Gaussian Elimination Solver
1.0

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Chapter 1

Gaussian Elimination Solver

This project solves systems of linear equations using Gaussian elimination.

The program reads matrices from .in files, performs Gaussian elimination with partial pivoting, determines the rank and consistency of the system, and displays the solution. It allows multiple runs and interacts with the user for input and exit control.

1.0.1 Features

- · Gaussian elimination with partial pivoting
- · Rank determination and consistency check
- · Handles cases with no solution, unique solution, or infinitely many solutions

1.0.2 Usage

- 1. Provide a matrix in an .in file.
- 2. The program reads the matrix and applies Gaussian elimination.
- 3. The user can run the program multiple times.

Chapter 2

File Index

2.1 File List

Here is a list of all files with brief descriptions:

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File Index

Chapter 3

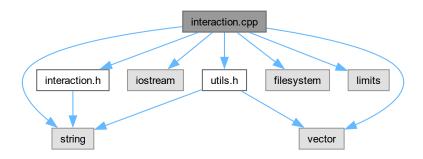
File Documentation

3.1 interaction.cpp File Reference

Implementation of user interaction functions.

```
#include "interaction.h"
#include <iostream>
#include <vector>
#include <string>
#include <filesystem>
#include <limits>
#include "utils.h"
```

Include dependency graph for interaction.cpp:



Functions

• string SelectInputFile ()

Allows the user to select an input .in file from the current directory.

• char AskRunAgain ()

Asks the user if they want to run the program again.

• void WaitForExit ()

Waits for the user to press Enter before exiting.

3.1.1 Detailed Description

Implementation of user interaction functions.

Author

Gilbert Young

Date

2024/09/25

This file implements the functions responsible for interacting with the user, including selecting input files, prompting whether to run the program again, and waiting for the user to exit. These functions guide the flow of the program based on user input.

3.1.2 Function Documentation

3.1.2.1 AskRunAgain()

```
char AskRunAgain ()
```

Asks the user if they want to run the program again.

Returns

char The user's choice ('y', 'Y', 'n', 'N').

```
00091 {
00092
          char choice;
          while (true)
00094
00095
              cout « "\nDo you want to run the program again? (y/n): ";
00096
              cin » choice;
00097
              if (choice == 'v' || choice == 'Y' || choice == 'n' || choice == 'N')
00098
00099
              {
00101
00102
              else
00103
              {
                  cout « "Invalid input. Please enter 'y' or 'n'." « endl;
00104
00105
00106
00107
          return choice;
00108 }
```

3.1.2.2 SelectInputFile()

```
string SelectInputFile ()
```

Allows the user to select an input .in file from the current directory.

Returns

std::string The name of the selected file. Empty string if no file is selected.

```
00029 {
00030
          vector<string> in files:
00031
          for (const auto &entry : filesystem::directory_iterator(filesystem::current_path()))
00032
00033
               if (entry.is_regular_file())
00034
00035
                   string filename = entry.path().filename().string();
00036
                   if (filename.size() >= 3 && filename.substr(filename.size() - 3) == ".in")
00037
00038
                       in_files.push_back(filename);
00039
                  }
00040
00041
          }
00042
00043
          string selected file:
00044
          if (in_files.empty())
00045
00046
              cout « "No .in files found in the current directory." « endl;
              return "";
00047
00048
00049
          else if (in files.size() == 1)
00050
              00051
00052
00053
00054
          else
00055
00056
              cout « "Multiple .in files found. Please select one:" « endl;
              for (size_t i = 0; i < in_files.size(); i++)</pre>
00057
00058
00059
                  cout « i + 1 « ". " « in_files[i] « endl;
00060
00061
              int file_choice;
00062
              \begin{tabular}{ll} // & Improved input validation \\ \end{tabular}
00063
              while (true)
00064
00065
                  cout « "Enter the number of the file you want to use (1-" « in_files.size() « "): ";
00066
                  cin » file_choice;
00067
00068
                   if (cin.fail() || file choice < 1 || file choice > static cast<int>(in files.size()))
00069
00070
                       cin.clear();
                                                                                // Clear error flags
00071
                       cin.ignore(numeric_limits<streamsize>::max(), '\n'); // Clear input buffer
00072
                       cout \overset{\,\,{}_{\circ}}{\,\,} "Invalid input. Please enter a number between 1 and " \overset{\,\,{}_{\circ}}{\,\,} in_files.size() \overset{\,\,{}_{\circ}}{\,\,} " \overset{\,\,{}_{\circ}}{\,\,}
     endl;
00073
00074
                  else
00075
                  {
00076
                       break;
00077
00078
00079
              selected_file = in_files[file_choice - 1];
08000
00081
          cout « endl;
00082
          return selected_file;
00083 }
```

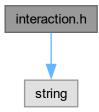
3.1.2.3 WaitForExit()

3.2 interaction.h File Reference

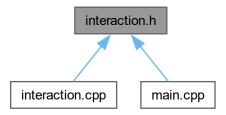
User interaction functions.

#include <string>

Include dependency graph for interaction.h:



This graph shows which files directly or indirectly include this file:



Functions

• std::string SelectInputFile ()

Allows the user to select an input .in file from the current directory.

• char AskRunAgain ()

Asks the user if they want to run the program again.

void WaitForExit ()

Waits for the user to press Enter before exiting.

3.2.1 Detailed Description

User interaction functions.

Author

Gilbert Young

Date

2024/09/25

3.2.2 Function Documentation

3.2.2.1 AskRunAgain()

```
char AskRunAgain ()
```

Asks the user if they want to run the program again.

Returns

```
char The user's choice ('y', 'Y', 'n', 'N').task char The user's choice ('y', 'Y', 'n', 'N').
```

```
00092
          char choice;
00093
          while (true)
00094
00095
              cout « "\nDo you want to run the program again? (y/n): ";
00096
              cin » choice;
00097
00098
              if (choice == 'y' || choice == 'Y' || choice == 'n' || choice == 'N')
00099
              {
00100
                  break;
              }
00101
00102
              else
00103
              {
00104
                  cout « "Invalid input. Please enter 'y' or 'n'." « endl;
00105
00106
00107
          return choice;
00108 }
```

3.2.2.2 SelectInputFile()

```
std::string SelectInputFile ()
```

Allows the user to select an input .in file from the current directory.

Returns

std::string The name of the selected file. Empty string if no file is selected.

```
00029 {
00030
         vector<string> in_files;
00031
         for (const auto &entry : filesystem::directory_iterator(filesystem::current_path()))
00032
00033
             if (entry.is_regular_file())
00034
00035
                string filename = entry.path().filename().string();
                if (filename.size() >= 3 && filename.substr(filename.size() - 3) == ".in")
00036
00037
00038
                    in_files.push_back(filename);
00039
                }
00040
00041
         }
00042
00043
         string selected file:
00044
         if (in_files.empty())
00045
00046
            cout « "No .in files found in the current directory." « endl;
00047
            return "";
00048
00049
         else if (in_files.size() == 1)
00050
            00051
00052
00053
00054
         else
00055
         {
00056
            cout « "Multiple .in files found. Please select one:" « endl;
00057
            for (size_t i = 0; i < in_files.size(); i++)</pre>
00058
```

```
cout « i + 1 « ". " « in_files[i] « endl;
00060
00061
              int file_choice;
00062
              \ // \ {\tt Improved input validation}
00063
              while (true)
00064
                  cout « "Enter the number of the file you want to use (1-" « in_files.size() « "): ";
00065
00066
                  cin » file_choice;
00067
00068
                  if (cin.fail() || file_choice < 1 || file_choice > static_cast<int>(in_files.size()))
00069
00070
                                                                             // Clear error flags
                      cin.clear():
00071
                      cin.ignore(numeric_limits<streamsize>::max(), '\n'); // Clear input buffer
                      cout « "Invalid input. Please enter a number between 1 and " « in_files.size() « "." «
     endl;
00073
00074
                  else
00075
                  {
                      break;
00077
                  }
00078
00079
              selected_file = in_files[file_choice - 1];
08000
00081
         cout « endl:
00082
          return selected_file;
00083 }
```

3.2.2.3 WaitForExit()

```
void WaitForExit ()
```

Waits for the user to press Enter before exiting.

3.3 interaction.h

Go to the documentation of this file.

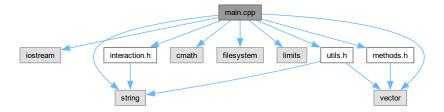
```
00001
00008 #ifndef INTERACTION_H
00009 #define INTERACTION_H
00010
00011 #include <string>
00012
00018 std::string SelectInputFile();
00019
00025 char AskRunAgain();
00026
00030 void WaitForExit();
00031
00032 #endif // INTERACTION_H
```

3.4 main.cpp File Reference

Entry point for the Gaussian Elimination Solver project.

```
#include <iostream>
#include <string>
#include <vector>
#include <cmath>
#include <filesystem>
#include <limits>
#include "utils.h"
```

```
#include "methods.h"
#include "interaction.h"
Include dependency graph for main.cpp:
```



Functions

• int main ()

3.4.1 Detailed Description

Entry point for the Gaussian Elimination Solver project.

Author

Gilbert Young

Date

2024/09/25

3.4.2 Function Documentation

3.4.2.1 main()

```
int main ()
00042 {
00043
            char choice;
00044
            do
00045
                 string selected_file = SelectInputFile();
00046
00047
                 if (selected_file.empty())
00048
00049
                      return 1; // File selection failed
00050
00051
00052
                 vector<vector<double> matrix;
00053
                 int rows, cols;
00054
                 if (!InitMatrix(matrix, selected_file, rows, cols))
00055
00056
                      return 1; // Matrix initialization failed
00057
00058
                 ShowEquations(matrix, rows, cols);
cout « "Starting Gaussian elimination process..." « endl;
int exchange_count = GaussianElimination(matrix, rows, cols);
00059
00060
00061
00062
                 cout « "Gaussian elimination completed." « endl
00063
                       « endl;
```

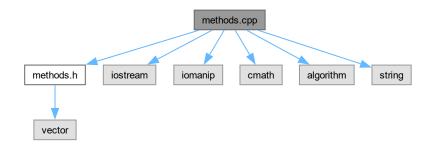
```
00065
              int rank = DetermineRank(matrix, rows, cols);
00066
              bool consistent = CheckConsistency(matrix, rows, cols);
00067
00068
              if (!consistent)
00069
00070
                  cout « "The system of equations is inconsistent and has no solution." « endl;
00071
              else if (rank < (cols - 1))</pre>
00072
00073
              {
00074
                  ShowGeneralSolution(matrix, rows, cols, rank);
00075
00076
              else
00077
00078
                  vector<double> solution;
00079
                  bool solvable = BackSubstitution(matrix, rows, cols, solution);
00080
                  if (solvable)
00081
00082
                      DisplaySolution(solution);
00083
00084
00085
00086
                      cout « "The system of equations is inconsistent and has no solution." « endl;
00087
                  }
00088
00089
00090
              choice = AskRunAgain();
00091
          } while (choice == 'y' || choice == 'Y');
00092
00093
00094
          WaitForExit();
00095
          return 0;
00096 }
```

3.5 methods.cpp File Reference

Implementation of computational functions for solving linear systems.

```
#include "methods.h"
#include <iostream>
#include <iomanip>
#include <cmath>
#include <algorithm>
#include <string>
```

Include dependency graph for methods.cpp:



Functions

- int Pivoting (const vector< vector< double > > &m, int current_row, int total_rows)
- void Exchange (vector< vector< double >> &m, int row1, int row2)

- bool Eliminate (vector< vector< double > > &m, int current_row, int total_rows, int total_cols)
- int GaussianElimination (vector< vector< double > > &m, int rows, int cols)
- bool BackSubstitution (const vector< vector< double >> &m, int rows, int cols, vector< double > &solution)
- int DetermineRank (const vector< vector< double >> &m, int rows, int cols)
- vector< int > IdentifyPivots (const vector< vector< double > > &m, int rows, int cols)
- void ShowGeneralSolution (const vector< vector< double > > &m, int rows, int cols, int rank)

3.5.1 Detailed Description

Implementation of computational functions for solving linear systems.

Author

Gilbert Young

Date

2024/09/25

This file implements key algorithms such as Gaussian elimination with partial pivoting, back-substitution, and rank determination. It also includes functionality to display the general solution when the system has infinitely many solutions.

3.5.2 Function Documentation

3.5.2.1 BackSubstitution()

```
bool BackSubstitution (
               const vector< vector< double > > & m,
               int rows,
               int cols,
               vector< double > & solution)
00120 {
00121
          solution.assign(cols - 1, 0.0);
          cout « "Starting back-substitution process..." « endl;
for (int i = rows - 1; i >= 0; i--)
00122
00123
00124
00125
               // Find the first non-zero coefficient in the row
00126
               int pivot_col = -1;
00127
               for (int j = 0; j < cols - 1; j++)
00128
00129
                   if (fabs(m[i][j]) > 1e-12)
00130
                   {
00131
                       pivot_col = j;
00132
                       break;
00133
                   }
00134
               }
00135
00136
               if (pivot_col == -1)
00137
00138
                   if (fabs(m[i][cols - 1]) > 1e-12)
00139
00140
                       // Inconsistent equation
00141
                       return false;
00142
00143
00144
                   {
00145
                       // 0 = 0, skip
00146
                       continue;
00147
                   }
00148
               }
00149
```

```
double rhs = m[i][cols - 1];
           cout « "Calculating x" « pivot_col + 1 « ":" « endl;
for (int j = pivot_col + 1; j < cols - 1; j++)</pre>
00151
00152
00153
           {
              00154
00155
00156
              rhs -= m[i][j] * solution[j];
00157
           cout « " RHS after subtraction = " « rhs « endl;
00158
           00159
00160
00161
00162
               « endl;
00163
00164
        return true;
00165 }
```

3.5.2.2 DetermineRank()

```
int DetermineRank (
              const vector< vector< double > > & m_{r}
              int rows.
              int cols)
00168 {
00169
          int rank = 0;
00170
          for (int i = 0; i < rows; i++)</pre>
00171
          {
00172
              bool non_zero = false;
00173
              for (int j = 0; j < cols - 1; j++)
00174
00175
                  if (fabs(m[i][j]) > 1e-12)
00176
                      non_zero = true;
00177
00178
                      break:
00179
                 }
00180
00181
              if (non_zero)
00182
                  rank++;
00183
00184
          return rank;
00185 }
```

3.5.2.3 Eliminate()

```
bool Eliminate (
             vector< vector< double > > & m,
            int current_row,
            int total_rows,
            int total_cols)
00047 {
00048
        for (int i = current_row + 1; i < total_rows; i++)</pre>
00049
00050
            if (fabs(m[current_row][current_row]) < 1e-12)</pre>
00051
            {
00052
               // Pivot is too small, cannot eliminate
00053
               return false;
00054
            00055
00056
00058
00059
            m[i][current_row] = 0.0;
00060
            for (int j = current_row + 1; j < total_cols; j++)</pre>
00061
            {
00062
               m[i][j] -= factor * m[current_row][j];
00063
00064
            cout « endl;
00065
00066
         return true;
00067 }
```

3.5.2.4 Exchange()

3.5.2.5 GaussianElimination()

```
int GaussianElimination (
               vector< vector< double > > & m_{r}
               int rows,
               int cols)
00070 {
00071
          int exchange_count = 0;
00072
          for (int i = 0; i < min(rows, cols - 1); i++)
00073
00074
              cout « "Processing column " « i + 1 « "..." « endl;
00075
              int imax = Pivoting(m, i, rows);
00076
              if (imax != i)
00077
              {
00078
                  Exchange(m, i, imax);
00079
                  exchange_count++;
08000
00081
              else
00082
00083
                  cout \ll "No need to swap rows for column " \ll i + 1 \ll "." \ll endl;
              }
00084
00085
00086
              // Check if pivot is zero
00087
              if (fabs(m[i][i]) < 1e-12)</pre>
00088
              {
00089
                  cout « "Warning: Pivot element in row " « i + 1 « " is close to zero. The matrix may be
     singular." « endl;
00090
00091
              else
00092
              {
00093
                  Eliminate(m, i, rows, cols);
00094
00095
00096
              \ensuremath{//} Display current matrix state with optimized formatting
00097
              cout « "Current matrix state:" « endl;
00098
              for (int r = 0; r < rows; r++)
00099
00100
                   for (int c = 0; c < cols; c++)</pre>
00101
                      double coeff = round(m[r][c] * 1e12) / 1e12; // Handle floating-point precision if (fabs(coeff - round(coeff)) < 1e-12)
00102
00103
00104
00105
                           cout « static_cast<long long>(round(coeff)) « "\t";
00106
00107
                       else
00108
00109
                           cout « fixed « setprecision(2) « coeff « "\t";
00110
00111
00112
                  cout « endl;
00113
              cout « "----" « endl;
00114
          }
00115
00116
          return exchange_count;
00117 }
```

3.5.2.6 IdentifyPivots()

```
vector< int > IdentifyPivots ( {\rm const\ vector} <\ {\rm vector} <\ {\rm double}\ >\ {\rm \&}\ {\it m},
```

```
int rows,
               int cols)
00188 {
00189
          vector<int> pivots;
00190
          for (int i = 0; i < min(rows, cols - 1); i++)
00191
00192
              // Find the pivot in the current row
00193
              int pivot_col = -1;
00194
              for (int j = 0; j < cols - 1; j++)
00195
00196
                  if (fabs(m[i][j]) > 1e-12)
00197
00198
                      pivot_col = j;
00199
                      break;
00200
00201
00202
              if (pivot_col != -1)
00203
                  pivots.push_back(pivot_col);
00204
00205
          return pivots;
00206 }
```

3.5.2.7 Pivoting()

```
int Pivoting (
                 const vector< vector< double > > & m,
                 int current_row,
                 int total_rows)
00024 {
00025
           int imax = current_row;
           double max_val = fabs(m[current_row][current_row]);
for (int i = current_row + 1; i < total_rows; i++)</pre>
00026
00027
00028
                if (fabs(m[i][current_row]) > max_val)
00030
00031
                    imax = i;
00032
                    max_val = fabs(m[i][current_row]);
00033
00034
00035
           return imax;
00036 }
```

3.5.2.8 ShowGeneralSolution()

```
void ShowGeneralSolution (
                const vector< vector< double > > & m_{\star}
                int rows.
                int cols,
                int rank)
00209 {
           cout « "The system has infinitely many solutions." « endl;
cout « "Solution space dimension: " « (cols - 1 - rank) « endl;
00210
00211
00212
00213
           // Identify pivot columns
00214
           vector<int> pivots = IdentifyPivots(m, rows, cols);
00215
           // Identify free variables
00216
           vector<int> free_vars;
for (int j = 0; j < cols - 1; j++)</pre>
00217
00218
00219
00220
                if (find(pivots.begin(), pivots.end(), j) == pivots.end())
00221
00222
                    free_vars.push_back(j);
00223
                }
00224
           }
00225
00226
           // Assign parameters to free variables
00227
           int num_free = free_vars.size();
00228
           vector<string> params;
00229
           for (int i = 0; i < num_free; i++)</pre>
00230
00231
                params.push_back("t" + to_string(i + 1));
00232
           }
00233
```

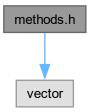
```
// Initialize solution vector with parameters
00235
           vector<double> particular_solution(cols - 1, 0.0);
00236
           vector<vector<double» basis_vectors;
00237
00238
           // Find a particular solution by setting all free variables to 0 for (int i = rows - 1; i \ge 0; i--)
00239
00241
                // Find the first non-zero coefficient in the row
00242
                int pivot_col = -1;
                for (int j = 0; j < cols - 1; j++)
00243
00244
00245
                     if (fabs(m[i][j]) > 1e-12)
00246
                    {
00247
                         pivot_col = j;
00248
00249
00250
                }
00251
                if (pivot_col == -1)
                {
00254
                    continue; // 0 = 0, skip
00255
00256
                double rhs = m[i][cols - 1];
00257
00258
                for (int j = pivot_col + 1; j < cols - 1; j++)</pre>
00260
                     rhs -= m[i][j] * particular_solution[j];
00261
00262
                particular_solution[pivot_col] = rhs / m[i][pivot_col];
00263
           }
00264
00265
           // Now, find basis vectors by setting each free variable to 1 and others to 0
00266
           for (int i = 0; i < num_free; i++)</pre>
00267
               vector<double> basis(cols - 1, 0.0);
basis[free_vars[i]] = 1.0; // Set the free variable to 1
00268
00269
00270
00271
                // Perform back-substitution for pivot variables
00272
                for (int r = rank - 1; r >= 0; r--)
00273
00274
                    int pivot_col = pivots[r];
                    double rhs = 0.0;
for (int j = pivot_col + 1; j < cols - 1; j++)</pre>
00275
00276
00277
00278
                         rhs -= m[r][j] * basis[j];
00279
00280
                    basis[pivot_col] = rhs / m[r][pivot_col];
00281
00282
00283
               basis vectors.push back(basis);
00284
           }
00285
00286
           // Display the general solution
           cout « "General solution:" « endl;
cout « "x = [";
00287
00288
00289
           for (int j = 0; j < cols - 1; j++)
00290
00291
                cout « fixed « setprecision(4) « particular_solution[j];
                if (j < cols - 2)
cout « ", ";
00292
00293
00294
00295
           cout « "]";
00296
00297
           for (int i = 0; i < num_free; i++)</pre>
00298
                cout « " + " « params[i] « " * [";
for (int j = 0; j < cols - 1; j++)</pre>
00299
00300
00301
00302
                    cout « fixed « setprecision(4) « basis_vectors[i][j];
                    if (j < cols - 2)
00303
                         cout « ", ";
00304
00305
               cout « "]";
if (i < num_free - 1)
    cout « " + ";</pre>
00306
00307
00308
00309
00310
           cout « endl
00311
                 « endl;
00312 }
```

3.6 methods.h File Reference

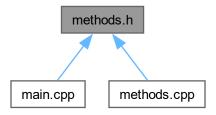
Core computational functions for solving linear systems.

#include <vector>

Include dependency graph for methods.h:



This graph shows which files directly or indirectly include this file:



Functions

- int GaussianElimination (std::vector< std::vector< double > > &m, int rows, int cols)

 Performs Gaussian elimination on the matrix.
- int DetermineRank (const std::vector < std::vector < double > > &m, int rows, int cols)
 Determines the rank of the matrix.
- bool BackSubstitution (const std::vector< std::vector< double >> &m, int rows, int cols, std::vector< double >> &solution)

Performs back-substitution to find the unique solution.

void ShowGeneralSolution (const std::vector< std::vector< double > > &m, int rows, int cols, int rank)
 Displays the general solution for systems with infinitely many solutions.

3.6.1 Detailed Description

Core computational functions for solving linear systems.

Author

Gilbert Young

Date

2024/09/25

3.6.2 Function Documentation

3.6.2.1 BackSubstitution()

Performs back-substitution to find the unique solution.

Parameters

т	The upper triangular matrix after Gaussian elimination	
rows	Number of rows in the matrix.	
cols	Number of columns in the matrix.	
solution	Reference to store the solution vector.	

Returns

true If a unique solution exists.

false If the system is inconsistent.

3.6.2.2 DetermineRank()

Determines the rank of the matrix.

Parameters

	m	The matrix.	
	rows	Number of rows in the matrix.	
cols Number of columns in the matri		Number of columns in the matrix.	

Returns

int The rank of the matrix.

3.6.2.3 GaussianElimination()

```
int GaussianElimination (
    std::vector< std::vector< double > > & m,
    int rows,
    int cols)
```

Performs Gaussian elimination on the matrix.

Parameters

m	Reference to the matrix to be modified.	
rows	Number of rows in the matrix.	
cols	Number of columns in the matrix.	

Returns

int Number of row exchanges performed.

3.6.2.4 ShowGeneralSolution()

Displays the general solution for systems with infinitely many solutions.

Parameters

m	The matrix after Gaussian elimination.
rows	Number of rows in the matrix.
cols	Number of columns in the matrix.
rank	The rank of the matrix.

3.7 methods.h

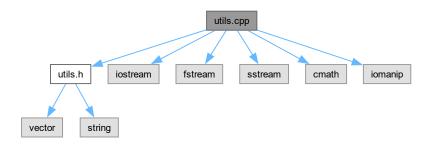
Go to the documentation of this file.

3.8 utils.cpp File Reference

Implementation of utility functions for matrix operations.

```
#include "utils.h"
#include <iostream>
#include <fstream>
#include <sstream>
#include <cmath>
#include <iomanip>
```

Include dependency graph for utils.cpp:



Functions

- bool InitMatrix (vector < vector < double > > &m, const string &filename, int &rows, int &cols)
- void ShowEquations (const vector< vector< double > > &m, int rows, int cols)
- bool CheckConsistency (const vector< vector< double > > &m, int rows, int cols)
- void DisplaySolution (const vector< double > &solution)

3.8.1 Detailed Description

Implementation of utility functions for matrix operations.

Author

Gilbert Young

Date

2024/09/25

This file contains the implementations of functions that handle reading matrices from .in files and displaying the corresponding system of linear equations. These utility functions are essential for the initialization and output of matrix data used in solving linear systems.

3.8.2 Function Documentation

3.8.2.1 CheckConsistency()

```
bool CheckConsistency (
              const vector< vector< double > > & m,
              int rows,
              int cols)
00113 {
00114
          for (int i = 0; i < rows; i++)</pre>
00115
              bool all_zero = true;
00116
              for (int j = 0; j < cols - 1; j++)</pre>
00117
00118
00119
                  if (fabs(m[i][j]) > 1e-12)
00120
00121
                      all_zero = false;
                      break;
00122
00123
                  }
00124
00125
              if (all_zero && fabs(m[i][cols - 1]) > 1e-12)
00126
00127
                  return false;
00128
00129
00130
          return true;
00131 }
```

3.8.2.2 DisplaySolution()

3.8.2.3 InitMatrix()

```
bool InitMatrix (
              vector< vector< double > > & m,
               const string & filename,
              int & rows,
              int & cols)
00024 {
00025
          ifstream in (filename);
00026
          if (!in.is open())
00027
          {
00028
              cerr « "Error: Cannot open file " « filename « endl;
00029
              return false;
00030
          }
00031
00032
          // Read the matrix dimensions dynamically
00033
          string line;
00034
          rows = 0;
00035
          cols = 0;
00036
          vector<vector<double» temp_matrix;
00037
          while (getline(in, line))
00038
              if (line.empty())
    continue; // Skip empty lines
00039
00040
00041
              vector<double> row;
00042
              double num;
00043
              istringstream iss(line);
00044
              while (iss » num)
00045
              {
00046
                  row.push_back(num);
```

3.9 utils.h File Reference 23

```
00048
               if (cols == 0)
00049
00050
                   cols = row.size();
00051
00052
               else if ((int)row.size() != cols)
00053
              {
00054
                   cerr \mbox{\tt ``Error: Inconsistent number of columns in the file." }\mbox{\tt ``endl;}
00055
                  in.close();
00056
                   return false;
00057
              }
00058
              temp_matrix.push_back(row);
00059
              rows++;
00060
00061
          in.close();
00062
          if (rows == 0 || cols < 2)
00063
00064
          {
              cerr « "Error: The matrix must have at least one equation and one variable." « endl;
00065
00066
              return false;
00067
00068
          // Assign to m
00069
00070
          m = temp_matrix;
00071
          return true;
00072 }
```

3.8.2.4 ShowEquations()

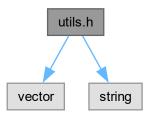
```
void ShowEquations (
               const vector< vector< double > > & m,
               int rows,
               int cols)
00075 {
           cout « "The current system of linear equations is:" « endl;
00076
00077
           for (int i = 0; i < rows; i++)</pre>
00078
00079
               string equation = "";
               for (int j = 0; j < cols - 1; j++)</pre>
08000
00081
               {
00082
                   // Check if the coefficient is an integer double coeff = round(m[i][j] \star 1e12) / 1e12; // Handle floating-point precision
00083
00084
                    if (fabs(coeff - round(coeff)) < 1e-12)</pre>
00085
                        equation += to_string(static_cast<long long>(round(coeff))) + "x" + to_string(j + 1);
00086
00087
                   }
00088
                   else
00089
                   {
00090
                        equation += to_string(round(m[i][j] * 10000) / 10000.0) + "x" + to_string(j + 1);
00091
                   }
00092
                   if (j < cols - 2)
    equation += " + ";</pre>
00093
00094
00095
               // Handle constant term
00096
00097
               double const_term = round(m[i][cols - 1] * 1e12) / 1e12;
00098
               if (fabs(const_term - round(const_term)) < 1e-12)</pre>
00099
               {
00100
                   equation += " = " + to_string(static_cast<long long>(round(const_term)));
00101
00102
               else
00103
               {
00104
                   equation += " = " + to_string(round(m[i][cols - 1] * 10000) / 10000.0);
00105
00106
00107
               cout « equation « endl;
00108
00109
           cout « endl;
00110 }
```

3.9 utils.h File Reference

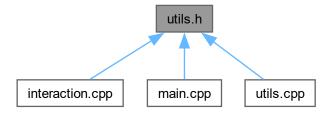
Utility functions for matrix initialization and display.

```
#include <vector>
#include <string>
```

Include dependency graph for utils.h:



This graph shows which files directly or indirectly include this file:



Functions

- bool InitMatrix (std::vector< std::vector< double > > &m, const std::string &filename, int &rows, int &cols)

 Initializes the matrix by reading from a .in file.
- void ShowEquations (const std::vector< std::vector< double > > &m, int rows, int cols)
 Displays the system of linear equations.
- bool CheckConsistency (const std::vector< std::vector< double > > &m, int rows, int cols)

 Checks the consistency of the system of equations.
- void DisplaySolution (const std::vector< double > &solution)
 Displays the unique solution.

3.9.1 Detailed Description

Utility functions for matrix initialization and display.

3.9 utils.h File Reference 25

Author

Gilbert Young

Date

2024/09/25

3.9.2 Function Documentation

3.9.2.1 CheckConsistency()

Checks the consistency of the system of equations.

Parameters

m	The matrix representing the system.
rows	Number of rows in the matrix.
cols	Number of columns in the matrix.

Returns

true If the system is consistent.

false If the system is inconsistent.

3.9.2.2 DisplaySolution()

```
void DisplaySolution ( {\tt const\ std::vector} < {\tt double} \ > \& \ solution)
```

Displays the unique solution.

Parameters

solution	The solution vector.
----------	----------------------

3.9.2.3 InitMatrix()

Initializes the matrix by reading from a .in file.

Parameters

m	Reference to the matrix to be initialized.	
filename	me Name of the input file.	
rows Reference to store the number of rows.		
cols	Reference to store the number of columns.	

Returns

true If the matrix was successfully initialized. false If there was an error during initialization.

3.9.2.4 ShowEquations()

Displays the system of linear equations.

Parameters

m	The matrix representing the system.	
rows	Number of equations.	
cols	Number of variables plus one (for constants).	

3.10 utils.h

Go to the documentation of this file.

```
00001
00008 #ifndef UTILS_H
00009 #define UTILS_H
00010
00011 #include <vector>
00012 #include <string>
00013
00024 bool InitMatrix(std::vector<std::vector<double» &m, const std::string &filename, int &rows, int &cols);
00025
00033 void ShowEquations(const std::vector<std::vector<double» &m, int rows, int cols);
00044 bool CheckConsistency(const std::vector<std::vector<double» &m, int rows, int cols);
00045
00051 void DisplaySolution(const std::vector<double> &solution);
00052
00053 #endif // UTILS_H
```

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