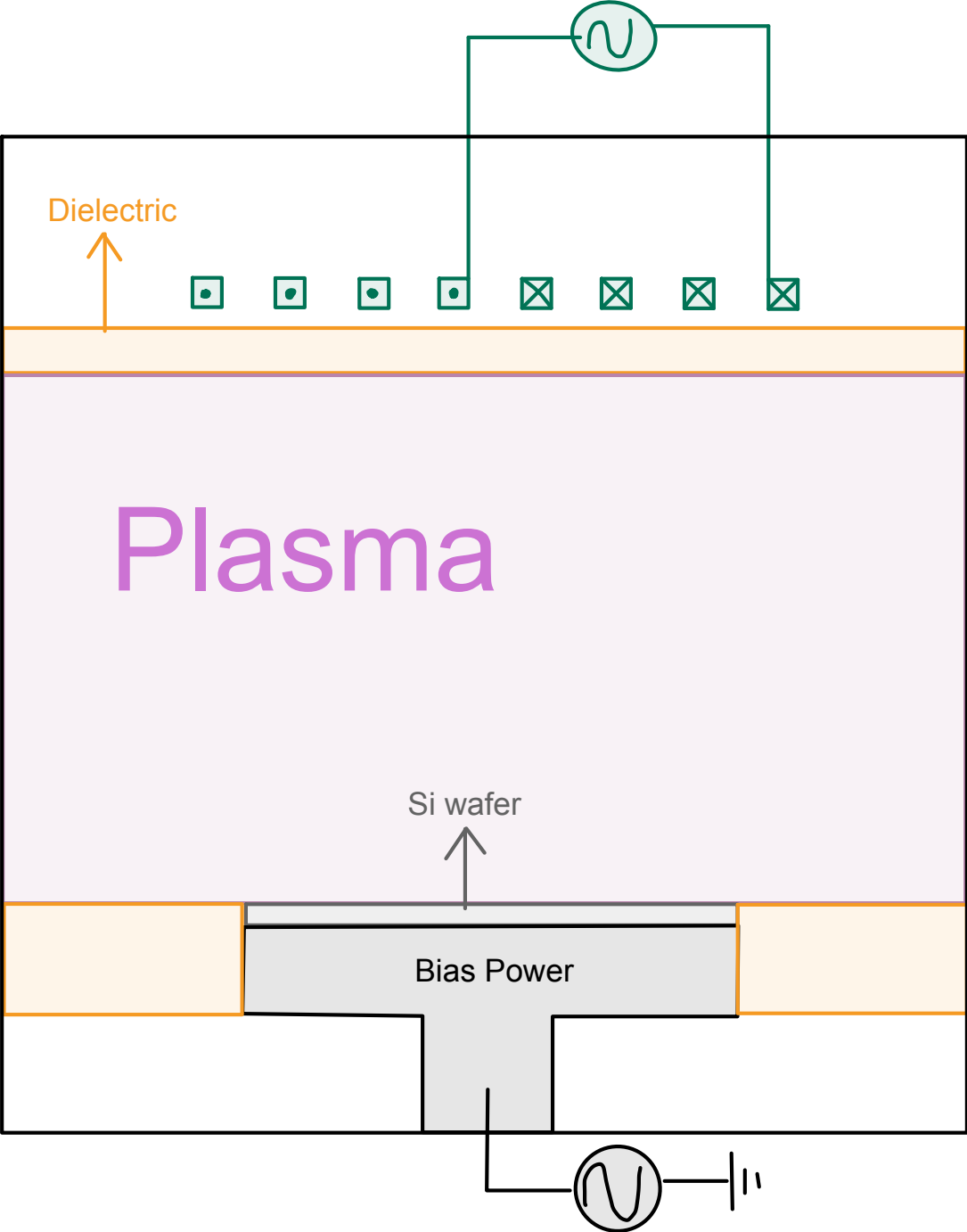
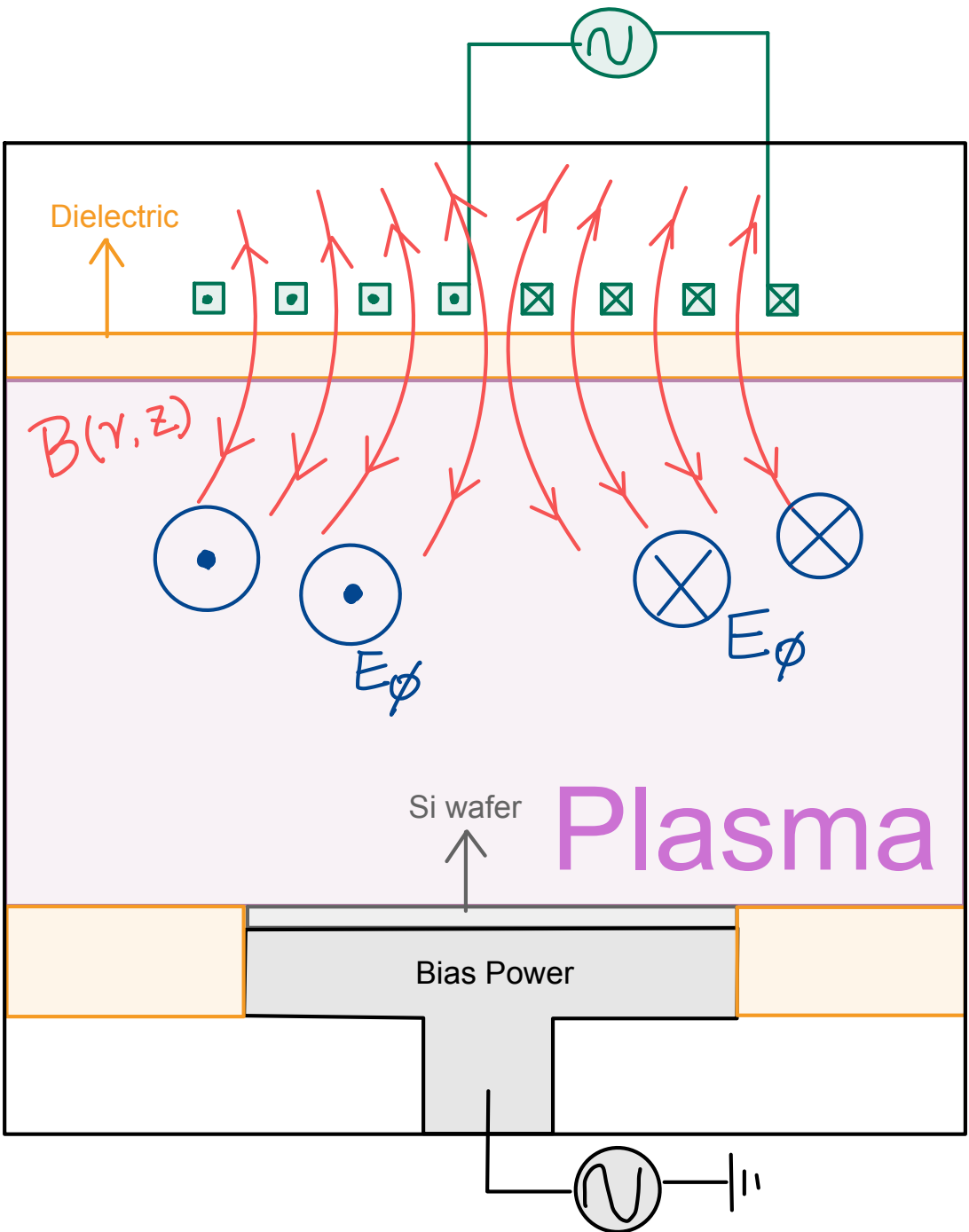
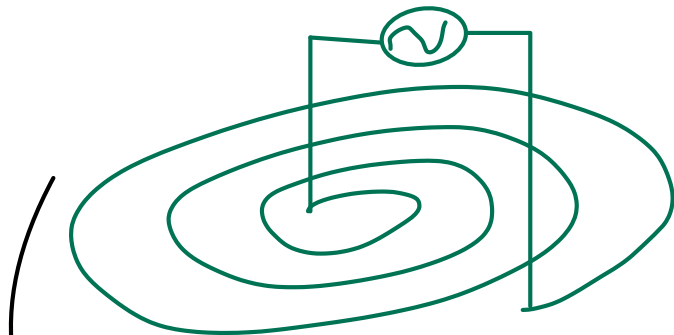


# Plasma Fluid Model V1.0



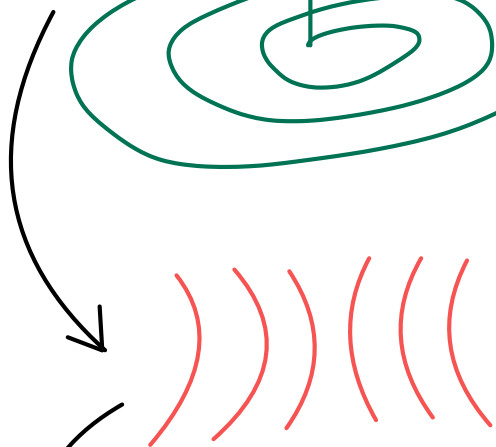
# Plasma Fluid Model V1.0





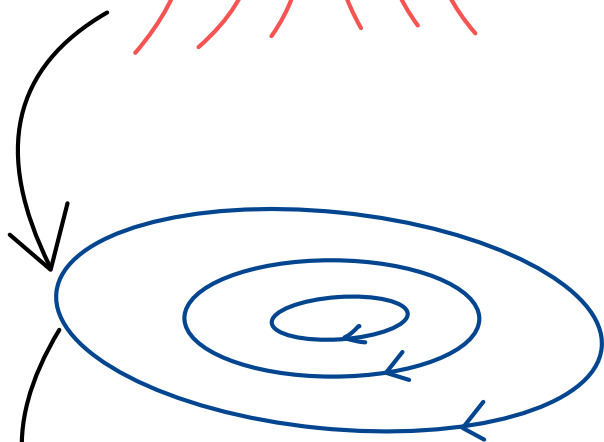
$$\vec{J} = J_0 e^{i\omega t}$$

Current in coils



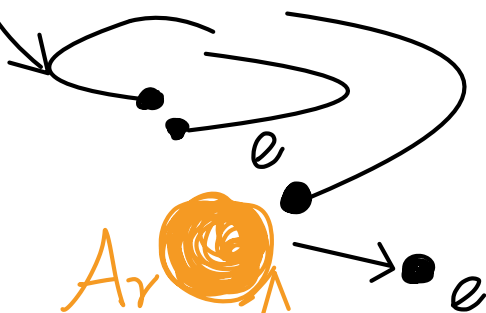
$$\vec{B} = B_0 e^{i\omega t}$$

$\vec{B}$  field in chamber



$$\vec{E} = E_\phi e^{i\omega t}$$

$\vec{E}$  field in plasma



Collision

$$a_\phi = \frac{q_e E_\phi e^{i\omega t}}{m_e}$$

steady state,

$$v_\phi = \mu_e E_\phi e^{i\omega t}$$

$$\vec{J} \rightarrow \vec{B} \rightarrow \vec{E} \rightarrow \vec{v}$$

$$J_\phi \rightarrow B_{r,z} \rightarrow E_\phi \rightarrow v_\phi$$

All B and E fields are the intermediate steps from current to velocity. As long as velocity is obtained, B and E fields are discarded.

Velocity  $\vec{v}$

$$v_\phi = \mu_e E_\phi$$

External  $J_\phi$

$$v_{r,z} = -D_e \frac{\nabla n_e}{n_e} - \mu_e E_{r,z}$$

Self induced  $(n_i - n_e)$

$$v_\phi \xrightarrow{\text{Collisions}} v_{r,z}$$

Collision Process can be very complicated.  
Instead, we solve for electron temperature,  $T_e$ .

$$D_e, \mu_e = D_e(T_e), \mu_e(T_e)$$

## Diffusion coefficient and mobility

$$\vec{\Gamma}_e = -D_e \nabla n_e - \mu_e n_e \vec{E}$$

$$D_e = \frac{kT_e}{m_e \nu_{\text{coll}}} \quad \mu_e = \frac{|e|}{m_e \nu_{\text{coll}}}$$

$$\nu_{\text{coll}} = \nu_{\text{coll}}(T_e)$$

Continuity Eq. for electron

$$\frac{\partial n_e}{\partial t} + \nabla \cdot \vec{\Gamma}_e = S_e$$

$$S_e = S_e(T_e)$$

# 1D Maxwellian velocity distribution

$$f(v) = \left( \frac{m}{2\pi kT} \right)^{1/2} \exp\left( -\frac{mv^2}{2kT} \right)$$

$m$  — mass of particle

$k$  — Boltzmann's constant

$T$  — particle temperature, width of the Maxwellian distribution

1D average kinetic energy

$$\mathcal{E}_{\text{mean}} = \frac{\int \frac{1}{2} m v^2 f(v) dv}{\int f(v) dv} = \frac{1}{2} kT$$

3D mean energy  $\mathcal{E}_{\text{mean}} = \frac{3}{2} kT$

With the assumption of Maxwellian distribution

$\mathcal{E}$  is equivalent to  $T$

In plasma physics, we usually use temperature instead of energy and velocity

## Energy equation

Continuity Eq. for electron

$$\frac{\partial n_e}{\partial t} + \nabla \cdot \vec{\Gamma}_e = S_e$$

Energy Eq. for electron

$$\frac{\partial}{\partial t}(n_e \varepsilon_e) + \nabla \cdot \vec{Q}_e = P_{in} - P_{coll-loss}$$

$$n_e \varepsilon_e = \frac{3}{2} n_e k T_e \quad \text{— Electron Energy Density}$$

$$\vec{Q}_e = \frac{5}{2} k T_e \vec{\Gamma}_e - k_e \nabla T_e \quad \text{— Energy Flux}$$

$$P_{in} = \boxed{\vec{\Gamma}_e \cdot \vec{E}} \quad \text{— Joule/Ohm/collision Heating}$$

$$\begin{aligned} P_{coll-loss} &= P_{momentum-loss} + P_{reaction-loss} \\ &= 3 \frac{m_e}{M} n_e k v_m (T_e - T_g) + n_e N \sum_j k_j (T_e) \Delta \varepsilon_j \end{aligned}$$

# Local heating vs. Non-local heating

Local Heating — Fluid Model  
collision freq is sufficient high  
Energy is balanced Locally

$$P_{in} = \vec{J}_e \cdot \vec{E} = J_\phi E_\phi + J_r E_r + J_z E_z$$

External Field

Induced Field

$$J_{coil} \rightarrow B \rightarrow E_\phi$$

$$\nabla^2 \phi = -\frac{e}{\epsilon_0} (n_i - n_e)$$

$$J_\phi = \sigma E_\phi$$

$$J_{r,z} = \sigma E_{r,z}$$

Ohm's Law

Assume plasma is homogeneous

$\sigma$  is same for all directions

$$\sigma = \frac{n_e e^2}{m_e \nu_{coll}}$$

$$\nu_{coll} = \nu_{coll}(T_e)$$



**ICP Field Solver**

$E\phi$

**Electron Energy Solver**

$T_e$

**Chemical Reaction Solver**

$T_e$

**Plasma Fluid Solver**  
Coupled with Poisson Equation

$S_e$

$n_{e,i}, \vec{T}_{e,i}, \vec{E}_{e,i}$

$\sigma, \vec{j}$