2 \Delta x$

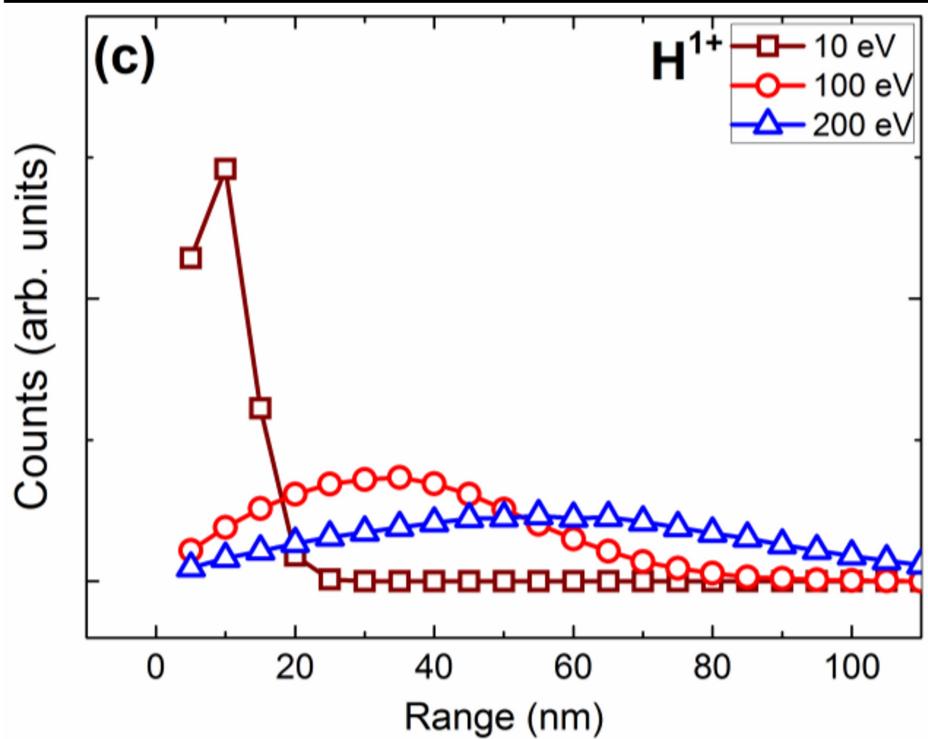
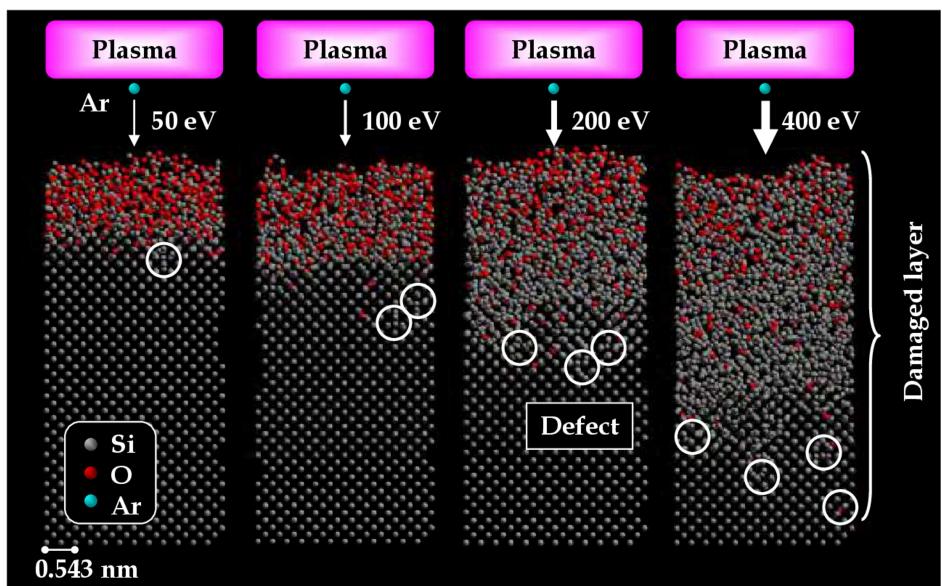
ptcl able to hit underlying layer



Trapped  
in rough  
surf



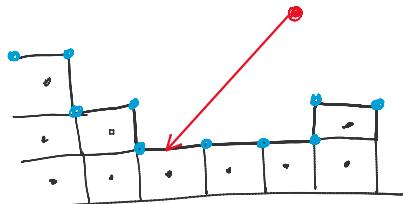
No need  
concept of  
SURF



# Ray Tracing

Wednesday, September 2, 2020 3:19 PM

## RAY TRACING



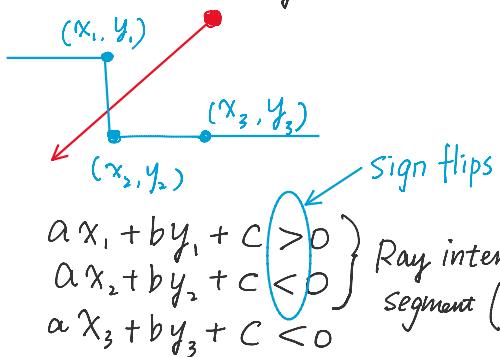
- a) construct the surf  
surf nodes  
surf segments

surf can be  
parallelled!

- b) sort the surf nodes

GPU 2D  
in para

c) line:  $ax + by + c = 0$



- d) map segment  $\rightarrow$  Node/cell  $(i, j)$

- e) Ray intersects with cell  $(i, j)$

Computational load depends on  
the surf area

?

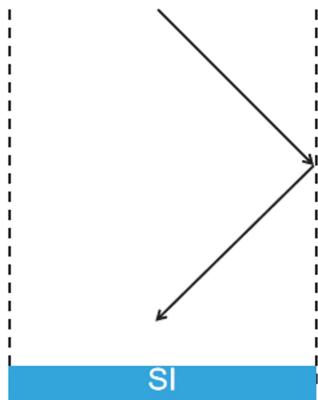
In 3D, computational load will be doubled

Eventually, all particles have to be mapped to meshgrid nodes. Surface intersection is a way of mapping. **How to take advantage of RT?**

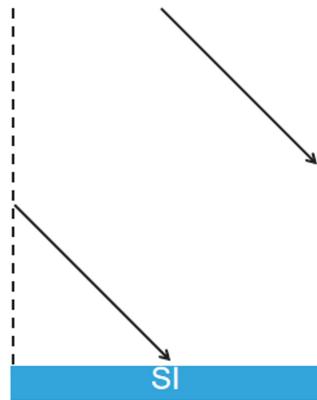


# Boundary Condition

Sunday, September 13, 2020 8:15 PM



Reflective B.C.



Periodical B.C.

## **Feature Model 2D - Reflection**

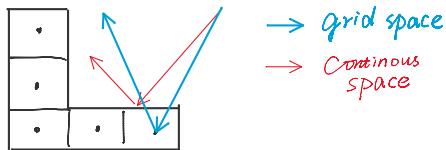
When a particle hits on a surface, there is a chance that the particle reflects from the surface.

# Reflection

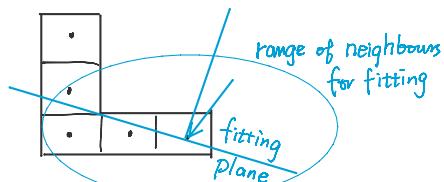
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## REFLECTION

All Reflections occur on Nodes instead of SURF



Find the reflecting surf  
Cell surf is only horizontal or vertical  
On nodes, surf is determined  
by plane fitting



assume the fitting plane is  
 $Ax + By + C = 0$   
for neighbours  $(x_i, y_i)$   
the distance from  $(x_i, y_i)$  to plane

$$Ax_i + By_i + C = 0$$

$$\text{dist} = \frac{|Ax_i + By_i + C|}{\sqrt{A^2 + B^2}}$$

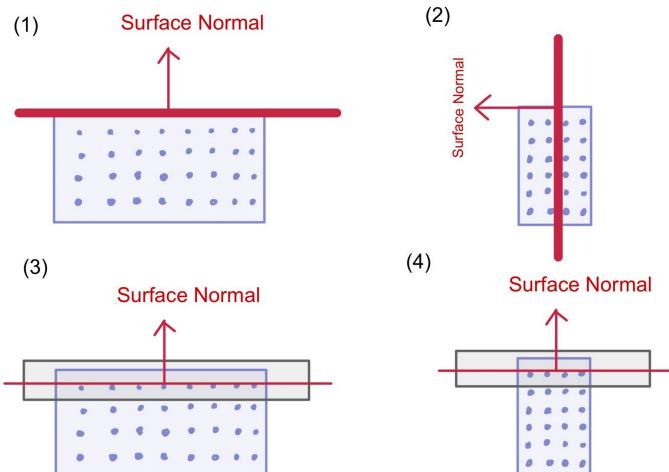
minimize total dist

$$D = \sum_i \text{dist}(x_i, y_i)$$

Usually, a simpler form is used

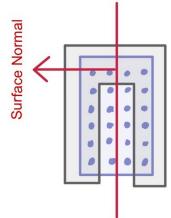
$$Q = \sum_i (Ax_i + By_i + C)^2$$

This sum can be only fitted on nodes  
Once the fitting plane is determined



1. It is better to use surface nodes than volume nodes.

2. The radius has an impact of surface normal calculation.



This sum can be only fitted on nodes  
Once the fitting plane is determined  
surf norm  $\hat{n}$  is chosen from  
Mat to Vac

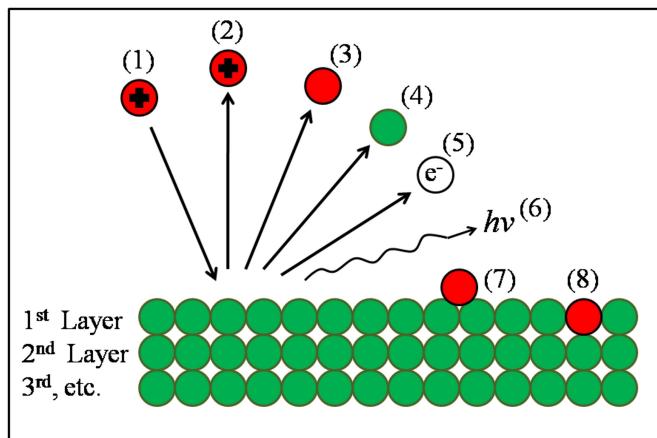
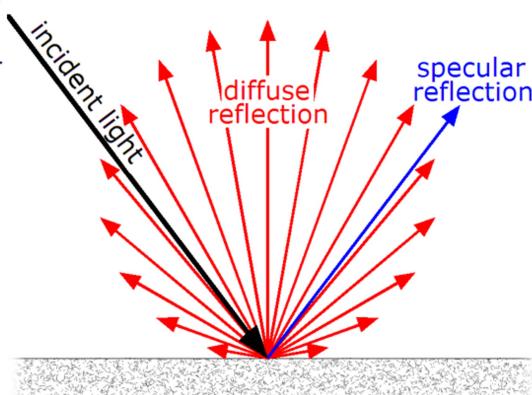
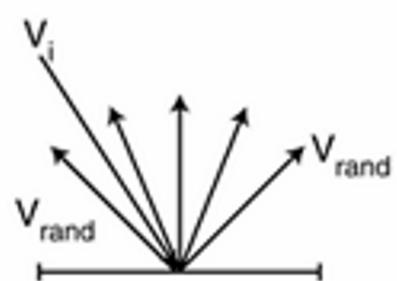
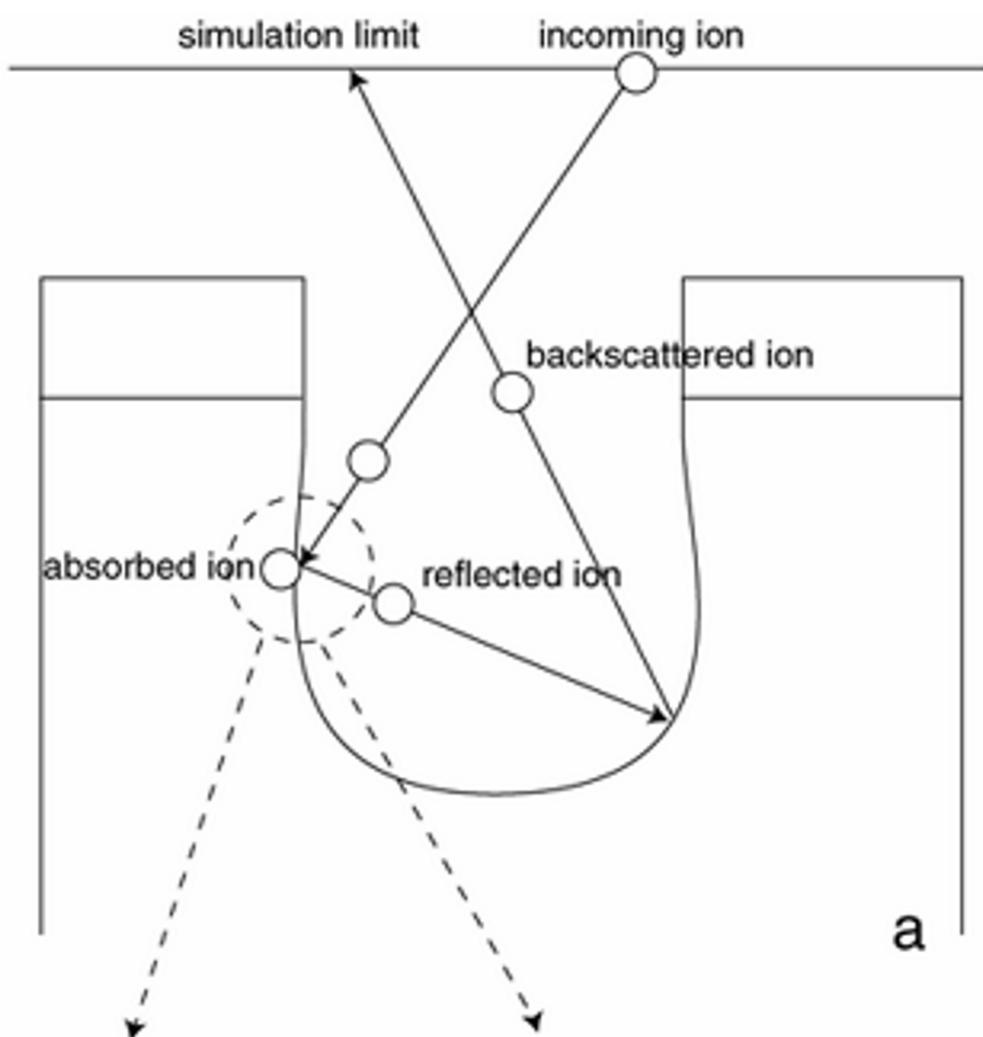


Diagram of various ion-surface interactions (non-exhaustive). (1) Incoming ion; (2) Scattering; (3) Neutralization and scattering; (4) Sputtering or recoiling; (5) Electron emission; (6) Photon emission; (7) Adsorption; (8) Displacement.

## DIFFUSE REFLECTION

- Neutral particles with thermal, or near thermal ( $< 1 \text{ eV}$ ) energies reflect or re-emit from surfaces diffusively following a cosine angular distribution.
- This occurs because each particle is in thermal equilibrium with the surface, allowing them to briefly physisorb to the surface, before being re-emitted into the gas by vibrational processes in the solid, such as phonon scattering.
- The emitting probability density function depends on the particle and surface condition.





## ENERGY LOSS DURING THE REFLECTION

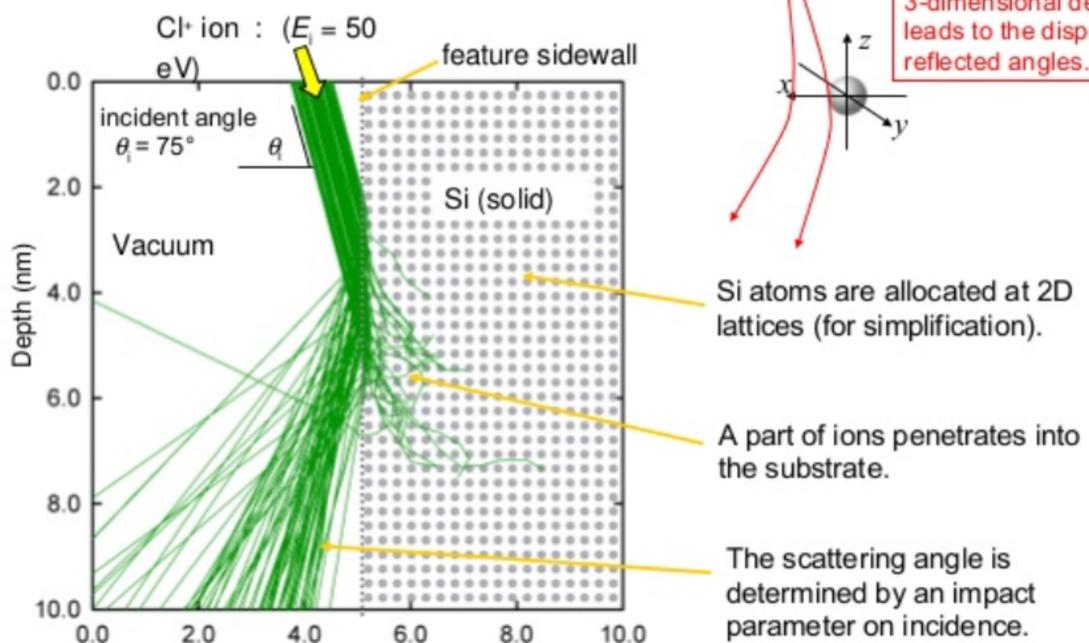
- Particles lose energy during the reflection as a function of initial energy and incident angle.

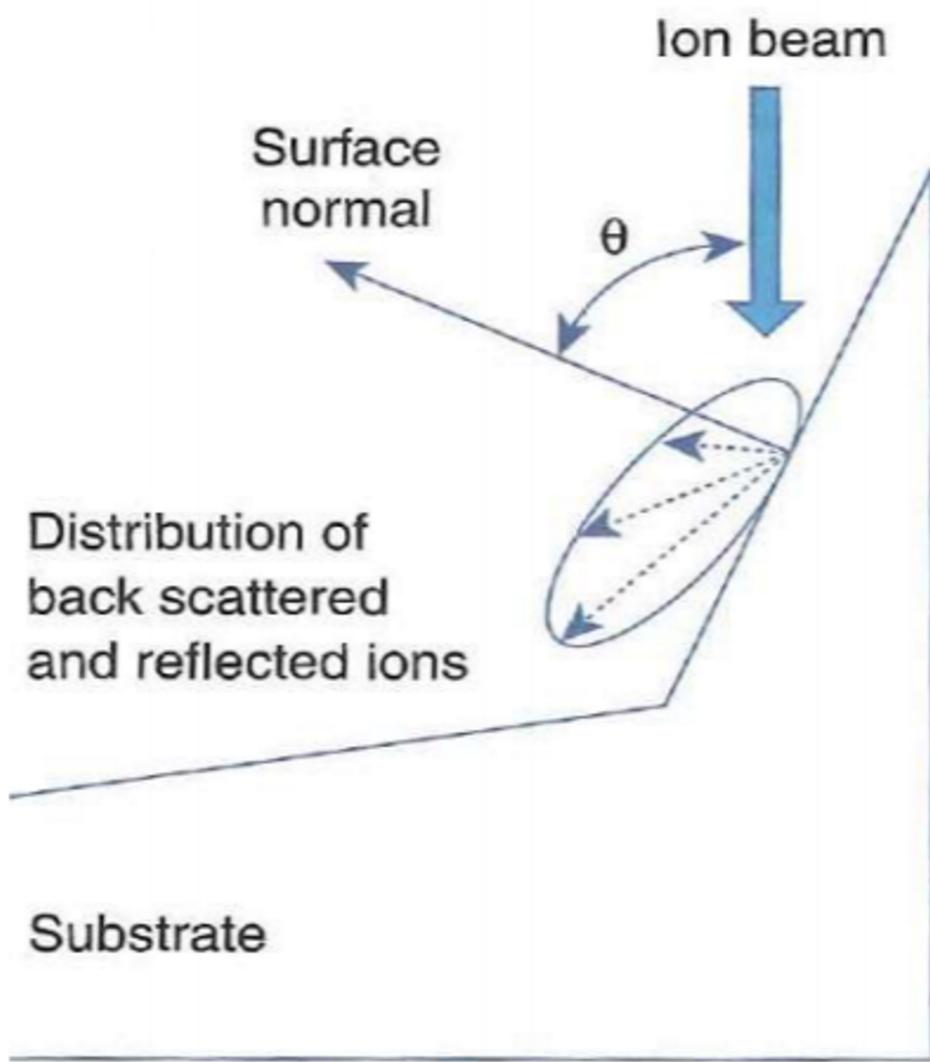
$$\varepsilon_f = \gamma_0 f(\theta) f(\varepsilon_i) \varepsilon_i$$

$$f(\varepsilon) = \begin{cases} 0 & \text{if } \varepsilon < \varepsilon_0 \\ \frac{\varepsilon - \varepsilon_0}{\varepsilon_s - \varepsilon_0} & \text{if } \varepsilon_0 \leq \varepsilon \leq \varepsilon_s \\ 1 & \text{if } \varepsilon > \varepsilon_s \end{cases} \quad f(\theta) = \begin{cases} 0 & \text{if } \theta < \theta_0 \\ \frac{\theta - \theta_0}{\theta_0} & \text{if } \theta > \theta_0 \end{cases}$$

for example,  $\gamma_0 = 0.85$ ,  $\varepsilon_0 = 0$  eV,  $\varepsilon_s = 50$  eV and  $\theta_0 = 30^\circ$

### Sample trajectories of reflected ions





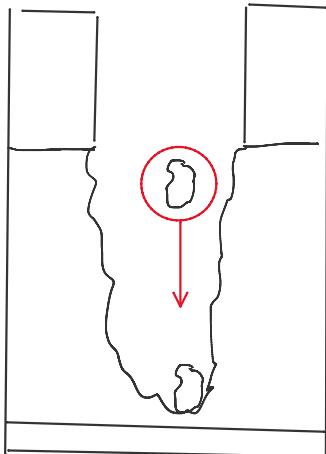
Ion beam gets deflected by tilted faces \*

## **Feature Model 2D - Drop**

After the mesh is updated, a drop algorithm is called to fix the floating cells/clusters.

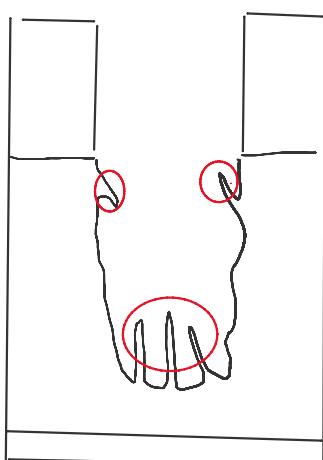
## Drop

Sunday, September 13, 2020 6:50 PM



When a cluster is detached/separated from the main feature, the cluster will drop to bottom and reconnect/deposit on surface.

Search for separate shape in topology is a classical problem.



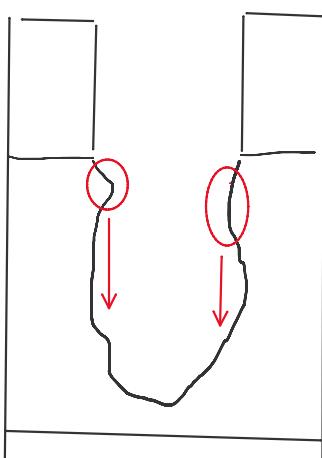
Occasionally, some branching shapes occur due to the statistical phenomenon. Mechanically, they could fall due to gravity.

Supporting/connecting force

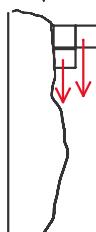
vs.

Gravity

This is very difficult for practical implementation.



Assumption: No horizontal connection.

A small schematic diagram showing a cell above a horizontal line. A red arrow points downwards, indicating the cell is dropping to the bottom over a horizontal connection.

as long as there is no supporting directly underneath the cell, the cell drops to bottom.

The resulting profile is exactly CONCAVE.

Dropping materials are specified in yuml file. e.g. "Si" mat is dropping, but "PR" is not.