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# 24-Game Solver

An enhanced version of the 24-game solver using recursive search and pruning.

This program allows users to solve the 24-game using the following features:

- · Recursive search with pruning
- · Progress bar to monitor search progress
- · OpenMP parallelization for multi-core systems
- · Optimization for commutative operations (addition and multiplication)

Users can either use default settings or customize them according to their needs. The program outputs include:

- · The first valid solution for 24
- · Detailed recursive steps and expressions

Additionally, the program supports solving the game with varying number of inputs and halts upon finding a valid solution.

### 1.0.1 Key Features

- · Implements recursive search for the 24-game
- Supports up to 8 input numbers
- · OpenMP for parallelization on larger input sizes
- · Progress bar for visual feedback during the search process

## 1.0.2 How to Use

- 1. Compile the program with OpenMP support (gfortran -fopenmp).
- 2. Enter the number of numbers (between 1 and 8).
- 3. Provide the input numbers or card values (A=1, J=11, Q=12, K=13).
- 4. View the solution if found, or a message indicating no solution.

2 24-Game Solver

# **Modules Index**

Here is a list of all mo	dules	s with	n brie	f desc	riptio	ns:								
game24_module							 	 	 	 		 	 	7

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# **File Index**

# 3.1 File List

Here is a list of all files with brief descriptions:

game24_ultra.f90	
The main entry point for the 24-game solver, utilizing recursive search, progress bar, and Open←	
MP parallelization	15

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# **Module Documentation**

# 4.1 game24 module Module Reference

#### **Functions/Subroutines**

- subroutine convert\_to\_number (input\_str, number, ios)
  - Converts user input (cards or numbers) into numeric values.
- subroutine remove decimal zeros (str, result)

Removes trailing zeros after the decimal point in a string.

- subroutine create\_new\_arrays (nums, exprs, idx1, idx2, result, new\_expr, new\_nums, new\_exprs)
  - Creates new arrays after performing an operation.
- subroutine update\_progress\_bar ()

Updates and displays the horizontal percentage-based progress bar.

recursive subroutine solve 24 (nums, exprs, found)

Recursively solves the 24 game by trying all possible operations.

#### Variables

- integer, parameter max\_limit = 8
- integer, parameter expr len = 200
- integer(int64), parameter total calls n6 = 20000000 int64
- integer(int64), parameter total\_calls\_n7 = 2648275200\_int64
- integer(int64), parameter total calls n8 = 444557593600 int64
- integer(int64) total calls = 0
- integer(int64) completed\_calls = 0
- integer last\_percentage = -1
- integer, parameter progress\_bar\_width = 50
- character(len=1) carriage\_return = char(13)
- logical show\_progress = .false.

### 4.1.1 Function/Subroutine Documentation

#### 4.1.1.1 convert to number()

Converts user input (cards or numbers) into numeric values.

Handles card values such as 'A', 'J', 'Q', 'K'.

#### **Parameters**

input_str	String representing the number or card value
number	The corresponding numeric value after conversion
ios	I/O status indicator (0 for success)

```
00089
               implicit none
               character(len=*), intent(in) :: input_str
00090
                                       :: number
:: ios
:: first_char
00091
               real, intent(out)
00092
               integer, intent(out)
00093
               character(len=1)
00094
               real
                                               :: temp_number
00095
00096
               ios = 0 ! Reset the I/O status to 0 (valid input by default)
00097
               first_char = input_str(1:1)
00098
               select case (first_char)
case ('A', 'a')
00099
00100
               number = 1.0

case ('J', 'j')

number = 11.0
00101
00102
00103
               case ('Q', 'q')
00104
               number = 12.0
case ('K', 'k')
00105
00106
00107
                  number = 13.0
00108
00109
                   read (input str. *, iostat=ios) temp number ! Attempt to read a real number
00110
00111
                   ! If input is not a valid real number or is not an integer, set ios to 1
                   if (ios /= 0 .or. mod(temp_number, 1.0) /= 0.0) then
ios = 1 ! Invalid input
00112
00113
00114
                       number = temp_number ! Valid integer input
00115
00116
                    end if
00117
               end select
```

#### 4.1.1.2 create\_new\_arrays()

Creates new arrays after performing an operation.

#### Parameters

nums	Input array of numbers
exprs	Input array of expressions
idx1	Index of the first element to remove
idx2	Index of the second element to remove
result	Result of the operation
new_expr	New expression string
new_nums	Output array of numbers with elements removed and result added
new_exprs	Output array of expressions with elements removed and new_expr added

```
00155 implicit none
00156 real, intent(in) :: nums(:) ! Input: Array of numbers
00157 character(len=expr_len), intent(in) :: exprs(:) ! Input: Array of expressions
00158 integer, intent(in) :: idx1, idx2 ! Input: Indices of elements to remove
```

```
00159
               real, intent(in)
                                                          :: result
                                                                            ! Input: Result of the operation
                                                          :: new_expr ! Input: New expression
:: new_nums(:) ! Output: New array of numbers
00160
               character(len=expr_len), intent(in)
00161
               real, allocatable, intent(out)
              character(len=expr_len), allocatable, intent(out) :: new_exprs(:) ! Output: New array of
00162
      expressions
00163
               integer
                                                          :: i, i, n
                                                                            ! Loop counters and size of input
      arrays
00164
00165
              n = size(nums)
00166
               allocate (new_nums(n - 1))
               allocate (new_exprs(n - 1))
00167
00168
00169
               j = 0
               do i = 1, n
00170
00171
                  if (i /= idx1 .and. i /= idx2) then
00172
                       j = j + 1
                       new_nums(j) = nums(i)
00173
00174
                       new_exprs(j) = exprs(i)
00175
                   end if
00176
              end do
00177
00178
              ! Add the result of the operation to the new arrays
              new_nums(n-1) = result

new_exprs(n-1) = new_expr
00179
00180
```

#### 4.1.1.3 remove\_decimal\_zeros()

Removes trailing zeros after the decimal point in a string.

#### **Parameters**

str	Input string that may contain trailing zeros
result	Output string with trailing zeros removed

```
00124
              implicit none
               \texttt{character(len=*), intent(in)} \quad :: \ \texttt{str}
00125
                                                            ! Input: String to remove zeros from
                                                            ! Output: String without trailing zeros
00126
               character(len=*), intent(out) :: result
00127
              integer
                                               :: i, len_str ! Loop counter and string length
00128
00129
              len_str = len_trim(str)
00130
              result = adjust1(str(1:len_str))
00131
              ! Find the position of the decimal point i = index(result, '.')
00132
00133
00134
00135
               ! If there's a decimal point, remove trailing zeros
00136
               if (i > 0) then
00137
                  do while (len_str > i .and. result(len_str:len_str) == '0')
00138
                      len\_str = len\_str - 1
00139
                   end do
00140
                   if (result(len_str:len_str) == '.') len_str = len_str - 1
00141
                   result = result(1:len_str)
00142
               end if
```

## 4.1.1.4 solve\_24()

Recursively solves the 24 game by trying all possible operations.

Utilizes OpenMP tasks for parallelization.

#### **Parameters**

nums	Array of numbers to use in the game
exprs	Array of string expressions representing the numbers
found	Logical flag indicating if a solution has been found

```
00226
             use omp_lib
00227
              implicit none
00228
             real, intent(in)
                                                                        ! Input: Array of numbers
                                                        :: nums(:)
00229
              character(len=expr_len), intent(in)
                                                         :: exprs(:)
                                                                          ! Input: Array of expressions
                                                                        ! Input/Output: Flag indicating if a
00230
              logical, intent(inout)
                                                        :: found
     solution is found
00231
                                                                          ! Size of the input arrays
             integer
                                                        :: n
00232
                                                        :: i, j, op
                                                                          ! Loop counters
              integer
00233
                                                        :: a, b, result ! Temporary variables for
              real
     calculations
00234
             real, allocatable
                                                         :: new_nums(:)
                                                                         ! Temp array to store numbers after
     an operation
00235
             character(len=expr_len), allocatable
                                                        :: new_exprs(:) ! Temp array to store expressions
     after an operation
             character(len=expr_len)
                                                        :: expr_a, expr_b, new_expr ! Temp variables for
     expressions
00237
00238
              n = size(nums)
00239
00240
              ! Increment the completed_calls counter and update progress bar
00241
              if (show_progress) then
00242
                  !$omp atomic
00243
                  completed_calls = completed_calls + 1
00244
                  call update_progress_bar()
              end if
00245
00246
00247
              ! If a solution is found, return
00248
              if (found) return
00249
00250
              ! Base case: If only one number is left, check if it is 24
00251
              if (n == 1) then
                  \frac{1}{1} (abs(nums(1) - 24.0) < 1e-4) then
00252
00253
                      if (show_progress) then
     write (*, '(A, F5.1, A)', advance='no') carriage_return//'['//repeat('=', progress_bar_width)//'] ', 100.0, '%'
                          write (*, '(A)') " ! Insert a blank line
00255
00256
                      end if
                      !$omp critical
00257
                      write (*, '(A, A, A, F10.7, A)') 'Solution found:', trim(exprs(1)), '= 24 (', nums(1),
00258
00259
                      found = .true.
00260
                      !$omp end critical
00261
                  end if
00262
                  return
00263
              end if
00264
00265
              ! Iterate over all pairs of numbers
00266
              do i = 1, n - 1
00267
                  do j = i + 1, n
                      a = nums(i)
00268
                      b = nums(j)
00269
00270
                      expr_a = exprs(i)
00271
                      expr_b = exprs(j)
00272
00273
                      ! Iterate over all operators
                      do op = 1, 4
   ! Avoid division by zero
00274
00275
00276
                           if ((op == 4 .and. abs(b) < 1e-6)) cycle
00277
00278
                          ! Perform the operation and create the new expression
00279
                          select case (op)
                          case (1)
00280
00281
                              result = a + b
                               new_expr = '('//trim(expr_a)//'+'//trim(expr_b)//')'
00282
00283
                          case (2)
00284
                               result = a - b
                               new_expr = '('//trim(expr_a)//'-'//trim(expr_b)//')'
00285
00286
                           case (3)
00287
                              result = a * b
                              new_expr = '('//trim(expr_a)//'*'//trim(expr_b)//')'
00288
00289
                          case (4)
                              result = a / b
new_expr = '('//trim(expr_a)//'/'/trim(expr_b)//')'
00290
00291
00292
                          end select
00293
00294
                           ! Create new arrays with the selected numbers removed
00295
                          call create_new_arrays(nums, exprs, i, j, result, new_expr, new_nums, new_exprs)
00296
```

```
00297
                            ! For the first few recursion levels, create parallel tasks
00298
                            if (n \ge 6 .and. omp_get_level() < 2) then
00299
                                !$omp task shared(found) firstprivate(new_nums, new_exprs)
00300
                                call solve_24(new_nums, new_exprs, found)
00301
                                !$omp end task
00302
                            else
00303
                                call solve_24(new_nums, new_exprs, found)
00304
                            end if
00305
00306
                            ! If a solution is found, deallocate memory and return
00307
                            if (found) then
00308
                                deallocate (new nums)
00309
                                deallocate (new_exprs)
00310
00311
                            end if
00312
                            ! Handle commutative operations only once
00313
00314
                            if (op == 1 .or. op == 3) cycle
00315
00316
                            ! Swap operands for subtraction and division
00317
                            if (op == 2 .or. op == 4) then
00318
                                if (op == 4 .and. abs(a) < 1e-6) cycle ! Avoid division by zero
00319
00320
                                select case (op)
00321
                                case (2)
                                   result = b - a
00322
00323
                                    new_expr = '('//trim(expr_b)//'-'//trim(expr_a)//')'
00324
                                case (4)
                                    result = b / a
new_expr = '('//trim(expr_b)//'/'/trim(expr_a)//')'
00325
00326
00327
                                end select
00328
00329
                                ! Create new arrays with the selected numbers removed
00330
                                call create_new_arrays(nums, exprs, i, j, result, new_expr, new_nums,
      new_exprs)
00331
                                ! For the first few recursion levels, create parallel tasks if (n \geq 6 .and. omp_get_level() < 2) then
00332
00333
00334
                                     !$omp task shared(found) firstprivate(new_nums, new_exprs)
00335
                                     call solve_24 (new_nums, new_exprs, found)
00336
                                    !$omp end task
00337
                                else
00338
                                    ! Recursively call the solve_24 function with the new arrays
00339
                                    call solve_24 (new_nums, new_exprs, found)
00340
                                end if
00341
00342
                                ! If a solution is found, deallocate memory and return
00343
                                {\tt if} (found) then
00344
                                    deallocate (new_nums)
00345
                                    deallocate (new exprs)
00346
                                    return
00347
                                end if
00348
                            end if
00349
                   end do ! End of operator loop
end do ! End of j loop
00350
00351
              end do ! End of i loop
```

#### 4.1.1.5 update\_progress\_bar()

subroutine game24\_module::update\_progress\_bar

### Updates and displays the horizontal percentage-based progress bar.

```
implicit none
00186
              real :: percentage
00187
              \verb|integer|:: filled_length|
00188
              character(len=progress_bar_width) :: bar
00189
              \verb|integer :: int_percentage|\\
00190
00191
              if (total_calls == 0 .or. .not. show_progress) return ! Avoid division by zero and check the
00192
00193
              percentage = real(completed_calls) / real(total_calls) * 100.0
00194
00195
              ! Ensure percentage does not exceed 100%
00196
              if (percentage > 100.0) percentage = 100.0
00197
00198
              ! Calculate integer percentage
00199
              int_percentage = int(percentage)
00200
00201
              ! Update progress bar only when percentage increases by at least 1%
00202
              if (int_percentage > last_percentage) then
```

```
last_percentage = int_percentage
00204
00205
                       ! Calculate the filled length of the progress bar
00206
                      filled_length = min(int(percentage / 100.0 * progress_bar_width), progress_bar_width)
00207
00208
                       ! Construct the progress bar string
                       bar = repeat('=', filled_length)
                      if (filled_length < progress_bar_width) then
  bar = bar//'>'//repeat(' ', progress_bar_width - filled_length - 1)
00210
00211
00212
                       end if
00213
                      ! Print the progress bar and integer percentage write (*, '(A, F4.1, A)', advance='no') carriage_return//'['/bar//'] ', percentage, '%' call flush (0) ! Ensure output is displayed immediately
00214
00215
00216
00217
```

## 4.1.2 Variable Documentation

#### 4.1.2.1 carriage\_return

#### 4.1.2.2 completed calls

```
integer(int64) game24_module::completed_calls = 0
00052    integer(int64) :: completed_calls = 0     ! Number of completed recursive calls
```

### 4.1.2.3 expr\_len

```
integer, parameter game24_module::expr_len = 200
00043    integer, parameter :: expr_len = 200    ! Maximum length for expressions
```

## 4.1.2.4 last\_percentage

```
integer game24_module::last_percentage = -1
00053    integer :: last_percentage = -1
! Last percentage reported
```

### 4.1.2.5 max\_limit

```
integer, parameter game24_module::max_limit = 8 00042 integer, parameter :: max_limit = 8 ! Maximum allowed value for the number of inputs
```

### 4.1.2.6 progress\_bar\_width

```
integer, parameter game24_module::progress_bar_width = 50
00054    integer, parameter :: progress_bar_width = 50    ! Width of the progress bar
```

## 4.1.2.7 show\_progress

#### 4.1.2.8 total\_calls

```
integer(int64) game24_module::total_calls = 0
00051 integer(int64) :: total_calls = 0 ! Total number of recursive calls
```

## 4.1.2.9 total\_calls\_n6

```
integer(int64), parameter game24_module::total_calls_n6 = 20000000_int64
00046    integer(int64), parameter :: total_calls_n6 = 20000000_int64
```

## 4.1.2.10 total\_calls\_n7

```
integer(int64), parameter game24_module::total_calls_n7 = 2648275200_int64
00047    integer(int64), parameter :: total_calls_n7 = 2648275200_int64
```

### 4.1.2.11 total\_calls\_n8

```
integer(int64), parameter game24_module::total_calls_n8 = 444557593600_int64
00048    integer(int64), parameter :: total_calls_n8 = 444557593600_int64
```

# **File Documentation**

# 5.1 game24 ultra.f90 File Reference

The main entry point for the 24-game solver, utilizing recursive search, progress bar, and OpenMP parallelization.

#### **Modules**

• module game24 module

#### **Functions/Subroutines**

- subroutine game24\_module::convert\_to\_number (input\_str, number, ios)
  - Converts user input (cards or numbers) into numeric values.
- subroutine game24\_module::remove\_decimal\_zeros (str, result)
  - Removes trailing zeros after the decimal point in a string.
- subroutine game24\_module::create\_new\_arrays (nums, exprs, idx1, idx2, result, new\_expr, new\_nums, new exprs)
  - Creates new arrays after performing an operation.
- subroutine game24\_module::update\_progress\_bar ()
  - Updates and displays the horizontal percentage-based progress bar.
- recursive subroutine game24\_module::solve\_24 (nums, exprs, found)
- Recursively solves the 24 game by trying all possible operations.
- program game24\_ultra

#### Variables

- integer, parameter game24 module::max limit = 8
- integer, parameter game24\_module::expr\_len = 200
- integer(int64), parameter game24\_module::total\_calls\_n6 = 20000000\_int64
- integer(int64), parameter game24\_module::total\_calls\_n7 = 2648275200\_int64
- integer(int64), parameter game24\_module::total\_calls\_n8 = 444557593600\_int64
- integer(int64) game24\_module::total\_calls = 0
- integer(int64) game24 module::completed calls = 0
- integer game24\_module::last\_percentage = -1
- integer, parameter game24\_module::progress\_bar\_width = 50
- character(len=1) game24\_module::carriage\_return = char(13)
- logical game24\_module::show\_progress = .false.

16 File Documentation

# 5.1.1 Detailed Description

The main entry point for the 24-game solver, utilizing recursive search, progress bar, and OpenMP parallelization.

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Date

2024/09/15

# 5.1.2 Function/Subroutine Documentation

# 5.1.2.1 game24\_ultra()

program game24\_ultra

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