

# Topological Hydrodynamics

From Proton Spin Asymmetry to Programmable Spacetime

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## Abstract

We present a unified theoretical framework connecting the proton spin crisis, the Sivers asymmetry, spin network renormalization, and topological quantum computation. Beginning with the experimental observation that quark intrinsic spins account for only  $\approx 30\%$  of the proton’s total spin  $J = 1/2$ , we develop a categorical and cohomological interpretation in which the “missing” angular momentum is encoded in the topology of an underlying spin network. The Sivers function is identified as a co-boundary obstruction in a Poincaré complex, the renormalization group flow is cast as a functorial coarse-graining via the Day convolution, and the proton itself is modeled as a self-correcting homological code. We propose a quantum circuit architecture—built on Majorana zero modes and surface codes—that programs torsion directly into the lattice geometry, enabling the simulation of traversable wormholes through syndrome teleportation. A distributed rApp protocol—implemented in the Babel categorical DSL on the Reality SDK—is formulated to govern topological charge conservation across entangled Poincaré complexes, and the critical exponents for the traversability phase transition are estimated against modern quantum hardware capabilities.

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# 1 Introduction

Many modern theories propose that reality is computational in nature. Wheeler’s “it from bit,” Bostrom’s simulation argument, loop quantum gravity’s discrete spin networks, the holographic principle—these are no longer fringe ideas. Across physics, computer science, and philosophy, a rough consensus is forming: whatever the universe *is*, it behaves like a computation.

Yet most simulation hypotheses stop at the metaphor. They assert “it’s a computation” but never specify *what kind* of computation. This paper takes the next step. If spacetime is a program, it must be built on **well-founded recursion**—a programming model in which every computation is guaranteed to terminate, every process is total, and the system is halt-free by construction [40]. The universe does not crash. It does not diverge. It settles. That constraint alone is enough to derive the categorical and topological structures we observe.

Under this lens, the proton spin crisis is not a mystery but a **debugging clue**. When quark spins account for only 30% of total proton spin, we are observing a measurement artifact analogous to querying a distributed system mid-transaction. The “missing” spin is not missing—it is in the mempool, awaiting confirmation. The Sivers asymmetry sign change between deep inelastic scattering and Drell–Yan is not a paradox but a **gauge artifact**: the same data read from two different entry points in the program’s execution graph. The inconsistencies of particle physics are the edge cases of a running program.

If spacetime runs on topological code, then understanding that code means we can modify it. This paper develops the tools to do exactly that: a categorical programming language for torsion, a syndrome monad that captures gravitational effects as computational side effects, and a protocol for teleporting topological charge between entangled regions. Programming a wormhole is not metaphor—it is the logical consequence of treating spacetime as executable topology.

The ideas that follow are speculative, but they are not unfalsifiable. The paper closes with five concrete predictions testable at existing facilities —RHIC, the Electron-Ion Collider, and near-term quantum hardware. The standard is simple: if the program model is right, the data will show it.

## 2 The Proton Spin Crisis

### 2.1 Experimental Origins

Proton spin asymmetry measures how the scattering of protons depends on their spin orientation relative to particle beams. The 1987 European Muon Collaboration (EMC) experiment revealed that quark intrinsic spins contribute only a small fraction—roughly 12–30%—of the total proton spin, contradicting the naïve quark-model expectation that three valence quarks carry the bulk of the angular momentum. This discrepancy became known as the *proton spin crisis*.

The total proton spin decomposes as

$$J = \frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g, \quad (1)$$

where  $\Delta\Sigma$  is the quark spin contribution,  $\Delta G$  the gluon spin contribution, and  $L_q$ ,  $L_g$  the orbital angular momentum of quarks and gluons respectively.

## 2.2 Key Observables

### Longitudinal Asymmetry $A_1$

Measured in deep-inelastic scattering (DIS) of polarized leptons off polarized protons, this observable reveals the helicity distributions of quarks and gluons. The integral of the spin-dependent structure function  $g_1$  constrains  $\Delta\Sigma$ .

### Transverse Single-Spin Asymmetry (TSSA)

Observed in proton–proton collisions, these asymmetries are often unexpectedly large, indicating non-zero orbital angular momentum and the need for transverse-momentum-dependent (TMD) parton distribution functions.

## 2.3 Experimental Facilities

Research at Brookhaven National Laboratory’s Relativistic Heavy Ion Collider (RHIC) has been instrumental in constraining the gluon spin contribution  $\Delta G$ . The future Electron-Ion Collider (EIC) will map the three-dimensional structure of the proton with unprecedented precision, probing generalized parton distributions (GPDs) and TMDs simultaneously.

# 3 Spin Network Interpretation

## 3.1 The Proton as a Bound State of a Spin Network

In Loop Quantum Gravity (LQG), space is discretized into a *spin network*—a graph whose edges carry spin representations  $j = 1/2, 1, 3/2, \dots$  and whose nodes represent quanta of volume.

**Definition 3.1** (Spin-Network Proton). Rather than viewing a proton as a point-like particle propagating through a background spacetime, we model it as a topological defect—a specific excitation of the spin network. The total spin  $J = 1/2$  is an emergent property of the local geometry and the way the network edges are woven together.

## 3.2 The Crisis as a Geometric Phenomenon

From the spin-network perspective, the “missing” spin admits a natural explanation:

- **Relational entanglement.** In a spin network, angular momentum is a property of the connections (edges) between nodes. If quarks are nodes, much of the angular momentum is stored in the edges (gluon fields / geometry) connecting them.
- **Orbital angular momentum.** Spin networks naturally incorporate the spatial relationships between components. What QCD calls “orbital angular momentum” is the quantum of area and volume encoded in the network’s geometry.

Framework	Perspective on Proton Spin
Braided Matter Models	Elementary particles are “braids” in the spin network (Bilson-Thompson). Spin is a topological property of how the strands twist.
Holographic Spin Networks	Internal degrees of freedom are holographically encoded on a 2D surface. Asymmetry arises from the boundary map.
Algebraic QFT	Uses spin-foam logic to describe the flux of spin, naturally accommodating the gluon contribution.

Table 1: Theoretical frameworks connecting spin networks to proton structure.

### 3.3 Theoretical Frameworks

## 4 The Sivers Effect and Functorial Models

### 4.1 The Sivers Function

The Sivers function  $f_{1T}^{\perp q}(x, \mathbf{k}_{\perp}^2)$  describes the correlation between the proton’s transverse spin  $\mathbf{S}_T$  and the quark’s transverse momentum  $\mathbf{k}_{\perp}$ . It is *T-odd*: it changes sign between semi-inclusive DIS (SIDIS) and Drell–Yan (DY) processes, a prediction confirmed by the COMPASS experiment.

### 4.2 Gauge Links as Functors

The Sivers effect relies on initial-/final-state interactions (ISI/FSI), represented in QCD by Wilson lines—path-ordered exponentials of the gauge field.

**Definition 4.1** (Wilson-Line Functor). A Wilson line defines a functor from the *path groupoid* (the paths a quark traverses) to the *category of vector spaces* (the color/spin states of the quark). The Sivers asymmetry measures the failure of this functor to be “flat” under a change in spin orientation: it maps a change in the spin category to a displacement in the momentum category.

### 4.3 Braided Categories and the Sign Change

In braided-ribbon-network models, the Sivers effect is represented by a *braiding morphism*. Treating the proton spin as a topological winding number, the asymmetry arises naturally from the braid twisting as a parton is ejected. This picture is qualitatively consistent with the observed sign change between SIDIS and DY.

### 4.4 AdS/QCD and Light-Front Holography

The most data-consistent “functor-like” mapping comes from AdS/CFT. Light-Front Holography (LFH), developed by Brodsky and de Téramond, creates a dictionary (functor) between a 5D gravitational theory and 4D QCD. Predictions for the Sivers-like distribution of quarks align with experimental extractions from HERMES and COMPASS.

## 5 Light-Front Holographic Equations of Motion

### 5.1 The Light-Front Schrödinger Equation

The radial equation of motion derived from the AdS/QCD mapping determines the mass spectrum of the proton:

$$\left( -\frac{d^2}{d\zeta^2} - \frac{1-4L^2}{4\zeta^2} + U(\zeta) \right) \phi(\zeta) = M^2 \phi(\zeta), \quad (2)$$

where  $\zeta = \sqrt{x(1-x)} |\mathbf{b}_\perp|$  is the holographic variable,  $L$  is the orbital angular momentum, and the confinement potential is

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2(L + S - 1). \quad (3)$$

### 5.2 Universal Radial Profile

The solution for a state with quantum numbers  $(n, L)$  is

$$\varphi_{n,L}(\zeta) = \kappa^{1+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{1/2+L} e^{-\kappa^2 \zeta^2/2} L_n^L(\kappa^2 \zeta^2). \quad (4)$$

For the ground-state proton ( $n = 0, L = 0$ ), this reduces to a Gaussian-like profile.

### 5.3 Spin-Improved Light-Front Wavefunctions

The Sivers asymmetry requires interference between  $L = 0$  and  $L = 1$  states. The spin-improved wavefunctions for a quark  $q$  inside a proton are

$$\psi_{+,h=+1/2}^q(x, \mathbf{k}_\perp) = \varphi_{L=0}(x, \mathbf{k}_\perp) + \alpha^q \frac{\mathbf{k}_\perp^2}{M^2} \varphi_{L=1}(x, \mathbf{k}_\perp), \quad (5)$$

$$\psi_{-,h=+1/2}^q(x, \mathbf{k}_\perp) = -\frac{k^1 - ik^2}{xM} \beta^q \varphi_{L=1}(x, \mathbf{k}_\perp), \quad (6)$$

where  $\alpha^q$  and  $\beta^q$  are parameters fixed by the anomalous magnetic moments of the proton and neutron.

### 5.4 Extraction of the Sivers Function

The Sivers function is computed as the overlap integral

$$f_{1T}^{\perp q}(x, \mathbf{k}_\perp^2) = \frac{M}{2\pi} \text{Im} \left[ \psi_{+,+1/2}^{q*}(x, \mathbf{k}_\perp) \psi_{-,+1/2}^q(x, \mathbf{k}_\perp) \right], \quad (7)$$

yielding the asymmetric “dipole” distribution observed in COMPASS and HERMES data: positive for  $u$ -quarks, negative for  $d$ -quarks.



## 6 Unifying Spin-Foam Renormalization with Light-Front Evolution

### 6.1 Scale as Resolution

In light-front evolution, the renormalization scale  $Q^2$  sets the resolution of the proton's constituents. In spin foams, scale is replaced by the refinement limit of the discretization. The unifying insight is:

**Proposition 6.1** (Functorial Link). The boosted light-front time  $x^+$  acts as a foliation parameter for the spin foam. As one evolves along the light front, the spin foam undergoes Pachner moves that increase the number of edges and nodes (quarks and gluons).

### 6.2 RG Flow as Coarse-Graining

- **Light-front view.** The RG flow (via DGLAP or CSS equations) evolves the TMD distributions.
- **Spin-foam view.** The RG flow is a coarse-graining procedure on the spin network. Tensor Network Renormalization (TNR, see section 7.2 for the detailed formalism) shows how a complex web of spins (high  $Q^2$ ) averages into a single effective “valence quark” node at low energy.
- **Synthesis.** The equations of motion for the Siverts effect emerge when *cylindrical consistency* of the spin network (required for diffeomorphism invariance; see section 7.3) is forced to match the *unitarity constraints* of the light-front Hamiltonian.

### 6.3 Hamiltonian Constraint in Light-Front Coordinates

The Hamiltonian constraint from LQG,  $\hat{H}\Psi = 0$ , is projected onto the light-front eigenvalue problem:

$$\hat{H}_{LF} |\Psi_{\text{proton}}\rangle = M^2 |\Psi_{\text{proton}}\rangle . \quad (8)$$

In a unified model,  $\hat{H}_{LF}$  is derived from the vertex amplitudes of the spin foam. The Siverts asymmetry appears as a non-commutative phase in the vertex amplitude when the spin labels on the network edges are polarized.

## 7 Spin Network Coarse-Graining and the Proton as a Complex Network

The preceding sections invoke coarse-graining of spin networks (section 6) and iterated hashing (section 11) informally. This section provides the mathematical backbone: we define the colored spin network of the proton, specify three coarse-graining operations, state the cylindrical-consistency condition that connects scales, and show how diffeomorphism invariance is restored in the continuum limit. The proton then appears as a multi-scale complex network whose topological complexity is directly related to its mass.

## 7.1 The Colored Spin Network of the Proton

Let  $\Gamma = (V, E)$  be a finite oriented graph embedded in a spatial 3-manifold  $\Sigma$ . To each edge  $e \in E$  we assign an irreducible representation  $\rho_e$  of  $SU(3)_c$  (the color gauge group) and, independently, a spin  $j_e \in \{0, 1/2, 1, \dots\}$  of  $SU(2)_J$  (rotational symmetry). At every node  $v \in V$  we place an intertwiner

$$\iota_v \in \text{Inv}\left(\bigotimes_{e \ni v} \rho_e \otimes V_{j_e}\right), \quad (9)$$

where the tensor product runs over all edges incident at  $v$  and  $\text{Inv}(\cdot)$  denotes the invariant subspace under the joint action of  $SU(3)_c \times SU(2)_J$ .

**Definition 7.1** (Colored Spin-Network Hilbert Space). The Hilbert space of colored spin-network states on  $\Gamma$  is

$$\mathcal{H}_\Gamma = \bigoplus_{\{\rho_e, j_e\}} \bigotimes_{v \in V} \mathcal{I}_v \otimes \bigotimes_{e \in E} V_{\rho_e} \otimes V_{j_e}, \quad (10)$$

where  $\mathcal{I}_v$  is the intertwiner space at node  $v$  and the direct sum runs over all admissible labelings.

**Remark 7.1** (Connection to the chain complex). The nodes  $V$  and edges  $E$  of  $\Gamma$  are precisely the 0-cells  $C_0$  and 1-cells  $C_1$  of the chain complex introduced in section 10: quarks sit at  $C_0$  and gluon flux tubes span  $C_1$ . The intertwiner  $\iota_v$  at each node enforces the local color-singlet constraint (cf. the closure condition of definition 11.1).

## 7.2 Coarse-Graining Operations

Three elementary operations reduce the complexity of  $(\Gamma, \{\rho_e, j_e, \iota_v\})$  while preserving long-range physics.

**1. Edge contraction.** Given an edge  $e = (v_1, v_2)$ , contract it to a single node  $v_{12}$  with effective intertwiner

$$\iota_{v_{12}}^{\text{eff}} = \sum_{\rho_e, j_e} d_{\rho_e} d_{j_e} (\iota_{v_1} \otimes \iota_{v_2})|_{\text{Inv}}, \quad (11)$$

where  $d_\rho$  and  $d_j$  are the dimensions of the respective representations and the projection is onto the invariant subspace. This merges two partons into one effective degree of freedom.

**2. Node decimation (block spin).** Partition  $V$  into disjoint blocks  $\{B_\alpha\}$ . For each block, trace over all internal edges:

$$\mathcal{I}_{B_\alpha}^{\text{eff}} = \text{Tr}_{E_{\text{int}}(B_\alpha)} \left( \bigotimes_{v \in B_\alpha} \iota_v \right). \quad (12)$$

The result is a coarse graph  $\Gamma'$  with one supernode per block. In QCD language this replaces a sea-quark–gluon subcloud by a single constituent quark.

**3. Tensor network renormalization (TNR).** Write the partition function as a tensor contraction [34, 31]:

$$Z_\Gamma = \sum_{\{j_e, \rho_e\}} \prod_{v \in V} T_v^{(\iota_v)} \prod_{e \in E} d_{\rho_e} d_{j_e}, \quad (13)$$

where  $T_v^{(\iota_v)}$  is the intertwiner tensor at node  $v$ . Perform a singular-value decomposition on every pair of adjacent tensors, truncate to the leading  $\chi$  singular values, and reconstitute the network on a coarser graph  $\Gamma'$ .

CG Operation	Spin-Network Action	QCD / Proton Interpretation
Edge contraction	Merge two nodes via an edge; sum over internal reps	Quark–gluon fusion: two partons merge into one effective parton
Node decimation	Trace over internal edges of a block	Constituent-quark picture: a sea-quark cloud collapses into a single constituent quark
TNR (SVD truncation)	Contract and truncate tensor network	DGLAP / CSS evolution: integrate out high- $k_\perp$ modes above a cutoff $\chi$

Table 2: Coarse-graining operations and their QCD counterparts.

### 7.3 Cylindrical Consistency and the Embedding Maps

Let  $\Gamma \subset \Gamma'$  denote a coarsening ( $\Gamma$  is obtained from  $\Gamma'$  by one or more of the operations above). Define the *embedding map*  $p_{\Gamma' \rightarrow \Gamma} : \mathcal{H}_{\Gamma'} \rightarrow \mathcal{H}_\Gamma$  by partial trace over the degrees of freedom in  $\Gamma' \setminus \Gamma$ .

**Definition 7.2** (Cylindrical Consistency). A family of states  $\{\Psi_\Gamma \in \mathcal{H}_\Gamma\}_\Gamma$  is *cylindrically consistent* if, for every pair  $\Gamma \subset \Gamma'$ ,

$$p_{\Gamma' \rightarrow \Gamma} \Psi_{\Gamma'} = \Psi_\Gamma. \quad (14)$$

The condition states that coarse-graining the fine state  $\Psi_{\Gamma'}$  must reproduce the coarse state  $\Psi_\Gamma$  exactly. This is the spin-network analog of the statement that a valence-quark observable at low  $Q^2$  must be reproducible from the full parton-level description at high  $Q^2$ .

The consistency condition is summarized by the commutative diagram

$$\begin{array}{ccc} \mathcal{H}_{\Gamma''} & \xrightarrow{p_{\Gamma'' \rightarrow \Gamma'}} & \mathcal{H}_{\Gamma'} \\ & \searrow p_{\Gamma'' \rightarrow \Gamma} & \downarrow p_{\Gamma' \rightarrow \Gamma} \\ & & \mathcal{H}_\Gamma \end{array} \quad (15)$$

which must commute for any triple  $\Gamma \subset \Gamma' \subset \Gamma''$ .

## 7.4 Restoration of Diffeomorphism Invariance

A spin network on a fixed graph  $\Gamma$  breaks the diffeomorphism invariance of the continuum theory. Three complementary mechanisms restore it in the limit [32, 33].

**1. Diffeomorphism averaging.** The physical (diffeomorphism-invariant) Hilbert space is obtained as a quotient [33]:

$$\mathcal{H}_{\text{phys}} = \mathcal{H}_{\text{kin}} / \text{Diff}(\Sigma), \quad (16)$$

where  $\text{Diff}(\Sigma)$  acts by moving graph vertices and edges through  $\Sigma$ . Two spin-network states that differ only by a diffeomorphism are identified; only the combinatorial (abstract-graph) data survive.

**2. Perfect discretization.** Following Bahr and Dittrich [29], one seeks an effective action  $S_{\text{eff}}[\Gamma]$  on the coarse graph such that

$$Z_{\Gamma}^{\text{eff}} = \int \mathcal{D}\phi_{\text{fine}} e^{-S[\Gamma', \phi_{\text{fine}}]} = e^{-S_{\text{eff}}[\Gamma]}, \quad (17)$$

i.e. the coarse partition function captures the full fine-grained dynamics exactly. The resulting discrete theory is automatically diffeomorphism-invariant to the extent that the continuum theory is.

**3. Continuum limit as RG fixed point.** Under iterated coarse-graining, the effective couplings flow toward a fixed point [30]:

$$\lim_{n \rightarrow \infty} (\mathcal{R}^n \cdot S) = S^*, \quad (18)$$

where  $\mathcal{R}$  is the coarse-graining superoperator and  $S^*$  is the fixed-point action. If  $S^*$  is diffeomorphism-invariant (as expected for QCD), then every finite truncation inherits approximate invariance, with corrections that vanish as the lattice is refined.

**Remark 7.2.** For the proton, “diffeomorphism invariance” maps concretely to  $\text{SU}(3)_c$  gauge invariance: the Wilson line (section 11.2) is the gauge-invariant hash that compresses a continuous gauge-field configuration into a single group element. The perfect-discretization condition (17) demands that this hash is *exact*—no gauge-invariant information is lost in the coarse-graining.

## 7.5 The Proton as a Multi-Scale Complex Network

At different resolutions, the proton’s spin network presents qualitatively different graph topologies. Table 3 summarizes three characteristic regimes.

To quantify the network structure at each scale, introduce three standard graph-theoretic observables:

- **Degree distribution**  $P(k)$ : the fraction of nodes with  $k$  incident edges.
- **Clustering coefficient**  $C$ : the probability that two neighbors of a node are themselves connected.

Scale	Resolution ( $Q^2$ )	Graph Topology	Physical Content
UV	$\gtrsim 100 \text{ GeV}^2$	Dense lattice, $ V  \gg 1$	Sea quarks, gluons, and their OAM (full partonic content)
Intermediate	$1\text{--}10 \text{ GeV}^2$	Effective graph, $ V  \sim 10$	Constituent quarks, gluon clusters, valence + sea
IR	$< 1 \text{ GeV}^2$	$Y$ -graph, $ V  = 3$	Three valence quarks connected by flux-tube junctions

Table 3: The proton as a multi-scale complex network.

- **Betweenness centrality**  $B_v$ : the fraction of shortest paths in the network that pass through node  $v$ .

**Proposition 7.1** (Coarse-graining simplifies network metrics). Under successive coarse-graining steps  $\Gamma_{\text{UV}} \rightarrow \cdots \rightarrow \Gamma_{\text{IR}}$ :

1.  $P(k) \rightarrow \delta_{k,2}$ : every node in the IR  $Y$ -graph has exactly two incident edges.
2.  $C \rightarrow 0$ : the  $Y$ -graph is a tree and contains no triangles.
3.  $\max_v B_v \rightarrow 1/3$ : each of the three valence-quark nodes lies on exactly one-third of the shortest paths.

These limiting values match the topological properties of the confining string junction that connects three quarks in the IR limit of lattice QCD.

## 7.6 Network Complexity and Mass Generation

Define the *topological complexity* of a colored spin network as

$$\mathcal{C}(\Gamma) = \sum_{v \in V} \ln \dim \mathcal{I}_v + \sum_{e \in E} \ln(d_{\rho_e} d_{j_e}) + \sum_{k \geq 1} \beta_k(\Gamma) \ln k, \quad (19)$$

where  $\beta_k(\Gamma)$  is the  $k$ -th Betti number of the graph. The first term counts intertwiner degrees of freedom (nodes / quarks), the second counts representation degrees of freedom (edges / gluons), and the third measures topological loops.

**Proposition 7.2** (Mass from complexity). At the RG fixed point  $\Gamma^*$  of the coarse-graining flow, the proton mass satisfies

$$M_p^2 \propto \mathcal{C}(\Gamma^*), \quad (20)$$

i.e. the squared mass is proportional to the topological complexity of the fixed-point network. This gives a microscopic derivation of the “mass as complexity” identification in the topological Einstein equation (54) of section 20.

The connection is natural: a more complex spin network requires a larger error-correction overhead (syndrome entropy) to stabilize, and the stabilizer pressure is precisely the mass seen by an external observer. The coarse-graining flow  $\Gamma_{\text{UV}} \rightarrow \Gamma^*$  integrates out UV fluctuations while preserving the topological invariant  $J = 1/2$ ; the residual complexity at the fixed point is the irreducible cost of maintaining that invariant against vacuum noise.

## 8 Majorana Zero Modes and Topological Quantum Computing

### 8.1 MZMs as Torsion Defects

In homological codes (Kitaev chain, Toric code), a Majorana Zero Mode (MZM) acts as a defect at the end of a spin chain. Braiding two MZMs performs a unitary transformation on the ground state—this “twist” is the topological equivalent of geometric torsion in a 3D spin network.

### 8.2 The Proton as a Majorana Bound State

Viewing the proton’s  $uud$  structure through a homological lens:

- Quarks are modeled as Majorana-like excitations at the nodes of the tensor network.
- The spin crisis is resolved: spin is stored topologically in the strings (gluons) connecting the MZMs.
- The Sivers effect becomes the Berry phase acquired by dragging a Majorana defect through the network during DIS scattering.

### 8.3 Wormholes via Majorana Entanglement

Using the Sachdev–Ye–Kitaev (SYK) model of MZMs in a random network:

1. Entangle a pair of MZMs across two separate homological codes (representing two “protons”).
2. The logical qubit now exists in both locations simultaneously.
3. The SYK model is holographically dual to a traversable wormhole in  $\text{AdS}_2$  gravity.

## 9 Functorial Correspondence: MZMs, Day Convolution, and Poincaré Complexes

### 9.1 From MZMs to Day Convolution

A Majorana Zero Mode is an object in a *Modular Tensor Category* (MTC). We define a functor  $\mathcal{F}$  mapping the braiding and fusion of MZMs into a monoidal category. The *Day convolution*  $\otimes_{\text{Day}}$  acts as the mechanism for merging or coarse-graining the tensor

network—it propagates local spin information (MZM twists) into global network properties and serves as the engine of the renormalization group. (The formal definition of Day convolution and the proof of its uniqueness as the free monoidal completion of the RG scale poset are given in section 12.6.)

## 9.2 The Poincaré Complex in Blockchain Cohomology

Treating spin nodes as a simplicial complex:

- **Blockchain cohomology** treats “blocks” (or spin nodes) as a simplicial complex. Validating a transaction is equivalent to checking that a boundary operator  $\partial$  vanishes (the chain is a cycle).
- A **Poincaré complex** satisfies Poincaré duality: the internal spin structure ( $k$ -cells) perfectly matches the external boundary ( $(n-k)$ -cells). It represents a state of *topological consensus*.
- The functor  $\mathcal{F}$  takes the noisy local Majorana braids (quarks) and, through the Day convolution, outputs a Poincaré complex—the “immutable ledger” of the proton.

## 9.3 The Wormhole as a Cross-Chain Bridge

Programming a wormhole is equivalent to constructing a *cross-chain functor*: the Day convolution ensures that the Poincaré complex of Proton A is entangled (isomorphic) with that of Proton B. By programming MZM torsion (the Siverts effect), one writes a “well-founded protocol” [40] into the fabric of spacetime, forcing two distinct regions into a single homological identity.

# 10 Boundary Operators and the Siverts Function

## 10.1 The Chain Complex of the Proton

Define the proton structure as a chain complex:

$$\cdots \xrightarrow{\partial_{n+1}} C_n \xrightarrow{\partial_n} C_{n-1} \xrightarrow{\partial_{n-1}} \cdots \xrightarrow{\partial_1} C_0, \quad (21)$$

where  $C_0$  (nodes) represents the quarks and  $C_1$  (edges) represents the gluon flux tubes. In a stable proton (a closed chain),  $\partial_n \circ \partial_{n+1} = 0$ .

## 10.2 The Siverts Function as a Co-boundary Obstruction

Let  $\delta$  be the co-boundary operator (adjoint of  $\partial$ ). The Siverts function  $f_{1T}^\perp$  corresponds to a 1-cocycle in  $H^1$ —a characteristic class measuring how the spin bundle is twisted over the momentum base:

$$\langle \text{Siverts} \rangle \propto \oint_{\partial\Sigma} \omega_{\text{spin}}, \quad (22)$$

where  $\partial\Sigma$  is the boundary of the transverse momentum space.

Particle Physics	Categorical Analog	Boundary Math
Quark transverse momentum	Local transaction payload	Chain element $c \in C_n$
Proton spin state	Global ledger consensus	Cycle $z \in \ker(\partial)$
Sivers function	Boundary obstruction	$\delta\omega \neq 0$
OAM	Homological loop	Non-trivial $H_1$ class
Gluon field	Distributed network graph	The simplicial complex

Table 4: Correspondence between particle physics and cohomological concepts.

### 10.3 Blockchain Cohomology Interpretation

## 11 The Poincaré Protocol and the Spin Crisis as Latency

The chain complex of section 10 and its blockchain-cohomology interpretation lead to a striking re-reading of the proton spin crisis: the “missing” spin is not missing at all; it is unresolved data in the mempool of the Poincaré protocol.

### 11.1 The Poincaré Protocol

**Definition 11.1** (Poincaré Protocol). The *Poincaré protocol* is the consensus mechanism by which the proton’s spin network maintains its global topological invariant  $J = 1/2$ . It operates on the chain complex  $C_\bullet = (C_n \xrightarrow{\partial_n} C_{n-1} \rightarrow \cdots \xrightarrow{\partial_1} C_0)$  and enforces two conditions at every energy scale  $Q^2$ :

1. **Closure.**  $\partial \circ \partial = 0$ : the boundary of a boundary is zero. This guarantees that the total spin ledger is self-consistent—no angular momentum is created or destroyed, only redistributed among cells.
2. **Poincaré duality.** The  $k$ -th homology group  $H_k$  of the complex is isomorphic to the  $(n-k)$ -th cohomology group  $H^{n-k}$ . This enforces a symmetry between the “interior” degrees of freedom (quarks, nodes) and the “boundary” degrees of freedom (gluons, edges): every unit of spin committed to a node is mirrored by a dual unit of spin stored in the surrounding edges.

The protocol is *scale-dependent*: the Day convolution  $\otimes_{\text{Day}}$  acts as the propagation mechanism that resolves finer structure as the probe energy  $Q^2$  increases, analogous to increasing the block height in a distributed ledger.

**Remark 11.1** (Cylindrical consistency as monad associativity). The cylindrical consistency condition (Eq. (14)) will be shown in section 12 to be equivalent to the *associativity law* of the Syndrome Monad:  $\mu \circ \mathsf{T}(\mu) = \mu \circ \mu_{\mathsf{T}}$ . The Poincaré protocol’s requirement that coarse-graining commutes with embedding is precisely the statement that the RG decoder  $\mu$  is associative—the order in which nested syndrome layers are collapsed does not matter.



## 11.2 The Wilson Line as a Hash Function

The dictionary in table 6 identifies the Wilson line as the “hash function” of the Poincaré protocol. This identification is not metaphorical; the Wilson line satisfies the defining properties of a cryptographic hash, with gauge invariance playing the role of collision resistance.

### 11.2.1 Construction

A quark traversing a path  $\gamma$  through the gluon field  $A_\mu(x)$  accumulates a net color rotation given by the path-ordered exponential:

$$W[\gamma] = \mathcal{P} \exp \left( -ig \int_\gamma A_\mu(x) dx^\mu \right) \in \text{SU}(3). \quad (23)$$

This operator takes the full continuous gauge-field configuration along  $\gamma$ —infinitely many degrees of freedom—and compresses it into a single  $\text{SU}(3)$  matrix (8 real parameters).

### 11.2.2 Property-by-Property Mapping

Hash Property	Cryptographic Meaning	Wilson-Line Realization
Deterministic	Same input $\Rightarrow$ same digest	Same gauge field $A_\mu$ and path $\gamma$ always yield the same $\text{SU}(3)$ matrix $W[\gamma]$
Compressive	Output is much smaller than input	$\infty$ field degrees of freedom $\rightarrow$ 8 real parameters
One-way	Cannot reconstruct input from digest	Given $W[\gamma]$ alone, the gauge-field configuration along $\gamma$ cannot be recovered; many configurations produce the same $W$ (gauge orbits)
Collision resistance	Hard to find two inputs with the same digest	Gauge invariance: physically distinct configurations are distinguished by $W$ ; gauge-equivalent ones (which are <i>not</i> physically distinct) map to the same orbit
Composable	Hashes can be chained: $H(H(x)  y)$	Wilson lines compose under path concatenation: $W[\gamma_1 \circ \gamma_2] = W[\gamma_1] W[\gamma_2]$

Table 5: Property-by-property correspondence between cryptographic hash functions and Wilson lines.

### 11.2.3 What “Hashing Local Spin Data” Means Physically

The phrase “the Day convolution hashes local spin data into the global Poincaré complex” refers to a three-step physical process:

1. **Local data (the transaction).** A quark at node  $A$  in the spin network has a definite spin-polarization state—say, helicity  $+1/2$ . In the chain complex, this is a chain element  $c \in C_0$ : a transaction waiting to be committed.
2. **Hash / propagation (the Wilson line).** The gluon flux tube connecting node  $A$  to node  $B$  defines a path  $\gamma$ . The Wilson line  $W[\gamma]$  acts on the quark’s color-spin state, rotating and mixing its degrees of freedom via Eq. (23). The detailed structure of the gluon field along the tube is irrelevant—only the net  $SU(3)$  rotation (the hash digest) matters. This is gauge invariance in action: the “raw data” of the gauge field is compressed into a single group element.
3. **Commitment to the ledger (the global invariant).** The quark’s spin state *after* rotation by the Wilson line is what gets committed to the global Poincaré complex. The total proton spin  $J = 1/2$  is the sum over all such committed states across all nodes and edges of the network.

### 11.2.4 Coarse-Graining as Iterated Hashing

The RG flow from high  $Q^2$  to low  $Q^2$  is an *iterated hashing* process (the formal coarse-graining operations are defined in section 7). At high  $Q^2$ , the spin network has many nodes (sea quarks) and edges (gluons), each with their own spin data. As  $Q^2$  decreases, the Day convolution contracts subgraphs into single effective nodes:

$$\underbrace{\{q_1, q_2, \bar{q}_3, g_4, g_5, \dots\}}_{\text{high-}Q^2 \text{ subgraph}} \xrightarrow{W[\gamma_{\text{eff}}]} \underbrace{q_{\text{valence}}}_{\text{low-}Q^2 \text{ node}} \quad \text{with} \quad \Delta q_{\text{valence}} = \text{tr}(W[\gamma_{\text{eff}}] \rho_{\text{subgraph}}). \quad (24)$$

A single valence quark at low  $Q^2$  is the hash digest of an entire subgraph at high  $Q^2$ . The valence quark spin  $\Delta q \approx 0.30$  encodes the net spin of a complex subsystem in a single number, and one cannot recover the detailed internal structure from that number alone without probing at higher  $Q^2$ —exactly the one-way property of a hash.

This is why the “spin crisis” is a latency problem: the valence-quark spin  $\Delta\Sigma$  is a low-resolution hash digest. It faithfully encodes the *net* spin contribution at that scale, but it has compressed away the detailed decomposition into  $\Delta G$ ,  $L_q$ , and  $L_g$ . To see those contributions, one must increase  $Q^2$  (raise the block height), forcing the Day convolution to resolve the subgraph and expose the mempool.

## 11.3 Dictionary: Blockchain Cohomology and Particle Physics

The following table provides a comprehensive dictionary between the concepts of distributed-ledger consensus and the internal dynamics of the proton. The left column defines the blockchain concept; the right column identifies its physical realization.

Table 6: Complete dictionary between blockchain cohomology and proton physics.

Blockchain concept	Con-	Physics concept	Con-	Formal Identification
Distributed ledger		Proton spin network		The simplicial complex $C_\bullet$ whose cells are quarks (nodes) and gluon flux tubes (edges)
Confirmed block		Valence state	quark	A 0-cycle $z \in \ker(\partial_1) \subset C_0$ : angular momentum that has been locally committed to a node
Mempool (unconfirmed transactions)		Sea quarks and gluons		Syndrome data: non-trivial chains in $C_1, C_2, \dots$ that carry angular momentum in the edges and higher cells
Block height		Probe resolution $Q^2$		The energy scale at which the Day convolution has propagated; higher $Q^2$ resolves finer cells in the complex
Global ledger state		Total proton spin $J = 1/2$		The homology class $[z] \in H_0(C_\bullet)$ : the logical qubit, always exactly $1/2$ regardless of block height
Consensus protocol		Poincaré protocol		The closure condition $\partial \circ \partial = 0$ plus Poincaré duality (Def. 11.1)
Mining / validation		Day convolution $\otimes_{\text{Day}}$		The functorial operation that hashes local spin data (MZM braids) into the global Poincaré complex
Hash function		Wilson line		The path-ordered exponential of the gauge field; maps a quark path (transaction route) to a color/spin state (hash digest)
Proof of work		Termination proof		<code>WellFounded.fromMeasure</code> : a decreasing measure guaranteeing that the consensus computation halts
Transaction		Quark momentum transfer		A chain element $c \in C_n$ representing a parton carrying transverse momentum $\mathbf{k}_\perp$
Transaction fee (gas)		Torsional phase $\phi$		The Sivers phase: the “cost” of routing a transaction through the network; determines the direction of the asymmetry

*Continued on next page*

Blockchain concept	Con- cept	Physics concept	Con- cept	Formal Identification
Fork		Torsion / asymmetry	Sivers	A non-trivial element in the tor- sion subgroup of $H^n(X; \mathbb{Z})$ ; the network branches when spin is po- larized
Fork resolution		Syzygy validation		The requirement that any fork be resolved into a valid Poincaré com- plex within $t_{\text{Planck}}$ cycles
Double-spend attack		Spin violation $J \neq 1/2$		Topologically forbidden: the Poincaré protocol guarantees $[z] = 1/2$ at all scales
Latency		RG flow / evolution	TMD	The “time” (in resolution-scale) re- quired for the Day convolution to propagate spin data from the mempool into the confirmed blocks
Mempool backlog		“Missing” (70%)	spin	Angular momentum stored in $C_1$ (gluon spin $\Delta G$ ) and in non-trivial $H_1$ classes (orbital angular mo- mentum $L_q + L_g$ )
Confirmation depth		Number of steps	RG	How many coarse-graining itera- tions (Pachner moves) have been applied; deeper confirmation = lower $Q^2$ = fewer resolved degrees of freedom
Syndrome		Sea quark/gluon excitation		A stabilizer eigenvalue $-1$ ; a quasi- particle generated when the probe energy exceeds the code’s gap
Error correction		Confinement		The decoder contracts the syn- drome cloud back into a color- singlet (the logical qubit $J = 1/2$ )
Logical qubit		Baryon number / total spin		The topological invariant pro- tected by the homological code; immune to local perturbations (syndrome noise)
Code distance $d$		Confinement scale $\Lambda_{\text{QCD}}$		The minimum number of syn- drome errors required to corrupt the logical state; $d \sim 1/\Lambda_{\text{QCD}}$
Cross-chain bridge		Wormhole bridge)	(ER bridge)	Entangled Poincaré complexes: the Day convolution connects two protons into a shared syndrome space
Well-founded proto- col		Topological transfer protocol		The <code>WormholeBridgeApp</code> of sec- tion 19: a self-executing set of con- straints governing syndrome tele- portation

## 11.4 The Spin Crisis as a Latency Problem

With the dictionary in hand, the proton spin crisis admits a precise re-statement.

### 11.4.1 The Standard Framing

In QCD, the spin sum rule reads

$$J = \frac{1}{2} = \underbrace{\frac{1}{2}\Delta\Sigma}_{\text{quark spin}} + \underbrace{\Delta G}_{\text{gluon spin}} + \underbrace{L_q + L_g}_{\text{orbital angular momentum}}. \quad (25)$$

A DIS experiment at resolution  $Q^2$  measures  $\Delta\Sigma$  and finds it accounts for only  $\sim 30\%$  of  $1/2$ . The “crisis” assumes that all the spin *should* reside at the quarks and asks: where did the rest go?

### 11.4.2 The Blockchain Cohomology Reframing

In the Poincaré protocol, the total spin  $J = 1/2$  is the *logical qubit*—the global homology class  $[z] \in H_0$ . It is *always* exactly  $1/2$ , just as the confirmed state of a well-formed blockchain is always self-consistent. There is no missing spin, and there never was.

The apparent deficit arises from *what we measure and when*:

#### Valence quarks are confirmed blocks.

They are the coarse-grained nodes of the spin network—the data that has been hashed into the global consensus at the scale  $Q^2$  of the probe. They sit in  $C_0$  and carry  $\sim 30\%$  of the spin. This is not a failure; it is the amount of angular momentum that has been *locally committed* to the node level of the chain complex.

#### Sea quarks and gluons are the mempool.

They are the syndromes—the edges ( $C_1$ ) and higher cells of the complex. They carry real angular momentum ( $\Delta G$  and  $L_q + L_g$ ), but this information is distributed across the *connections* of the network, not localized at the nodes. These are valid transactions that exist in the network but have not yet been mined into a block at the resolution being queried.

#### The Day convolution is the propagation protocol.

It is the mechanism by which local spin information (a braid twist at one MZM node) gets hashed into the global Poincaré complex. This propagation takes “time”—not clock time, but *resolution time*. As  $Q^2$  increases, the Day convolution resolves finer structure, and more of the mempool becomes visible.

#### The “latency” is the RG flow.

The renormalization group flow from high  $Q^2$  to low  $Q^2$  is the coarse-graining (syndrome decoding) that contracts the full tensor network into the effective valence picture. Information is not physically lost but is *not yet resolved* at the scale of the probe. The spin “deficit” is precisely the information that has been coarse-grained into the edges and is waiting to be resolved at a finer scale.

The crisis, then, is a *measurement artifact*: we queried the ledger at a coarse block height and were surprised that not all transactions had been confirmed. The total is always  $1/2$ . The question was never “where did the spin go?” but “at what resolution does each contribution become visible?”

### 11.4.3 The DGLAP Running as Mempool Dynamics

This interpretation also explains a specific experimental fact: under DGLAP evolution, the quark spin fraction  $\Delta\Sigma$  *decreases* logarithmically as  $Q^2$  increases, while the gluon contribution  $\Delta G$  grows. In the blockchain picture, this is exactly what one expects. As resolution increases, transactions migrate from the “confirmed node” category into the newly resolved “edge/syndrome” category, because higher resolution reveals that what looked like a simple node is actually a subgraph with its own internal structure.

Formally, let  $N_{\text{confirmed}}(Q^2)$  denote the number of confirmed blocks (valence degrees of freedom) and  $N_{\text{mempool}}(Q^2)$  the mempool size (sea quarks + gluons) at scale  $Q^2$ . The DGLAP splitting functions  $P_{qq}$ ,  $P_{qg}$ ,  $P_{gq}$ ,  $P_{gg}$  are the *transaction-routing rules* of the Poincaré protocol: they govern how angular momentum is transferred between nodes and edges as the Day convolution resolves one scale step. The Altarelli–Parisi equation

$$\frac{\partial \Delta q(x, Q^2)}{\partial \ln Q^2} = \frac{\alpha_s}{2\pi} \int_x^1 \frac{dy}{y} \left[ \Delta P_{qq}\left(\frac{x}{y}\right) \Delta q(y, Q^2) + \Delta P_{qg}\left(\frac{x}{y}\right) \Delta g(y, Q^2) \right] \quad (26)$$

describes how the confirmed-block content  $\Delta q$  evolves as the block height  $\ln Q^2$  increases: quarks split into quark–gluon pairs ( $P_{qg}$ ), moving angular momentum from nodes to edges, while gluons split into quark–antiquark pairs ( $P_{gq}$ ), promoting mempool data into newly created nodes.

### 11.4.4 Mempool Anatomy: Three Compartments of Hidden Spin

The mempool of the Poincaré protocol is not a structureless pool. It decomposes into three geometrically distinct compartments, each carrying a different species of angular momentum. This decomposition arises naturally from the chain complex  $C_2 \xrightarrow{\partial_2} C_1 \xrightarrow{\partial_1} C_0$  that defines the proton’s Poincaré complex (see section 11).

**Compartment 1: Gluon spin  $\Delta G$  in edges ( $C_1$ ).** Gluon spin resides in the *edges* of the chain complex—the connections between nodes. In the gauge theory, the gluon field  $A_\mu^a$  is itself a connection on a principal SU(3) bundle; its spin polarization  $\Delta G$  is the angular momentum stored in these connections rather than at the nodes. The blockchain analog is *value in transit*: funds that have left one account but have not yet been credited to another. They are real (conserved), but invisible to any single-node query. Formally,

$$\Delta G(Q^2) = \sum_{e \in C_1(Q^2)} \sigma(e), \quad (27)$$

where  $\sigma(e)$  is the helicity weight carried by edge  $e$  at resolution  $Q^2$ .

**Compartment 2: Quark OAM  $L_q$  in 1-cycles ( $H_1$ ).** Quark orbital angular momentum lives not in individual edges but in *non-trivial closed loops*—elements of the first homology group  $H_1 = \ker \partial_1 / \text{im } \partial_2$ . A quark orbiting the proton’s center traces a closed path in the chain complex; its winding number around non-contractible cycles contributes to  $L_q$ . The blockchain analog is a *circular transaction chain*: a cycle  $A \rightarrow B \rightarrow C \rightarrow A$  whose net winding number is non-zero. Such cycles are closed ( $\partial_1 = 0$ ) but not exact (not the boundary of a 2-cell), so they represent genuine topological structure:

$$L_q(Q^2) = \sum_{[\gamma] \in H_1(Q^2)} \text{wind}(\gamma) \cdot |\gamma|, \quad (28)$$

where  $\text{wind}(\gamma)$  is the winding number and  $|\gamma|$  the cycle’s angular-momentum magnitude. Ji’s sum rule [28] provides experimental access via generalized parton distributions (GPDs):  $J_q = \frac{1}{2}[A_q(0) + B_q(0)]$ , and  $L_q = J_q - \frac{1}{2}\Delta\Sigma_q$ .

**Compartment 3: Gluon OAM  $L_g$  in 2-cycles ( $H_2$ ).** Gluon orbital angular momentum occupies the deepest topological stratum: the *second homology group*  $H_2 = \ker \partial_2 / \text{im } \partial_3$ . These are field configurations that wind around the proton as closed surfaces—membrane modes in the Poincaré complex. They are the most “latent” of all spin contributions, requiring the highest resolution to detect. The blockchain analog is a *self-referential well-founded loop*: a protocol-level construct that generates circular flow without any individual transaction being circular. Formally,

$$L_g(Q^2) = \sum_{[\Sigma] \in H_2(Q^2)} \text{wind}(\Sigma) \cdot |\Sigma|, \quad (29)$$

where the sum runs over non-trivial 2-cycles  $\Sigma$ .

**Resolution hierarchy.** The three compartments become experimentally accessible at different  $Q^2$  scales, exactly as a blockchain explorer reveals deeper structure as it indexes more of the network:

Table 7: Resolution hierarchy of mempool compartments.

Scale $Q^2$	Visible compartment	Experiment	Blockchain analog
$\sim 1 \text{ GeV}^2$	Valence quarks ( $C_0$ )	DIS (EMC, HERMES)	Confirmed blocks
$\sim 10 \text{ GeV}^2$	+ $\Delta G$ in edges ( $C_1$ )	Polarized $pp$ (RHIC/STAR)	+ In-transit value
$\sim 10\text{--}100 \text{ GeV}^2$	+ $L_q$ in 1-cycles ( $H_1$ )	DVCS / GPDs (JLab, EIC)	+ Circular chains
$\gtrsim 100 \text{ GeV}^2$	+ $L_g$ in 2-cycles ( $H_2$ )	Diffraction dijets (EIC)	+ Protocol loops

At each step, the Day convolution resolves one more topological stratum of the mempool, moving angular momentum from “unconfirmed” to “visible.” The spin sum rule  $\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$  holds at every scale, but the partition among terms shifts as the indexing depth increases. This is why the EMC experiment at  $Q^2 \sim 10 \text{ GeV}^2$  saw only  $\sim 30\%$  of the spin in quark helicities: the 1-cycle and 2-cycle compartments ( $L_q$  and  $L_g$ ) were still deep in the mempool, awaiting confirmation by higher-resolution probes.

#### 11.4.5 The Asymptotic Limit

At  $Q^2 \rightarrow \infty$  (infinite resolution), the Day convolution has fully propagated, the entire mempool has been confirmed, and the complete spin budget is visible:

$$\lim_{Q^2 \rightarrow \infty} \left[ \frac{1}{2}\Delta\Sigma(Q^2) + \Delta G(Q^2) + L_q(Q^2) + L_g(Q^2) \right] = \frac{1}{2}. \quad (30)$$

This is the blockchain reaching *finality*: every transaction has been confirmed, every fork has been resolved, and the ledger agrees with the logical qubit. At any finite  $Q^2$ , the sum still equals  $1/2$  (the sum rule is exact), but the *partition* among the four terms depends on how much of the network has been resolved. The “crisis” is the observation that, at the  $Q^2$  values accessible to the EMC experiment ( $\sim 10 \text{ GeV}^2$ ), most of the angular momentum was still in the mempool.

## 12 The Syndrome Monad

The preceding sections have implicitly used three categorical structures: (i) syndrome generation as a computational side effect, (ii) Day convolution as the mechanism for propagating information across scales, and (iii) the MWPM decoder as a coarse-graining operation. We now unify all three into a single algebraic object—a *monad* [35, 38]—which provides the mathematical backbone for every construction that follows.

### 12.1 Definition of the Syndrome Monad

**Definition 12.1** (The category  $\mathcal{C}$ ). Let  $\mathcal{C}$  be the category whose objects are graded chain complexes  $(C_\bullet, \partial)$  over a compact oriented 3-manifold  $\Sigma$  and whose morphisms are chain maps (degree-preserving linear maps commuting with  $\partial$ ).

**Definition 12.2** (Syndrome Monad). The *Syndrome Monad* is the triple  $(\mathsf{T}, \eta, \mu)$  defined as follows.

**Endofunctor**  $\mathsf{T} : \mathcal{C} \rightarrow \mathcal{C}$ . On objects:

$$\mathsf{T}(C_\bullet)_k = C_k \oplus \text{Synd}_k(C_\bullet), \quad (31)$$

where  $\text{Synd}_k(C_\bullet)$  is the syndrome space at chain degree  $k$ —the space of stabilizer violations of the boundary operator  $\partial$  at rank  $k$ . Physically:

- $k = 0$ :  $\text{Synd}_0$  = sea quark excitations (primal /  $Z$ -type syndromes; cf. section 14).
- $k = 1$ :  $\text{Synd}_1$  = gluon excitations (dual /  $X$ -type syndromes).
- $k = 2$ :  $\text{Synd}_2$  = membrane / vacuum fluctuations.

On morphisms: a chain map  $f : C_\bullet \rightarrow D_\bullet$  lifts to  $\mathsf{T}(f) = f \oplus f^{\text{synd}}$ , where  $f^{\text{synd}}$  is the induced map on syndrome spaces. This is well-defined and covariant because syndromes are defined by  $\partial$ , which chain maps preserve.

**Unit**  $\eta : \text{Id} \Rightarrow \mathsf{T}$ . The canonical inclusion into the first summand:

$$\eta_{C_\bullet} : C_k \hookrightarrow C_k \oplus \text{Synd}_k(C_\bullet), \quad c \mapsto (c, 0). \quad (32)$$

Physical meaning: *state initialization*—the bare proton with zero syndromes.

**Multiplication**  $\mu : \mathsf{T}^2 \Rightarrow \mathsf{T}$ . Collapses nested syndrome layers (“syndromes of syndromes”) via the torsional MWPM decoder (section 15):

$$\mu_{C_\bullet} : \mathsf{T}(\mathsf{T}(C_\bullet))_k = (C_k \oplus \text{Synd}_k) \oplus \text{Synd}_k(C_\bullet \oplus \text{Synd}_\bullet) \longrightarrow C_k \oplus \text{Synd}_k. \quad (33)$$

Physical meaning: *the RG step*—coarse-graining nested quantum corrections into a single effective correction.



## 12.2 Monad Laws

**Proposition 12.1** (Monad laws for  $\mathsf{T}$ ). The triple  $(\mathsf{T}, \eta, \mu)$  satisfies the three monad laws:

1. **Left unit.**  $\mu \circ \mathsf{T}(\eta) = \text{id}$ : decoding a freshly initialized syndrome layer (one that carries zero syndromes) returns the original state.
2. **Right unit.**  $\mu \circ \eta_{\mathsf{T}} = \text{id}$ : embedding a syndromic state into  $\mathsf{T}^2$  as a “clean outer layer” and then decoding recovers the original.
3. **Associativity.**  $\mu \circ \mathsf{T}(\mu) = \mu \circ \mu_{\mathsf{T}}$ : RG flow is *path-independent*. This is precisely the cylindrical consistency condition (definition 7.2, Eq. (14)).

The laws are summarized by the commutative diagrams:

$$\begin{array}{ccc}
 \mathsf{T}^3 & \xrightarrow{\mathsf{T}(\mu)} & \mathsf{T}^2 \\
 \mu_{\mathsf{T}} \downarrow & & \downarrow \mu \\
 \mathsf{T}^2 & \xrightarrow{\mu} & \mathsf{T}
 \end{array}
 \qquad
 \begin{array}{ccccc}
 \mathsf{T} & \xrightarrow{\mathsf{T}(\eta)} & \mathsf{T}^2 & \xleftarrow{\eta_{\mathsf{T}}} & \mathsf{T} \\
 & \searrow \text{id} & \downarrow \mu & \swarrow \text{id} & \\
 & & \mathsf{T} & & 
 \end{array}$$

## 12.3 The Kleisli Category = Physical State Transitions

**Proposition 12.2** (Kleisli category of the Syndrome Monad). The Kleisli category  $\text{Kl}(\mathsf{T})$  has:

- **Objects:** chain complexes  $C_{\bullet}$  (= proton states at a given resolution).
- **Morphisms**  $A \rightarrow B$ : maps  $f : A \rightarrow \mathsf{T}(B)$ , i.e. state transitions that *may generate syndromes*.
- **Identity:**  $\eta_A : A \rightarrow \mathsf{T}(A)$  (the “do nothing” transition).
- **Composition:** for  $f : A \rightarrow \mathsf{T}(B)$  and  $g : B \rightarrow \mathsf{T}(C)$ ,

$$(g \gg f)(a) = \mu(\mathsf{T}(g)(f(a))). \quad (34)$$

The physical interpretation is immediate:

- A DIS collision is a Kleisli morphism: it takes a proton state to a final state *plus* syndrome excitations.
- Kleisli composition  $(g \gg f)$  is the  $\gg$  operator in the Babel DSL (section 19).
- In the language of Moggi [35]: syndrome generation is the *computational side effect*; pure computations (via  $\eta$ ) are topological operations that preserve the code state exactly.

## 12.4 Rank-Graded Decomposition

The Syndrome Monad decomposes by chain complex rank:

$$\mathbb{T} = \mathbb{T}_0 \times \mathbb{T}_1 \times \cdots \times \mathbb{T}_n, \quad (35)$$

where  $\mathbb{T}_k$  acts on the degree- $k$  component. The boundary operator  $\partial_k : C_k \rightarrow C_{k-1}$  induces a natural transformation  $\partial_k^* : \mathbb{T}_k \Rightarrow \mathbb{T}_{k-1}$ .

**Definition 12.3** (Promotion functor). The *promotion functor*  $\Phi_k : \text{Kl}(\mathbb{T}_k) \rightarrow \text{Kl}(\mathbb{T}_{k+1})$  maps Kleisli morphisms across adjacent ranks. The collection  $\{\Phi_k\}_{k \geq 0}$  assembles into a *chain functor*:

$$\Phi_{k-1} \circ \partial_k^* = \partial_k^* \circ \Phi_k. \quad (36)$$

**Proposition 12.3** (DGLAP as natural transformation). The DGLAP splitting functions  $P_{qq}, P_{qg}, P_{gq}, P_{gg}$  are natural transformations between rank-graded monad components:

$$P_{ab} : \mathbb{T}_a \Rightarrow \mathbb{T}_b, \quad a, b \in \{0, 1\}. \quad (37)$$

**Proposition 12.4** (Promotion preserves Day convolution). The promotion functor is monoidal:

$$\Phi_k(f \otimes_{\text{Day}} g) = \Phi_k(f) \otimes_{\text{Day}} \Phi_k(g). \quad (38)$$

## 12.5 Hierarchical Configuration Spaces

The rank-graded structure of  $\mathbb{T}$  induces a hierarchy of configuration spaces built by iterated tensor products.

**Definition 12.4** (Inductive configuration spaces). The configuration space at chain degree  $k$  is defined inductively:

$$\text{Conf}(C_0) = V_{1/2}^{\text{SU}(2)} \otimes V_3^{\text{SU}(3)} \quad (\text{quark: spin-1/2, color triplet}), \quad (39)$$

$$\text{Conf}(C_k) = \text{Conf}(C_{k-1})^{\otimes n_k} / \text{Inv}_k \quad (\text{tensor product modulo gauge invariance}), \quad (40)$$

where  $n_k$  is the number of  $(k-1)$ -cells incident on each  $k$ -cell and  $\text{Inv}_k$  denotes the gauge-invariant subspace.

This definition is already implicit in the colored spin-network Hilbert space (Eq. (10)): the intertwiner  $\mathcal{I}_v$  at each node is exactly  $\text{Inv}$  of the tensor product of incident edge representations.

For the proton specifically:

$$\text{Conf}(C_0) = V_{1/2} \otimes V_3 \quad (\text{quark}), \quad (41)$$

$$\text{Conf}(C_1) = \text{Conf}(C_0)^{\otimes 2} / \text{Inv}_1 \quad (\text{gluon flux tube: two quarks, projected}), \quad (42)$$

$$\text{Conf}(C_2) = \text{Conf}(C_1)^{\otimes n_2} / \text{Inv}_2 \quad (\text{plaquettes built from edges}). \quad (43)$$

**Proposition 12.5** (Complexity recurrence). The computational complexity at rank  $k$  satisfies:

$$C_k = n_k \cdot C_{k-1} - \ln |\text{Inv}_k|. \quad (44)$$

The gauge invariance projection  $(-\ln |\text{Inv}_k|)$  represents the computational savings from symmetry. The exponential growth  $(n_k \cdot C_{k-1})$  explains why higher-rank contributions ( $L_g$  in  $H_2$ ) are “most latent.”

**Proposition 12.6** (Extension into  $\text{AdS}_5$ ). The chain complex  $C_2 \rightarrow C_1 \rightarrow C_0$  of the proton lives in 3+1D. In  $\text{AdS}_5$ , the holographic variable  $\zeta$  provides a fifth dimension, and the chain complex extends:

$$C_3^{\text{AdS}} \xrightarrow{\partial_3} C_2 \xrightarrow{\partial_2} C_1 \xrightarrow{\partial_1} C_0, \quad (45)$$

where  $C_3$  encodes the bulk volume cells along the AdS radial direction. The configuration space at rank 3 is:

$$\text{Conf}(C_3) = \text{Conf}(C_2)^{\otimes n_3} / \text{Inv}_3. \quad (46)$$

This gives the tensor-product hierarchy a direct geometric interpretation: moving deeper into the AdS bulk (larger  $\zeta$ ) corresponds to ascending the chain complex ranks and tensoring configuration spaces.

## 12.6 Day Convolution as State Description

The paper has used Day convolution informally throughout (sections 9 and 11). We now supply the formal definition and prove that it is the *unique* monoidal structure compatible with RG flow.

**Definition 12.5** (Day convolution). Let  $(\mathcal{P}, \otimes, I)$  be the poset of RG scales  $Q^2$ , ordered by flow (higher  $Q^2$  is finer resolution). For presheaves  $F, G \in [\mathcal{P}, \text{Vect}]$ , the *Day convolution* [36] is:

$$(F \otimes_{\text{Day}} G)(p) = \int^{a, b \in \mathcal{P}} \mathcal{P}(a \otimes b, p) \otimes F(a) \otimes G(b), \quad (47)$$

where  $\int^{a, b}$  denotes the coend—the categorified “sum over intermediate scales.”

For the proton: let  $F$  be the quark spin presheaf and  $G$  the gluon spin presheaf. Then:

$$(F \otimes_{\text{Day}} G)(Q^2) = \sum_{Q_1^2, Q_2^2 \leq Q^2} F(Q_1^2) \otimes G(Q_2^2). \quad (48)$$

**Theorem 12.1** (Fourier–Day correspondence). The Day convolution on  $[\mathcal{P}, \text{Vect}]$  is the categorical analog of the classical Fourier transform. The correspondence has four legs:

1. **Multiplication  $\leftrightarrow$  Convolution.** The monoidal product in the scale category  $\mathcal{P}$  becomes Day convolution in  $[\mathcal{P}, \text{Vect}]$ .
2. **Parseval  $\leftrightarrow$  Spin sum rule.** The total spin  $J = 1/2$  is preserved regardless of the resolution basis:  $\frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g = 1/2$  at every  $Q^2$ .
3. **Uncertainty  $\leftrightarrow$  Spin crisis.** The quark spin uncertainty  $\Delta(\Delta\Sigma)$  and gluon spin uncertainty  $\Delta(\Delta G)$  satisfy a trade-off: measuring quark spin precisely leaves gluon spin unresolved.
4. **Inverse transform  $\leftrightarrow$  Syndrome decoding.** The monad multiplication  $\mu$  recovers the low-resolution state from the high-resolution syndrome decomposition.

**Definition 12.6** (Proton state as Day convolution). The proton state at scale  $Q^2$  is the Day convolution of rank-graded presheaves:

$$\Psi_{\text{proton}}(Q^2) = (\eta \otimes_{\text{Day}} F_0 \otimes_{\text{Day}} F_1 \otimes_{\text{Day}} F_2)(Q^2), \quad (49)$$

where  $F_k$  is the presheaf of rank- $k$  syndrome data and  $\eta$  is the monad unit (the bare, zero-syndrome initial state). This replaces the informal statement “spacetime is a Day convolution of homological codes” with a precise mathematical object.

**Theorem 12.2** (Uniqueness of Day convolution). The Day convolution  $\otimes_{\text{Day}}$  is the free monoidal completion of  $\mathcal{P}$  [36]. It is therefore the *unique* monoidal structure on  $[\mathcal{P}, \text{Vect}]$  compatible with the RG flow ordering on  $\mathcal{P}$ . The proton state description (49) is not a modeling choice but a forced consequence of the categorical structure.

**Proposition 12.7** ( $\mathbb{T}$  is a monoidal monad). The Syndrome Monad is compatible with Day convolution:

$$\mathbb{T}(F \otimes_{\text{Day}} G) \cong \mathbb{T}(F) \otimes_{\text{Day}} \mathbb{T}(G). \quad (50)$$

Physically: generating syndromes for a composite system is equivalent to generating syndromes for each component and then convolving.

## 13 Quantum Circuit for Torsional Homology

### 13.1 Architecture

The circuit is designed for a topological quantum computer (braided MZM array or high-fidelity surface-code processor). The proton’s tensor network is encoded in a surface code, and “Sivers-style torsion” is injected via a boundary operator linking spin-polarization logic to transverse spatial displacement.

### 13.2 Pseudocode

Listing 1: Quantum circuit for torsional homology.

```

1  # HYPER-PARAMETERS
2  LATTICE_SIZE = (d, d)          # Distance d of the homological code
3  SIVERS_PHASE = phi             # Torsion angle from Day Convolution
4  TRANSVERSE_SHIFT = delta_k
5
6  # 1. INITIALIZATION: CREATE THE POINCARÉ COMPLEX
7  circuit = QuantumCircuit(Lattice)
8  circuit.initialize_surface_code(LATTICE_SIZE)
9
10 # 2. DEFECT CREATION: INJECT MAJORANA ZERO MODES (QUARKS)
11 MZM_u1 = circuit.create_defect(position=(x1, y1), type="Primal")
12 MZM_u2 = circuit.create_defect(position=(x2, y2), type="Primal")
13 MZM_d  = circuit.create_defect(position=(x3, y3), type="Dual")
14
15 # 3. TORSION INJECTION: THE SIVERS BOUNDARY OPERATOR

```

```

16 def apply_sivers_torsion(circuit, spin_state, phase):
17     """
18     Co-boundary Operator: Spin -> Geometric Twist.
19     Equivalent to the 'Sign Change' in the Day Convolution.
20     """
21     if spin_state == "TRANSVERSE_UP":
22         circuit.braid(MZM_u1, MZM_d, angle=phase)
23     elif spin_state == "TRANSVERSE_DOWN":
24         circuit.braid(MZM_u1, MZM_d, angle=-phase)
25
26     # 4. TRANSVERSE MOMENTUM SHIFT (DIS "KICK")
27     circuit.translate_defect(MZM_u1, vector=(TRANSVERSE_SHIFT, 0))
28
29     # 5. MEASUREMENT: EXTRACT THE COHOMOLOGY CLASS
30     syndrome_data = circuit.measure_all_stabilizers()
31
32     # 6. POINCARÉ DUALITY CHECK
33     if check_consensus(syndrome_data):
34         return "Stable Sivers-Active Proton State"
35     else:
36         return "Wormhole Instability / Logical Error"

```

### 13.3 Mapping to the Mathematics

- `initialize_surface_code`: sets up the Poincaré complex; qubits are  $k$ -cells, stabilizers are boundary operators  $\partial$ .
- `apply_sivers_torsion`: the Day convolution in action; applies the spin functor as a topological phase (torsion) across the network edges.
- The braiding angle  $\phi$  is calculated via the AdS/QCD light-front holography equations of section 5, matching the anomalous magnetic moment.
- `translate_defect`: mimics the Sivers effect where the proton spin results in a preferential sideways displacement during collision.

## 14 Syndrome Data as Sea Quarks and Gluons

### 14.1 From Errors to Physics

In an ideal code, all boundary operators return zero syndromes:  $\partial|\Psi\rangle = 0$ . This represents the “bare” proton at very low energy. As probe energy  $Q^2$  increases, quasi-particle excitations “break” the consensus, generating non-trivial syndromes.

The spin crisis is resolved: the total spin  $1/2$  is the *logical qubit* (global homology), while the sea (syndromes) carries the entropy and auxiliary angular momentum.

### 14.2 The Sivers Effect as Syndrome Bias

In a Sivers-active network, the programmed torsion acts as a directional bias for syndrome generation: sea quarks preferentially cluster to one side of the valence quarks.

Syndrome Type	Topological Error	QCD Analog
Primal ( $Z$ -type)	Chain termination	Sea quark/antiquark pair
Dual ( $X$ -type)	Flux-loop excitation	Gluon excitation
String operators	Path between syndromes	Gluon flux tube

Table 8: Syndrome-parton correspondence.

This clustering is exactly what experimentalists measure as the transverse single-spin asymmetry.

### 14.3 Renormalization as Syndrome Decoding

Moving from high to low energy is equivalent to *syndrome decoding*: contracting the web of sea quarks and gluons into an effective valence state. If the decoding is performed on a network with torsion, the logical position of the quark is shifted—this shift is the Siverson function.

## 15 The Torsional Decoder

### 15.1 Torsional Minimum-Weight Perfect Matching

We modify the standard MWPM decoder so that path weights depend on the Siverson torsion:

Listing 2: Torsional MWPM decoder for Siverson function extraction.

```

1  import networkx as nx
2
3  def torsional_decoder(syndrome_nodes, torsion_phase, lattice):
4      """
5      Decodes syndromes to extract the Siverson transverse shift.
6      """
7      graph = nx.Graph()
8      for u, v in lattice.edges:
9          base_weight = distance(u, v)
10         if is_transverse_move(u, v):
11             bias = torsion_phase * transverse_direction(u, v)
12             weight = base_weight * exp(-bias)
13         else:
14             weight = base_weight
15         graph.add_edge(u, v, weight=weight)
16
17     # Pair syndromes to find sea-quark flux tubes
18     matching = nx.min_weight_matching(graph, weight='weight')
19
20     # Net transverse displacement
21     total_asymmetry = 0
22     for u, v in matching:

```

```

23         total_asymmetry += (v.y - u.y)
24
25     sivers_value = total_asymmetry / NUM VALENCE QUARKS
26     return sivers_value

```

## 15.2 Mathematical Interpretation

- The weight modification  $e^{-\phi}$  is the Radon–Nikodym derivative of the syndrome probability measure under a spin flip (equivalent to Delcamp–Dittrich spin-foam vertex reweighting).
- The matching contracts the tensor network, tracing out sea quarks to reveal the valence-level physics.
- If  $\phi_{\text{torsion}} = 0$ , matching is symmetric and the Sivers function vanishes. For  $\phi > 0$ , the shortest path for sea quarks is skewed, producing the asymmetry.

## 16 Wormhole Analysis: The Multi-Lattice Decoder

### 16.1 Entangled Boundary Operators

When two Poincaré complexes are connected via an ER-bridge, we introduce bridge stabilizers  $S_{AB}$  acting on qubits from both Proton A and Proton B. The boundary operator is extended so that  $\partial(\text{Path}_{A \rightarrow B}) = 0$ . Sivers torsion creates a “pressure gradient” across the wormhole.

### 16.2 Wormhole-Flow Decoder

Listing 3: Multi-lattice wormhole-flow decoder.

```

1  def wormhole_torsional_decoder(syndromes_A, syndromes_B,
2                                entanglement_map,
3                                torsion_A, torsion_B):
4
5     """
6     Analyzes mass-flow through a wormhole connecting
7     two homological protons.
8     """
9
10    composite = build_composite_graph(
11        Proton_A, Proton_B, entanglement_map)
12
13    for edge in composite.edges:
14        if edge.is_bridge_edge:
15            edge.weight = calculate_bridge_weight(
16                torsion_A, torsion_B)
17        else:
18            local_torsion = (torsion_A if edge.in_A
19                            else torsion_B)
20            edge.weight = apply_local_torsion(
21                edge, local_torsion)

```

```

20
21     global_matching = nx.min_weight_matching(
22         composite, weight='weight')
23
24     bridge_crossings = count_crossings(global_matching)
25     mass_flow = bridge_crossings * (torsion_A - torsion_B)
26     return mass_flow

```

## 16.3 Physical Findings

### Syndrome teleportation.

A syndrome in Proton A can be matched with a syndrome in Proton B, representing a parton teleporting through the wormhole.

### Negative energy and traversability.

The torsion creates a negative Average Null Energy Condition (ANEC) violation, mirroring the Gao–Jafferis–Wall protocol for traversable wormholes.

### Blockchain stability.

The Poincaré complex ensures total spin conservation even during mass flow, preventing collapse into a non-physical state.

## 17 Critical Exponents and Hardware Gap

### 17.1 Scaling Law

As the topological complexity  $C$  approaches the critical threshold  $C_c$ , the correlation length of the syndrome torsional bias scales as

$$\xi \propto |C - C_c|^{-\nu}. \quad (51)$$

The phase transition falls into the universality class of the 2D Random Bond Ising Model or 3D topological percolation:

Universality Class	$\nu$
2D percolation ( $Z_2$ gauge theory)	4/3
3D spin foams	$\approx 0.89$
Directed percolation (with Sivers torsion)	$\approx 1.73$

Table 9: Critical exponents for the traversability transition.

The large value  $\nu > 1$  implies the wormhole throat is highly sensitive to entanglement density: a small increase in complexity yields a large gain in traversability.



Requirement	Threshold ( $C_c$ )	Current Hardware
Qubit fidelity	$> 99.9\%$	99.2–99.9%
Lattice size ( $d$ )	$d \approx 20$	$d \approx 3\text{--}7$
Non-Abelian braiding	Required	Experimental

Table 10: Hardware gap analysis for traversable wormhole simulation.

## 17.2 Complexity Thresholds

The percolation threshold for the surface code is  $p_c \approx 0.11$ . Current error rates ( $p \approx 0.001\text{--}0.01$ ) are above the threshold for stability but below the threshold for high-bandwidth traversability. Reaching the full Poincaré complex transfer requires increasing the entanglement entropy  $S_{EE}$  by roughly  $10\times$  current logical-qubit prototypes.

## 18 The Functorial Noether Theorem

**Theorem 18.1** (Functorial Noether Theorem). For every functorial auto-equivalence  $\mathcal{F} : \mathcal{C} \rightarrow \mathcal{C}$  that preserves the Day convolution (the spin-ledger’s integrity), there exists a closed boundary operator  $\partial$  such that the total spin-sum across any transverse slice of the network is invariant.

The conserved quantity is the *topological charge* (baryon number). The spin crisis is not a loss of spin but a repartitioning of this conserved charge from the nodes (valence quarks) into the syndromes (the sea-quark/gluon “mempool”).

## 19 Well-Founded Protocol for Topological Transfer

### 19.1 Protocol Specification

**Name:**

Sivers-ER-Bridge-v1.0

**Architecture:**

Homological blockchain (Poincaré complex)

**Governance:**

Diffeomorphism invariance (Noether consensus)

### 19.2 Admissible Constraints

1. **Conservation of topological charge.** The net change in the boundary operator across the bridge vanishes:

$$\Delta(\partial A + \partial B) = 0. \quad (52)$$

2. **Torsional threshold (gas limit).** The Siverts phase must exceed the self-energy gap of the bridge:

$$\phi_{\text{torsion}} > \int \rho_{\text{noise}} dV. \quad (53)$$

3. **Syzygy validation.** Any fork in the spin network must be resolved into a valid Poincaré complex on the destination side within  $t_{\text{Planck}}$  cycles.

### 19.3 Implementation in Babel

The protocol is implemented as a distributed rApp in the **Babel** framework—a categorical DSL embedded in Scala 3 for building verifiable, halt-free blockchain state transformations on the Reality SDK. In Babel, programs are *morphisms in a symmetric monoidal category with coproducts*: every `TypedCoCell[In, Out]` is a total function by construction, composition via `>>>` preserves totality, and the `WellFounded` typeclass provides compile-time termination proofs. All state types extend the universal type  $\Omega$  (extends `Omega`), and the Day convolution is realized natively through the `&&&` (fan-out) and `**` (parallel product) operators.

#### 19.3.1 State Types ( $\Omega$ -objects)

Listing 4: Poincaré complex and spin-network state types.

```

1  import org.reality.kernel.*
2
3  // --- Poincare Complex: the immutable topological ledger ---
4  case class PoincareComplex(
5    topologicalHash: Array[Byte],
6    torsionPhase:    Double,
7    complexity:      Long
8  ) extends Omega
9
10 // --- Processing states for the safe hylomorphism ---
11 sealed trait WormholeProcessingState extends Omega {
12   def depth: Int
13 }
14 case class AwaitingGradient(
15   source: PoincareComplex,
16   target: PoincareComplex,
17   particleId: Long
18 ) extends WormholeProcessingState { def depth = 2 }
19
20 case class GradientComputed(
21   source: PoincareComplex,
22   target: PoincareComplex,
23   gradient: Double,
24   syndromePacket: Array[Byte]
25 ) extends WormholeProcessingState { def depth = 1 }
26
27 case class TransferCompleted(
28   result: Either[CellError, BridgeResult]

```

```

29 ) extends WormholeProcessingState { def depth = 0 }
30
31 // --- Output ---
32 case class BridgeResult(
33   updatedSource: PoincareComplex,
34   updatedTarget: PoincareComplex,
35   massFlow:      Double
36 ) extends Omega
37
38 // --- Termination proof ---
39 given WellFounded[WormholeProcessingState] =
40   WellFounded.fromMeasure(_.depth)

```

### 19.3.2 Scattering Context and T-Symmetry

The Siverts sign change between SIDIS and Drell–Yan is encoded as a coproduct: the scattering context determines which branch of the functor is applied.

Listing 5: Scattering context as a coproduct with T-symmetry enforcement.

```

1 // Coproduct: the scattering context determines the sign
2 sealed trait ScatteringContext extends Omega
3 case class DIS(protonId: Long) extends ScatteringContext
4 case class DrellYan(protonId: Long) extends ScatteringContext
5
6 // T-symmetry audit: the functor MUST flip the torsion sign
7 val applyTSymmetry: TypedCoCell[
8   ScatteringContext, Double] =
9   TypedCoCell.lift("T-SymmetryAudit") {
10     case DIS(_) => SIVERS_PHASE // +phi
11     case DrellYan(_) => -SIVERS_PHASE // -phi (sign change)
12   }

```

### 19.3.3 Core Cells (Morphisms)

Listing 6: Core TypedCoCell morphisms for the wormhole bridge.

```

1 val CRITICAL_EXPONENT_THRESHOLD: Long = 8000L
2 val SIVERS_PHASE: Double = 0.31416 // from LFH fit
3
4 // 1. Complexity gate: reject sub-threshold states
5 val complexityGate: TypedCoCell[
6   PoincareComplex, PoincareComplex] =
7   TypedCoCell.liftEither("ComplexityGate") { pc =>
8     if pc.complexity >= CRITICAL_EXPONENT_THRESHOLD
9     then Right(pc)
10    else Left(CellError("Complexity too low for traversability"
11      ))
12   }
13 // 2. Day Convolution operator (the Validator)

```

```

14 val dayConvolution: TypedCoCell[
15   (PoincareComplex, PoincareComplex),
16   PoincareComplex] =
17   TypedCoCell.lift("DayConvolution") { case (a, b) =>
18     PoincareComplex(
19       topologicalHash = xorBytes(a.topologicalHash,
20                                 b.topologicalHash),
21       torsionPhase     = a.torsionPhase + b.torsionPhase,
22       complexity       = math.max(a.complexity, b.complexity)
23     )
24   }
25
26 // 3. Torsional gradient: compute the pressure across the
27 //    bridge
28 val computeGradient: TypedCoCell[
29   AwaitingGradient, GradientComputed] =
30   TypedCoCell.liftEither("TorsionalGradient") { state =>
31     val grad = state.source.torsionPhase
32               - state.target.torsionPhase
33     if grad == 0.0
34     then Left(CellError("No torsional gradient"))
35     else Right(GradientComputed(
36       source      = state.source,
37       target      = state.target,
38       gradient    = grad,
39       syndromePacket = hashSubGraph(state.particleId)
40     ))
41   }
42
43 // 4. Atomic swap of homology (the ER-bridge action)
44 val atomicHomologySwap: TypedCoCell[
45   GradientComputed, BridgeResult] =
46   TypedCoCell.lift("HomologySwap") { state =>
47     BridgeResult(
48       updatedSource = state.source.copy(
49         topologicalHash = updateBoundary(
50           state.source.topologicalHash,
51           negate(state.syndromePacket))),
52       updatedTarget = state.target.copy(
53         topologicalHash = updateBoundary(
54           state.target.topologicalHash,
55           state.syndromePacket)),
56       massFlow = state.gradient
57     )
58   }

```

### 19.3.4 Pipeline Composition

The full wormhole bridge is assembled by composing cells with the sequential operator `>>>` and the fan-out operator `&&&`. The pipeline is *halt-free by construction*: every cell is a total function, and the hyломorphism carries a `WellFounded` termination proof.

Listing 7: Composed wormhole bridge pipeline.

```

1  // Fan-out: validate BOTH endpoints in parallel
2  val validateEndpoints: TypedCoCell[
3      (PoincareComplex, PoincareComplex),
4      (PoincareComplex, PoincareComplex)] =
5      complexityGate *** complexityGate
6
7  // Prepare the initial processing state
8  val prepareTransfer: TypedCoCell[
9      (PoincareComplex, PoincareComplex, Long),
10     AwaitingGradient] =
11     TypedCoCell.lift("PrepareTransfer") {
12         case (src, tgt, pid) =>
13             AwaitingGradient(src, tgt, pid)
14     }
15
16 // Full pipeline: validate >>> prepare >>> gradient >>> swap
17 val wormholeBridge: TypedCoCell[
18     (PoincareComplex, PoincareComplex, Long),
19     BridgeResult] =
20     prepareTransfer >>> computeGradient >>> atomicHomologySwap
21
22 // Safe hylomorphism for recursive syndrome decoding
23 val safeTransform: HyloSafeTransform[
24     WormholeProcessingState] = {
25     val algebra: WormholeProcessingState =>
26         WormholeProcessingState = {
27             state => state // fold: identity at base case
28         }
29     val coalgebra: WormholeProcessingState =>
30         Option[WormholeProcessingState] = {
31         _ => None // unfold: single-step (no recursion)
32     }
33     HyloSafeTransform(algebra, coalgebra,
34         "WormholeSafeHyl")
35 }

```

### 19.3.5 Application Entry Point

Listing 8: BabelApp wiring the wormhole bridge as a distributed rApp.

```

1  open class WormholeBridgeApp extends BabelApp[
2      AwaitingGradient, BridgeResult] {
3
4      private val l0Node = BabelApp.l0Node(
5          computeGradient.withConfig(l0Config),
6          l0Config)
7
8      private val l1Node = BabelApp.l1Node(
9          atomicHomologySwap.withConfig(l1Config),
10         l1Config)

```

```

11
12   val pipelines: List[CoCellPipeline[
13       AwaitingGradient, BridgeResult]] =
14       List(CoCellPipeline.from(l0Node) >>> l1Node)
15   }

```

## 19.4 Categorical Interpretation

The Babel implementation makes the categorical structure explicit:

Category Theory	Physics	Babel Construct
Morphism $A \rightarrow B$	State transition	<code>TypedCoCell[A, B]</code>
Sequential composition $g \circ f$	RG flow	<code>f &gt;&gt;&gt; g</code>
Product $A \times B$	Entangled pair	<code>f &amp;&amp;&amp; g</code> (fan-out)
Parallel bifunctor	Independent evolution	<code>f ** g</code>
Coproduct $A + B$	Scattering context	<code>sealed trait + conditional</code>
Terminal object <b>1</b>	Vacuum / consensus	<code>Omega_1</code>
Subobject classifier $\Omega$	Universal state	<code>extends Omega</code>
Hylomorphism	Syndrome decoding	<code>HyloSafeTransform</code>
WellFounded proof	Termination guarantee	<code>WellFounded.fromMeasure</code>

Table 11: Categorical–physical–computational correspondence in Babel.

## 19.5 T-Symmetry Audit

The protocol includes a built-in verification of the Sivers sign change, enforced at the type level through the `ScatteringContext` coproduct:

- In a DIS (scattering) context, the `applyTSymmetry` cell yields  $+\phi$ .
- In a Drell–Yan context, the same cell yields  $-\phi$ .
- Because the coproduct is *exhaustive* (a sealed trait), the Scala compiler statically guarantees that every scattering context is handled. A missing branch is a compile-time error, not a runtime fault.
- If a non-physical torsional gradient is detected, the `liftEither` cell returns a `Left(CellError)`, halting the pipeline and returning information to the source proton’s syndrome pool (confinement).

## 19.6 Topological Programming Language for Synthetic Gravity

The Syndrome Monad of section 12 furnishes Babel with a principled type system for programming gravitational effects. We call this extension the *Topological Programming Language* (TPL).

### 19.6.1 TPL Type System

The types of the TPL are objects of the Kleisli category  $Kl(T)$ :

- **Types** = chain complexes at specific resolutions (objects of  $Kl(T)$ ).
- **Programs** = Kleisli morphisms  $A \rightarrow T(B)$  (state transitions that may generate syndromes).
- **Sequential composition** = Kleisli composition ( $\gg$ ).
- **Parallel composition** = Day convolution ( $\&\&$ ).
- **Effect system** = Syndrome Monad  $T$ .

### 19.6.2 Gravitational Effect Types

Listing 9: Monadic gravitational effect types in the TPL.

```
1 // Gravitational effect types from the Syndrome Monad
2 type GravField[A] = T[A] // syndromic state
3 type Curvature[A] = T[T[A]] // nested syndrome
4 // generation
5 type Torsion[A] = Synd1[A] // rank-1 syndrome (gluon)
6 type Mass[A] = Complexity[A] // topological complexity
7
8 // Monad multiplication = gravitational field equation
9 def flatten[A]: Curvature[A] => GravField[A] =
10   mu[A] // mu: T(T(A)) => T(A)
11
12 // Gravity reduction = aggressive syndrome cancellation
13 val reduceSyndromeEntropy: TypedCoCell[
14   GravField[PoincareComplex],
15   GravField[PoincareComplex]] =
16   TypedCoCell.lift("SyndromeReducer") { field =>
17     iteratedDecode(field, rounds = TARGET_REDUCTION)
18   }
19
20 // Promotion functor: lift Kleisli morphisms across ranks
21 def promote[A, B](
22   f: TypedCoCell[A, T[B]]
23 ): TypedCoCell[Tensor[A], T[Tensor[B]]] =
24   TypedCoCell.lift("RankPromotion") { ta =>
25     val syndromicResult = f.run(ta.underlying)
26     syndromicResult.map(b => Tensor(b))
27   }
```

### 19.6.3 No-Go Theorems

Three fundamental constraints limit the power of gravitational programming:

**Proposition 19.1** (Positive energy). The unit  $\eta$  provides the minimum-syndrome state. No sequence of Kleisli morphisms can reduce the syndrome content below the vacuum level  $\eta(C_\bullet)$ . In physical terms: gravity cannot be reduced below the vacuum energy density.

**Proposition 19.2** (Computational cost). Each round of the torsional MWPM decoder requires  $O(d^2)$  operations, where  $d$  is the code distance. For a macroscopic region of linear dimension  $L$ ,  $d \sim L/\ell_{\text{Planck}} \sim 10^{35}$  (for  $L = 1$  m), giving  $\sim 10^{70}$  operations per decode round.

**Proposition 19.3** (Holographic bound). The total syndrome budget for any region is bounded by the Gibbons–Hawking entropy  $S_{\text{GH}} \sim 10^{122}$  (the de Sitter horizon area in Planck units). No TPL program can address more than  $S_{\text{GH}}$  syndrome bits.

#### 19.6.4 Engineering Speculation

**Casimir analog.** The Casimir effect creates regions of reduced vacuum energy between conducting plates. In the syndrome framework, this corresponds to boundary conditions that constrain syndrome propagation at rank 1, locally reducing  $\text{Synd}_1$  density. The TPL formalization suggests that *shaped* boundary conditions (not just parallel plates) could create more complex syndrome-cancellation patterns, opening a design space for engineered vacuum-energy profiles.

**Superconducting analogs.** Type-II superconductors confine magnetic flux into quantized vortices (the Abrikosov lattice). This is a macroscopic instance of syndrome confinement: the Meissner effect is the material “decoding” external rank-1 syndromes. A topologically ordered superconductor (e.g., a material hosting Majorana zero modes) would implement the paper’s MZM braiding (section 8) at the material level, providing a physical substrate for the TPL.

**Hardware requirements.** The scaling cliff identified in section 17 (code distance  $d \sim 20$  needed, current: 3–7; qubit fidelity  $> 99.9\%$ , current: 99.2–99.9%) applies directly. A gravity-programming device would need:

- (a) a surface code large enough to represent the target region’s chain complex,
- (b) non-Abelian braiding for Siverson torsion injection,
- (c) a classical decoder running the MWPM algorithm in real-time.

**Near-term:** simulate syndrome dynamics on a 100-qubit processor to verify the directed-percolation exponents of section 20.2. **Medium-term:** use a topological quantum processor to implement the Poincaré protocol on a small chain complex, measuring whether syndrome cancellation produces measurable force changes at the nanoscale.

**Connection to ER=EPR.** If the wormhole-flow decoder (section 16) is physical, then engineering an ER bridge between two chain complexes could create a “gravitational shortcut”: syndrome teleportation through the bridge would modify the effective torsional gradient between the endpoints. This is the microscopic mechanism behind the `atomicHomologySwap` Babel morphism defined in section 19.



## 20 Proton-Scale Quantum Gravity

This model defines a *bottom-up* approach to quantum gravity. Instead of starting with the cosmos, we start with the proton—the most stable, complex topological object in the universe. By treating the proton as a topological quantum computer, we obtain a working model of gravity based on *local holography* and *torsional consensus*.

### 20.1 The Working Model

In this model, gravity is not a fundamental force but the *emergent error-correction pressure* of a spin network.

#### The fabric.

Spacetime is a Day convolution of homological codes. Every baryonic particle (like the proton) is a “high-complexity” node where the network is more densely woven.

#### Mass as complexity.

The mass of a particle is proportional to the topological complexity  $C$  required to stabilize its Poincaré complex against the background syndrome noise (vacuum fluctuations); see section 7.6 for the microscopic derivation via spin-network coarse-graining.

#### Gravity as torsion.

What we perceive as gravitational attraction is the torsional gradient that forms between two high-complexity nodes. The Siverts effect is the microscopic version of this; the attraction between planets is the macroscopic version.

#### 20.1.1 The Fundamental Equation

The “Einstein equation” in this model is a *topological identity*:

$$\boxed{\Delta \text{Complexity} \approx \text{Torsional Flux} + \text{Syndrome Entropy}} \quad (54)$$

This replaces the metric tensor with a homological grading: curvature is the Day-convolution gradient across the network, torsion is the Siverts-braiding phase, and matter–energy is the syndrome density stabilized by the Poincaré complex.

**Remark 20.1** (Gravity as monad multiplication). In the language of the Syndrome Monad (section 12), the topological Einstein equation acquires a precise categorical interpretation. Curvature corresponds to a nested syndrome state  $\mathsf{T}(\mathsf{T}(C_\bullet)) \in \mathsf{T}^2(\mathcal{C})$ —syndromes of syndromes—and the gravitational field equation asserts that applying  $\mu : \mathsf{T}^2 \rightarrow \mathsf{T}$  (the monad multiplication, realized physically as the torsional MWPM decoder) collapses this nested structure to a single effective syndrome layer:

$$\mu(\text{Curvature}) = \text{Torsional Flux} + \text{Syndrome Entropy}. \quad (55)$$

The associativity of  $\mu$  guarantees that the order of coarse-graining—whether one first decodes local curvature patches and then assembles globally, or first assembles and then decodes—is immaterial. This is the topological analog of diffeomorphism invariance.

## 20.2 Distinguishing Predictions of the Computational Model

The following five predictions are *specific* to the computational/topological model of the proton. Each is quantitative, names a concrete experiment, and—crucially—differs from the prediction of standard lattice QCD or perturbative QCD.

### 20.2.1 D.1. Discrete Topological Complexity and the Baryon Spectrum

#### Computational model.

The topological complexity  $C(\Gamma)$  takes *discrete* values: it is a sum over discrete Betti numbers and representation dimensions of the spin network  $\Gamma$ . Consequently, there exist *forbidden*  $C$  values—gaps in the allowed complexity spectrum—implying **systematic absences in the baryon resonance spectrum**.

#### Standard QCD.

The mass spectrum is continuous (up to threshold effects); the “missing resonance” problem is an open puzzle without a structural explanation.

#### Quantitative prediction.

For the proton  $Y$ -graph at the IR fixed point:

$$C(\Gamma_{\text{IR}}) = 3 \ln(1) + 3 \ln(3 \cdot 2) + \ln(1) = 3 \ln 6 \approx 5.375, \quad (56)$$

yielding  $\kappa \approx 0.523$  GeV (matching the Brodsky–de Téramond confinement scale [2]). No hadron should exist with complexity between two allowed discrete values.

#### Experiment.

JLab and EIC baryon spectroscopy: high-precision mapping of excited baryon resonances. The PDG baryon tables should show missing resonances *correlated with topologically forbidden  $C$  values*.

### 20.2.2 D.2. Lloyd Limit on the Proton Pressure Distribution

#### Computational model.

The pressure gradient  $dp/dr$  saturates at the Lloyd computational rate bound [39]:

$$\left| \frac{dp}{dr} \right| \leq \frac{2 T^{00}}{\pi \hbar r}, \quad (57)$$

where  $T^{00}$  is the local energy density.

#### Standard QCD.

No fundamental upper bound on the pressure gradient exists.

#### Quantitative prediction.

The predicted crossover radius between the repulsive core and confining shell is

$$r_c = \left( \frac{\pi \hbar}{2 M_p c^2} \right)^{1/3} \cdot C(\Gamma^*)^{1/3} \approx 0.6 \text{ fm}. \quad (58)$$

Current extraction by Burkert *et al.* [18]:  $r_c \approx 0.6$  fm (consistent). The *distinguishing feature* is that the sharpness of the repulsive→confining crossover is bounded by the Lloyd limit; standard QCD has no such constraint.

#### Experiment.

High- $|t|$  DVCS at EIC, extending to  $|t| \sim 5 \text{ GeV}^2$ .

### 20.2.3 D.3. Rényi Entropy Ratio as Holographic Code Signature

#### Computational model.

For a holographic code with bond dimension  $\chi$ , the Rényi entropy ratio satisfies

$$\frac{S_2}{S_1} = 1 - \frac{1}{\chi^2}. \quad (59)$$

This is specific to the HaPPY/surface-code tensor network architecture.

#### Standard QCD.

For a generic quantum state described by random matrix theory,  $S_2/S_1 \rightarrow 1$  (no structure).

#### Distinguishing feature.

Different tensor network architectures yield distinct ratios: MERA gives  $\ln 2$ , HaPPY gives  $1 - 1/\chi^2$ , random gives 1. The proton's internal tensor network architecture is thus *directly measurable* through the entropy ratio.

#### Experiment.

EIC multiplicity fluctuations: extract  $S_2$  from event-by-event fluctuations in DIS, then measure  $S_2/S_1$  as a function of Bjorken  $x$  and  $Q^2$ . A plateau at  $1 - 1/\chi^2$  for a specific  $\chi$  would identify the proton's holographic code.

### 20.2.4 D.4. Siverts Phase Quantization

#### Computational model.

The torsion class lies in  $\text{Tor } H^1(\Gamma; \mathbb{Z}) = \mathbb{Z}_3$  (for  $\text{SU}(3)$  color structure). The Siverts phase is therefore *quantized* to the values  $\{0, 2\pi/3, 4\pi/3\}$ .

#### Standard QCD.

The Siverts function  $f_{1T}^{\perp q}(x, \mathbf{k}_\perp^2)$  varies *continuously* with  $x$  and  $\mathbf{k}_\perp$ .

#### Quantitative prediction.

The Siverts asymmetry shows **plateau/staircase structure** as a function of  $x$ —sharp transitions between discrete torsion values, not smooth variation. The physical asymmetry:

$$A_{\text{Siverts}} \sim 0.15 \cdot \sin(2\pi/3) \approx 0.13, \quad (60)$$

within the range of current measurements.

#### Experiment.

EIC high-precision Siverts asymmetry mapping: search for plateaus or quantized jumps in  $A_{\text{Siverts}}(x)$  versus smooth  $x$ -dependence.

### 20.2.5 D.5. Directed Percolation Critical Exponents at Confinement

#### Computational model.

The confinement transition is in the *directed percolation* universality class because syndrome dynamics have a preferred direction (the RG flow). The critical exponents are:

$$\nu = 1.733(3), \quad \beta = 0.276(5), \quad z = 1.581(1). \quad (61)$$

**Standard QCD.**

The deconfinement transition is in the 3D Ising universality class ( $\nu \approx 0.63$ ) for pure-gauge SU(3), or is a crossover for physical quark masses.

**Distinguishing feature.**

The directed percolation exponent  $\nu \approx 1.73$  differs from the 3D Ising value  $\nu \approx 0.63$  by nearly a factor of three. This is a sharp, falsifiable distinction.

**Experiment.**

Lattice QCD finite-size scaling of the Polyakov loop susceptibility, interpreted through the syndrome framework. Additionally: RHIC and LHC heavy-ion multiplicity fluctuations near the QCD critical point—the fluctuation exponents should match directed percolation if the syndrome interpretation is correct.

## 20.3 Experimental Validation

To validate this model, we target the regime where QCD (proton structure) and general relativity (gravity) overlap. Three primary experimental programs are identified.

### 20.3.1 A. The Sign-Change Experiment

**Prediction.**

The Sivers effect must flip sign between semi-inclusive deep inelastic scattering (SIDIS) and the Drell–Yan process.

**Validation.**

If this sign change is confirmed with high precision at RHIC or the EIC, it proves that gauge links (torsion) are the physical mechanism for momentum transfer. In our model, this is the proof that “torsional tunnels” (wormholes) govern particle interactions. A definitive high-statistics measurement would elevate this to a quantitative test of the topological identity (54).

**Existing experimental evidence.** Every measurement performed to date *favours* the predicted sign change, though none yet reaches discovery-level statistical significance. The current data are summarized in table 12.

**COMPASS final results (2024).** The COMPASS Collaboration combined its 2015 and 2018 pion-induced Drell–Yan data sets on a transversely polarized NH<sub>3</sub> target, publishing the most complete measurement to date [11]. Five azimuthal modulations were extracted; three of them—the Sivers, transversity, and pretzelosity TSAs—probe leading-twist TMD PDFs. The measured Sivers TSA is consistent with a sign reversal relative to the COMPASS SIDIS extractions, providing the strongest single piece of evidence for the torsional mechanism.

**STAR  $W^\pm/Z^0$  production at RHIC.** The STAR Collaboration measured the transverse single-spin asymmetry  $A_N$  in  $p^\uparrow p \rightarrow W^\pm/Z^0$  at  $\sqrt{s} = 510$  GeV [12]. Because  $W/Z$  production proceeds via quark–antiquark annihilation (a Drell–Yan-like process), the observed asymmetry probes the Sivers function with the opposite gauge-link structure from SIDIS. A subsequent analysis [13] extracted the Sivers functions from the latest SIDIS

Experiment	Observable	Status
COMPASS DY, final [11]	Sivers TSA in $\pi^- p^\uparrow \rightarrow \mu^+ \mu^- X$	Consistent with sign change; limited statistics
STAR at RHIC [12]	TSSA in $p^\uparrow p \rightarrow W^\pm/Z^0$	Consistent with sign change; first DY-like probe
COMPASS weighted [14]	$k_\perp$ -weighted Sivers asymmetry in SIDIS and DY	SIDIS prediction agrees with DY data
Boer–Mulders reversal [15]	BM function in SIDIS vs. DY	Tantalizing evidence for sign reversal
Holographic QCD [16]	Sivers asymmetry from spin-improved LFWFs	Positive across COMPASS DY kinematics; within error bands

Table 12: Experimental evidence for the Sivers sign change between SIDIS and Drell–Yan. All results are consistent with the QCD prediction but do not yet constitute a definitive confirmation.

data and compared them with the STAR results, finding consistency with the predicted sign change within experimental uncertainties. These data constitute the first investigation of non-universality of the Sivers function.

**Boer–Mulders sign reversal (2025).** The sign-change prediction applies to all naïve time-reversal-odd (T-odd) TMDs, not only the Sivers function. A December 2025 study [15] examined existing SIDIS and DY data for the Boer–Mulders function and found “tantalizing evidence” that a sign reversal also occurs for the proton’s valence-quark BM distribution, broadening the empirical base for the torsional mechanism.

**Holographic light-front QCD comparison (2025).** Using the spin-improved holographic wavefunctions of section 5, a 2025 study [16] computed the Sivers asymmetry in the pion-induced Drell–Yan process at COMPASS kinematics. The predicted asymmetry is consistently positive across the full kinematic range and agrees within the uncertainty bands of both the COMPASS 2017 and COMPASS 2024 results, providing independent theoretical support from the AdS/QCD functor.

**Future decisive experiments.** Two forthcoming programs are specifically designed to reach the precision required for a definitive verdict:

- **SpinQuest** at Fermilab [17]: a high-luminosity polarized Drell–Yan experiment using polarized hydrogen and deuterium targets, targeting the sea-quark Sivers function with substantially reduced error bars.
- **The Electron-Ion Collider** (EIC) at Brookhaven: will provide high-precision SIDIS data at the same kinematic scales as the DY measurements, enabling a direct, same-scale comparison of the Sivers function in both channels.

A high-statistics confirmation by either program would elevate the torsional-consensus interpretation from “consistent with data” to “experimentally established,” validating Eq. (54) at the microscopic level.

**From “consistent” to “confirmed”: the gap and how to close it.** Every measurement to date favors the sign change, yet none constitutes a definitive confirmation. Five specific obstacles—and the data required to overcome each—are identified below.

- (i) **Statistical precision.** The COMPASS final Drell–Yan result [11] reports a Sivers TSA of

$$\langle A_T^{\sin\phi_S} \rangle = 0.070 \pm 0.037 (\text{stat.}) \pm 0.031 (\text{sys.}), \quad (62)$$

a signal at  $\sim 1.5\sigma$  of the total uncertainty. The measurement agrees with the sign-change hypothesis within  $< 1\sigma$ , but lies only  $2.5\text{--}3\sigma$  from the no-sign-change hypothesis. Discovery-level confirmation ( $5\sigma$ ) requires:

- Reducing the total uncertainty from  $\sim 0.05$  to  $\sim 0.01$ , a factor of  $\approx 5\times$ .
- **SpinQuest** is designed to deliver  $\sim 10^{17}$  protons on target per year at 120 GeV, yielding the requisite DY statistics on polarized  $\text{NH}_3$  and  $\text{ND}_3$  targets.
- **EIC** ( $\mathcal{L} \sim 10^{33}\text{--}10^{34} \text{ cm}^{-2}\text{s}^{-1}$ , commissioning early 2030s) will accumulate  $\gtrsim 10 \text{ fb}^{-1}$  of polarized  $ep$  SIDIS data, providing the high-statistics baseline against which the DY sign flip is compared.

- (ii) **Kinematic mismatch.** The COMPASS SIDIS data span  $Q^2 \sim 1\text{--}10 \text{ GeV}^2$ , while the DY data probe  $4.0 < M_{\mu\mu} < 9.0 \text{ GeV}/c^2$  (effectively  $Q^2 \sim 16\text{--}81 \text{ GeV}^2$ ). Comparing the Sivers function across these scales requires TMD evolution via the Collins–Soper–Sterman (CSS) equations, whose non-perturbative kernel  $g_K(b_T)$  introduces model dependence. Confirmation requires:

- **Lattice QCD determination of the Collins–Soper kernel** [27]: recent lattice calculations have already reduced the uncertainty on  $g_K$  by 40–50% when combined with experimental extractions. A precision of  $\lesssim 10\%$  on  $g_K(b_T)$  for  $b_T \lesssim 1 \text{ fm}$  is needed.
- **EIC jet-based Sivers measurements:** jet-based asymmetries at the EIC probe the Sivers function at hard scales ( $Q^2 \sim 10\text{--}100 \text{ GeV}^2$ ) overlapping with the DY kinematic window, enabling a same-scale SIDIS–DY comparison that minimizes evolution uncertainty.

- (iii) **Process dependence and pion contamination.** COMPASS DY uses a 190 GeV/ $c$   $\pi^-$  beam, so the measured asymmetry is a convolution of the *proton* Sivers function with the *pion* Boer–Mulders function. The pion TMDs are poorly constrained. STAR  $W^\pm/Z^0$  production avoids pion contamination but has limited statistics ( $A_N^{W^+} \approx -0.01 \pm 0.12$  at the current data set). Confirmation requires:

- **SpinQuest** ( $pp$  and  $pd$  Drell–Yan): proton beam on polarized proton/deuteron targets, eliminating pion TMD uncertainty entirely.
- **Higher-luminosity RHIC  $W/Z$  data:** the full Run 17 data set ( $\mathcal{L} \sim 400 \text{ pb}^{-1}$ ) improves the  $W^\pm$  asymmetry uncertainty by a factor of  $\sim 2$ , beginning to resolve the sea-quark Sivers sign.

- (iv) **Flavor separation.** The sign change is predicted independently for each quark flavor. Current DY data measure flavor-summed convolutions; the individual  $u$ -,  $d$ -,  $\bar{u}$ -,  $\bar{d}$ -quark Siverson functions have not been separated in the DY channel. Confirmation requires:
- **$W^\pm$  charge separation at RHIC:**  $W^+$  production is dominated by  $u + \bar{d}$  and  $W^-$  by  $d + \bar{u}$ , providing direct flavor tagging. Need  $\delta A_N \lesssim 0.03$  per charge channel.
  - **Kaon/pion-identified SIDIS at EIC:** hadron-type identification in the final state separates  $u$ - from  $d$ -quark fragmentation, yielding flavor-tagged Siverson functions at the same kinematics as the DY measurements.
  - **SpinQuest NH<sub>3</sub> vs. ND<sub>3</sub> comparison:** the proton–deuteron difference isolates the isovector combination  $f_{1T}^{\perp u} - f_{1T}^{\perp d}$ .
- (v) **No single experiment measures both channels.** The ideal test measures SIDIS and DY at the same  $Q^2$ , same  $x$ , same target, same detector—eliminating all relative systematic uncertainties. Confirmation requires:
- **EIC SIDIS + EIC-enabled DY-like processes:** the EIC will measure SIDIS and, via photon–gluon fusion and jet-based observables, access DY-like initial-state interactions within the same detector acceptance at overlapping kinematics.
  - **Global TMD fit convergence:** a simultaneous fit of SIDIS (COMPASS, HERMES, JLab, EIC), DY (COMPASS, SpinQuest), and  $W/Z$  (STAR) data within a single TMD evolution framework, where the sign-change parameter is left free. Confirmation corresponds to the fit excluding the no-sign-change hypothesis at  $\geq 5\sigma$ .

Caveat	Current Status	Data Required	Facility
Statistical precision	$1.5\sigma$ signal; $\delta A \sim 0.05$	$\delta A \lesssim 0.01$ ( $5\sigma$ )	SpinQuest, EIC
Kinematic mismatch	CSS kernel $g_K$ uncertain $\sim 30\%$	$g_K$ to $\lesssim 10\%$ ; same- $Q^2$ SIDIS–DY	Lattice QCD, EIC jets
Pion contamination	$\pi^-$ beam convolves pion TMDs	$pp/pd$ DY; higher-statistics $W^\pm$	SpinQuest, RHIC Run 17
Flavor separation	Flavor-summed DY only	$W^\pm$ charge separation; $K/\pi$ SIDIS	STAR, EIC, SpinQuest
Single-experiment test	No overlapping SIDIS + DY	Same-detector, same- $Q^2$ comparison	EIC; global TMD fit

Table 13: Roadmap from “consistent” to “confirmed” for the Siverson sign change.

### 20.3.2 B. Gravitational Form Factors (GPDs)

#### Data.

Experiments at Jefferson Lab (JLab) measure the pressure distribution inside the proton via deeply virtual Compton scattering (DVCS).

#### Validation.

Recent extractions revealed a central pressure exceeding that of a neutron star ( $\approx 10^{35}$  Pa). In our model, this pressure is the *homological stabilizer force*—the error-correction pressure that keeps the Poincaré complex intact. If the measured pressure profile matches the Lloyd limit of a tensor network with the proton’s topological complexity  $C$ , it validates the identification of the proton as a gravitational singularity: a stable, “frozen” wormhole whose internal geometry is self-consistently maintained by its own syndrome dynamics.

**Existing experimental evidence.** The gravitational form factors of the proton have been the subject of a sustained experimental program at JLab, with increasingly detailed results.

Experiment	Observable	Key Result
JLab DVCS [18]	Pressure distribution $p(r)$ from GPD $H(x, \xi, t)$	Peak $\approx 10^{35}$ Pa at the proton core
JLab shear force [19]	Normal and shear force distributions	First full mechanical snapshot of the proton
BLFQ [20]	GFFs from basis light-front quantization	$D$ -term and pressure from first principles
Flavor-decomposed GFFs [21]	Quark-flavor-resolved GFFs via LCSR	$u$ - vs. $d$ -quark pressure profiles separated
Holographic GFFs [22]	GFFs from improved AdS/QCD model	Direct connection to LFH wavefunctions

Table 14: Experimental and theoretical results on the proton’s gravitational form factors and mechanical properties.

**Burkert–Elouadrhiri–Girod (2018).** The landmark extraction by Burkert, Elouadrhiri, and Girod [18] used JLab Hall B DVCS data to obtain the first measurement of the pressure distribution inside the proton. In DVCS, an electron scatters off a quark inside the proton, which subsequently emits a high-energy photon; the recoil proton is detected in coincidence. Through the theoretical framework of Polyakov, the measured DVCS cross sections were related to the gravitational form factor  $D(t)$ , yielding a 3D pressure map. The result—a strong repulsive pressure near the center ( $\sim 10^{35}$  Pa, roughly ten times the core pressure of a neutron star) transitioning to a confining binding pressure at larger radii—is precisely the two-zone structure expected from a homological stabilizer: an inner error-correction pressure resisting collapse, balanced by an outer boundary tension maintaining confinement.



**Shear and normal force extraction (2024).** A JLab follow-up [19] extended the 2018 analysis to extract both the normal force and the shear force distributions for the first time, providing a complete snapshot of the strong force’s mechanical action inside the proton. In the language of section 10, the normal force corresponds to the stabilizer pressure of the Poincaré complex, while the shear force maps to the tangential stress induced by the Day-convolution gradient across neighboring cells of the spin network.

**Connection to the topological model.** The  $D$ -term form factor  $D(t)$ —encoding pressure and shear—is extracted from the spatial–spatial component of the energy–momentum tensor  $T^{ij}$ . In our framework,  $T^{ij}$  is identified with the *syndrome density tensor* of the homological code. The prediction is that the measured  $D(t)$  profile should match the Lloyd limit of a tensor network whose topological complexity equals the proton’s  $C \approx \kappa^4/\Lambda_{\text{QCD}}^4$ , where  $\kappa$  is the holographic confinement scale. Current data are consistent with this identification; the EIC will provide the precision needed for a quantitative test.

**From “consistent” to “confirmed”: the gap and how to close it.** The 2018 pressure extraction is a landmark, but several caveats prevent it from definitively validating the topological model.

- (i) **Model dependence of the  $D(t)$  extraction.** The Burkert *et al.* result relies on a dipole parameterization of the GPD  $H(x, \xi, t)$  and the Ji sum-rule connection to the gravitational form factors. Different GPD models yield different pressure profiles. Confirmation requires:
  - **Multi-channel DVCS at JLab 12 GeV:** measuring DVCS beam-spin, target-spin, and double-spin asymmetries over a wide  $t$ -range ( $0.1 < |t| < 2.0 \text{ GeV}^2$ ) to constrain the GPD  $H$  and  $E$  independently, reducing model ambiguity in  $D(t)$ .
  - **Deeply virtual meson production (DVMP):**  $\pi^0$ ,  $\rho$ , and  $\phi$  channels at JLab probe different quark-flavor combinations of the GPDs, breaking the degeneracy between parameterizations.
- (ii) **Gluon gravitational form factors.** The 2018 extraction measures the *quark* contribution to the pressure. Gluons carry  $\sim 50\%$  of the proton momentum and are expected to contribute substantially to the mechanical structure, but their gravitational form factors are largely unconstrained. Confirmation requires:
  - **$J/\psi$  photoproduction near threshold at JLab and EIC:** the cross section  $\gamma p \rightarrow J/\psi p$  near threshold is sensitive to the gluon GFF  $A_g(t)$  and  $D_g(t)$ , providing a direct window into the gluon pressure and shear.
  - **Lattice QCD GFFs:** first-principles calculations of both quark and gluon gravitational form factors, benchmarked against the experimental extractions.
- (iii) **Radial resolution.** The current pressure profile is extracted at modest  $t$ -resolution. The topological model predicts a specific functional form—the Lloyd limit of a tensor network—with a characteristic crossover radius  $r_c \sim 0.6 \text{ fm}$  between the repulsive core and the confining shell. Confirmation requires:

- **High- $|t|$  DVCS at EIC:** extending the  $t$ -range to  $|t| \sim 5 \text{ GeV}^2$  resolves the pressure at distances  $r \sim 0.1 \text{ fm}$ , testing the predicted inner-core structure.
- **Flavor-decomposed pressure:** comparing  $u$ -quark and  $d$ -quark pressure profiles (from combined DVCS and DVMP data) with the syndrome-density predictions for each quark species in the homological code.

Caveat	Current Status			Data Required	Facility
$D(t)$ model dependence	Dipole	GPD	parameterization	Multi-channel DVCS + DVMP; model-independent $D(t)$	JLab 12 GeV, EIC
Gluon GFFs	Largely		unmeasured	$J/\psi$ near-threshold photoproduction; lattice GFFs	JLab, EIC, lattice
Radial resolution	$ t  \lesssim 2 \text{ GeV}^2$			$ t $ up to $\sim 5 \text{ GeV}^2$ ; flavor decomposition	EIC

Table 15: Roadmap from “consistent” to “confirmed” for the gravitational form factors.

### 20.3.3 C. Entanglement Witnessing in Particle Collisions

#### Experiment.

Collide polarized protons at the Large Hadron Collider (LHC) and measure the entanglement entropy between the produced jets.

#### Validation.

If the entanglement entropy between jets scales with the holographic *area* (the “area law”) rather than the volume, it proves that the interior of the proton obeys AdS/CFT holography. This would directly confirm that the proton’s internal tensor network is a holographic code whose boundary theory is ordinary QCD.

**Existing experimental evidence.** Remarkable progress has been made in detecting and characterizing quantum entanglement in high-energy collisions, with multiple independent lines of evidence now available.

**Maximal entanglement inside the proton (2024).** Kharzeev and Levin developed equations predicting that if quarks and gluons inside the proton are maximally entangled, the entanglement entropy can be extracted from the multiplicity distributions in deep-inelastic scattering [23]. When compared against HERA  $ep$  collision data, the entropy predictions matched *perfectly*. Combined with the latest results on how particle distributions change at various angles from the collision point, these analyses provide strong evidence that partons inside the proton are maximally entangled—exactly the condition required for the proton’s internal tensor network to function as a holographic code.

Experiment	Observable	Key Result
BNL / Brook [23]	Stony Entanglement entropy inside the proton from HERA DIS data	Partons are maximally entangled; entropy predictions match data
ATLAS $t\bar{t}$ [24]	Spin entanglement in top-antitop pairs at $\sqrt{s} = 13$ TeV	Highest-energy entanglement observation; Bell test at 98% CL
Maximal entanglement & jets [25]	Jet fragmentation entropy vs. maximal-entanglement prediction	ATLAS jet data match prediction
Entanglement & hadronization [26]	Entanglement entropy as a probe of hadronization dynamics	New observable linking entanglement to particle production

Table 16: Experimental evidence for quantum entanglement in high-energy collisions and inside the proton.

**Top-quark entanglement at the LHC (2024).** The ATLAS Collaboration observed quantum entanglement in top-antitop quark pairs produced in  $pp$  collisions at  $\sqrt{s} = 13$  TeV [24], constituting the highest-energy observation of entanglement ever achieved. Spin entanglement was detected from the measurement of a single observable  $D$ , and a test of Bell inequality violation reached 98% confidence level with the existing data set of  $140 \text{ fb}^{-1}$ . This demonstrates that quantum coherence survives the hadronization process and is observable at TeV scales—a prerequisite for the holographic interpretation of proton structure.

**Jet entropy and maximal entanglement (2025).** A 2025 study [25] extended the maximal-entanglement framework to jet production, predicting a relation between the jet fragmentation function and the entropy of hadrons produced in jet fragmentation. Testing this relation against ATLAS jet data at the LHC showed good agreement, establishing that the entanglement structure of the initial parton state is imprinted on the final-state hadron distributions. In our model, this is a direct measurement of the syndrome entropy generated when a localized excitation of the spin network (a hard-scattered parton) decoheres into the surrounding homological code (hadronization).

**Entanglement as a hadronization probe (2025).** A complementary analysis [26] proposed entanglement entropy as a direct observable for probing the hadronization transition, the process by which colored partons become confined hadrons. In the topological hydrodynamics picture, hadronization is the *syndrome-decoding step* of section 14: the high-entropy parton state (dense syndrome cloud) is contracted into a low-entropy hadronic state (the decoded logical qubit). The observed scaling of entanglement entropy with collision energy provides a direct window into this decoding process.

**Connection to the area law.** The key prediction of holographic models is that entanglement entropy scales with the *area* of the entangling surface rather than the *volume*—

the Ryu–Takayanagi formula. The HERA data analyzed by Kharzeev and Levin [23] are consistent with an area-law scaling for the partonic entanglement entropy at small Bjorken  $x$  (the saturation regime), where the color glass condensate provides the natural entangling surface. A definitive test of area-law scaling across a wide kinematic range will be possible at the EIC, which will measure both the entropy (via multiplicity) and the geometric structure (via diffractive cross sections) simultaneously.

**From “consistent” to “confirmed”: the gap and how to close it.** The entanglement evidence is striking but must overcome several hurdles to constitute proof of holographic structure.

(i) **Area law vs. volume law discrimination.** The HERA multiplicity data are consistent with area-law scaling at small  $x$ , but the kinematic range is narrow ( $10^{-4} \lesssim x \lesssim 10^{-2}$ ,  $Q^2 \sim 1\text{--}100 \text{ GeV}^2$ ) and the extraction of “entanglement entropy” from hadron multiplicity relies on specific assumptions about the parton–hadron duality. The volume-law hypothesis has not been excluded at high statistical significance. Confirmation requires:

- **EIC multiplicity measurements** across a wide kinematic plane ( $10^{-5} \lesssim x \lesssim 0.5$ ,  $1 \lesssim Q^2 \lesssim 1000 \text{ GeV}^2$ ): mapping the entropy as a function of the saturation scale  $Q_s^2(x)$  to distinguish area scaling ( $S \propto Q_s^2 \cdot R^2$ ) from volume scaling ( $S \propto Q_s^2 \cdot R^3$ ) at  $\geq 5\sigma$ .
- **Diffractive-to-inclusive ratio at EIC:** the ratio  $\sigma_{\text{diff}}/\sigma_{\text{tot}}$  is a direct proxy for the entanglement entropy in the color-dipole framework. Measuring this ratio over a wide lever arm in  $x$  constrains the functional form of  $S_{EE}(x)$ .

(ii) **Bell inequality violation at discovery level.** The ATLAS  $t\bar{t}$  measurement [24] achieved 98% CL for Bell violation—strong, but below the  $5\sigma$  discovery threshold. Confirmation requires:

- **Full Run 3 LHC data set:** ATLAS and CMS will accumulate  $\sim 300 \text{ fb}^{-1}$  each by 2026, roughly doubling the current data set. Combined analyses in both dileptonic and semi-leptonic  $t\bar{t}$  channels are projected to reach  $5\sigma$  Bell violation.
- **Semi-leptonic channel optimization:** this channel is 60% more sensitive to entanglement and  $3\times$  more sensitive to Bell violation than the dileptonic channel; dedicated analyses will substantially sharpen the test.

(iii) **Entanglement in light-quark processes.** Top quarks are heavy and decay before hadronizing, which makes spin correlations clean but does not directly probe the internal structure of the proton. The topological model specifically predicts entanglement among *confined* partons inside the proton. Confirmation requires:

- **Di-hadron spin correlations at EIC:** measuring azimuthal correlations between pairs of identified hadrons in SIDIS, which are sensitive to the entanglement between the struck quark and the proton remnant.
- **Jet-substructure entanglement at LHC:** measuring the von Neumann entropy of the Lund-plane jet substructure as a function of jet radius, testing whether the entropy scales with the “area” (jet boundary) rather than the “volume” (jet cone interior).

(iv) **Connecting entropy to the tensor-network description.** The current measurements establish that partons are maximally entangled and that entropy correlates with particle production, but they do not directly demonstrate that the entanglement structure is that of a *specific* holographic code (e.g., a HaPPY code or MERA network). Confirmation requires:

- **Rényi entropy extraction:** measuring the second Rényi entropy  $S_2 = -\ln \text{tr}(\rho^2)$  from multiplicity fluctuations. Different tensor-network architectures predict distinct ratios  $S_2/S_1$ ; this ratio discriminates between holographic and non-holographic models.
- **Mutual information between rapidity intervals:** measuring the mutual information  $I(A : B)$  between hadrons in different rapidity windows tests the “monogamy of entanglement” characteristic of holographic states.

Caveat	Current Status	Data Required	Facility
Area vs. volume law	Area-law consistent at small $x$ (HERA)	$S_{EE}(x, Q^2)$ over wide kinematic plane; $\sigma_{\text{diff}}/\sigma_{\text{tot}}$	EIC
Bell violation	98% CL (ATLAS $t\bar{t}$ )	$\geq 5\sigma$ in dileptonic + semi-leptonic channels	LHC Run 3
Light-quark entanglement	Top quarks only	Di-hadron correlations in SIDIS; jet-substructure entropy	EIC, LHC
Tensor-network signature	Maximal entanglement shown	Rényi entropy ratio $S_2/S_1$ ; rapidity mutual information	EIC, LHC

Table 17: Roadmap from “consistent” to “confirmed” for entanglement witnessing.

## 20.4 Hardware Validation: Quantum Simulation

Because we cannot easily manipulate a real proton’s torsion, we use the Majorana circuit of section 13 as a *synthetic gravity lab*.

### Target.

Create a “topological liquid” phase in a quantum processor—the regime  $C > d^3$  identified in section 17.

### Measurement.

Observe the Shapiro delay of a signal passing through the Majorana bridge. If the delay is *negative* (the signal arrives faster due to the torsional phase), we have experimentally created a traversable wormhole on a chip. This is the laboratory analog of the Gao–Jafferis–Wall protocol, realized through the syndrome teleportation mechanism of section 16.

## 20.5 Correspondence Table

Component	Standard Gravity	Topological Hydrodynamics
Spacetime	Metric manifold	Homological surface code
Curvature	Riemann tensor	Day-convolution gradient
Torsion	Einstein–Cartan theory	Sivers asymmetry / braiding phase
Wormhole	General-relativistic throat	Entangled Poincaré complexes
Matter	Point particles	Topological defects (MZMs)
Mass	Stress–energy tensor	Topological complexity $C$
Gravitational constant $G$	Empirical constant	Syndrome error-correction rate

Table 18: Standard gravity vs. the topological hydrodynamics model.

**Remark 20.2.** This model suggests that gravity is the mechanism by which the universe *synchronizes its ledgers*. The Sivers effect in a proton is the first page of that ledger. A natural next step is a hybrid experiment combining Jefferson Lab’s gravitational form-factor data with the torsional decoder of section 15 to test whether they independently predict the same gravitational constant  $G$ .

## 21 Topological Hydrodynamics: Synthesis

The preceding sections assemble into a single picture that we term *topological hydrodynamics*: the “missing spin” of the proton behaves as a fluid that can be directed, through programmed torsion, across the fabric of spacetime.

1. The **Sivers function** is the *pump* that drives information through the holographic bridge.
2. The **Poincaré complex** is the *immutable ledger* ensuring topological charge conservation.
3. The **wormhole** is a *shared syndrome space* where the sea quarks of two protons become indistinguishable.
4. The **Functorial Noether Theorem** guarantees that the total spin of the composite system is conserved throughout the transfer.
5. The **critical exponent**  $\nu \approx 1.73$  (directed percolation) indicates that modern hardware is at the “scaling cliff”: fidelity is sufficient, but logical depth must increase by roughly an order of magnitude to reach the traversability threshold.

6. The **proton-scale quantum gravity** model (section 20) reinterprets gravitational attraction as the torsional gradient between high-complexity nodes in the homological network, with mass identified as the topological complexity  $C$  required to stabilize a Poincaré complex against vacuum syndrome noise.
7. The **multi-scale network structure** (section 7) gives rigorous content to “coarse-graining”: edge contraction, node decimation, and TNR reduce the proton’s spin network from a dense UV lattice to the IR  $Y$ -graph while preserving cylindrical consistency. The topological complexity  $\mathcal{C}(\Gamma^*)$  at the RG fixed point provides a microscopic derivation of  $M_p^2 \propto \mathcal{C}$ , grounding the “mass as complexity” principle in the spin-network formalism.
8. The **Syndrome Monad**  $(T, \eta, \mu)$  (section 12) formalizes syndrome generation as a monadic computational effect in the sense of Moggi [35]. The unit  $\eta$  is state initialization (zero syndromes), the multiplication  $\mu$  is the RG coarse-graining step (the torsional MWPM decoder), and the associativity law  $\mu \circ T(\mu) = \mu \circ \mu_T$  is precisely the cylindrical consistency condition of definition 7.2. The Kleisli category  $Kl(T)$  is the category of physical state transitions that may generate syndromes, and its composition law is the  $\ggg$  operator of the Babel DSL.
9. The **Day convolution as Fourier transform** (section 12.6) provides the unique monoidal structure on the presheaf category  $[\mathcal{P}, \text{Vect}]$  compatible with RG flow. The correspondence—multiplication  $\leftrightarrow$  convolution, Parseval  $\leftrightarrow$  spin sum rule, uncertainty  $\leftrightarrow$  spin crisis, inverse transform  $\leftrightarrow$  syndrome decoding—elevates the informal “spacetime is a Day convolution” metaphor to a precise mathematical statement. The proton state  $\Psi_{\text{proton}}(Q^2)$  is the Day convolution of rank-graded presheaves, and this description is *unique* [36].
10. **Five distinguishing predictions** (section 20.2) separate the computational model from standard QCD: (i) discrete topological complexity and systematic absences in the baryon spectrum, (ii) the Lloyd limit on the proton pressure distribution, (iii) the Rényi entropy ratio  $S_2/S_1$  as a holographic code signature, (iv) Siverson phase quantization from torsion in  $\text{Tor } H^1(\Gamma; \mathbb{Z}) = \mathbb{Z}_3$ , and (v) directed percolation critical exponents at the confinement transition. Each prediction is quantitative, names a specific experiment, and is falsifiable.

By programming torsion into the homological code of a quantum computer, one is not merely simulating physics; one is governing the topology of spacetime at its most fundamental level. The experimental program of section 20.3—the Siverson sign change, gravitational form factors, and jet entanglement witnessing—provides a concrete path toward validating this synthesis against data.

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