3/13/23, 3:47 PM OneNote

Problem 1

11 January 2022 09:59 AM



1)a EPP system using CDM method



EQ_HW2...

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```
%Assignment #2 Pla-Inelastic response of SDOF system using
%Central Difference Scheme
fid = fopen('El Centro Ground Motion data.txt') ; % open the text file
S = textscan(fid,'%s'); % text scan the data
fclose(fid) ;
                 % close the file
a_g = cellfun(\theta(x)str2double(x), S); % convert the cell array to double
% Remove NaN's which were strings earlier
a_g(isnan(a_g))=[];
col = 2;
count = 0:
temp_arr =[];
temp_row = [];
for i = 1:length(a_g)
    if count == col
        temp_arr = [temp_arr;
                    temp_row];
       count = 0:
       temp_row = [];
    end
    temp_row = [temp_row,a_g(i)];
    count = count +1;
end
temp_arr = [temp_arr;
            temp_row];
a_g = temp_arr(:,2:end);
a_g=a_g.*9.81;
clear temp_arr temp row S;
% Creating Time axis with zero padding of 20 sec
t=zeros(length(a_g),1);
for i=2:length(a g)+(20/0.02)
   t(i)=t(i-1)+0.02;
del_t=0.005;
dt=0.005; % Time step for EPP analysis
% Refning the time axis with dt=0.005
t1=0:0.005:51.180;
% Adding zero padding to the given Earthquake excitation data
a_g=[a_g;zeros((20/0.02),1)]; % appneding the a_g vector with zeros for the next 20 \, \text{L}
% interpolating the acceleration values within the refined time range
a_g1=interp1(t,a_g,t1);
Tn=0.5; %Natural Period of the system
Z=0.0; %Damping ratio
m=1; %Considering unit mass
Wn=(2*pi)/Tn; %Natural Frequency
k=m*Wn^2; %Linear elastic Stiffness
Wd=Wn*sqrt(1-Z^2); %Damped Natural Frequency
%Defining Parameters required A,B,C,D & A1,B1,C1,D1
\texttt{A=exp}\left(-\texttt{Z*Wn*del\_t}\right)*\left(\left(\texttt{Z/sqrt}\left(1-\texttt{Z}^2\right)\right)*sin\left(\texttt{Wd*del\_t}\right)+cos\left(\texttt{Wd*del\_t}\right)\right);
B=exp(-Z*Wn*del_t)*(sin(Wd*del_t)/Wd);
(Wd*del_t) - (1+((2*Z)/(Wn*del_t)))*cos(Wd*del_t)))/Wn^2;
D=(1-((2*Z)/(Wn*del_t))+exp(-Z*Wn*del_t)*(((2*Z^2-1)/(Wd*del_t))*sin(Wd*del_t)+((2*Z)/*
```

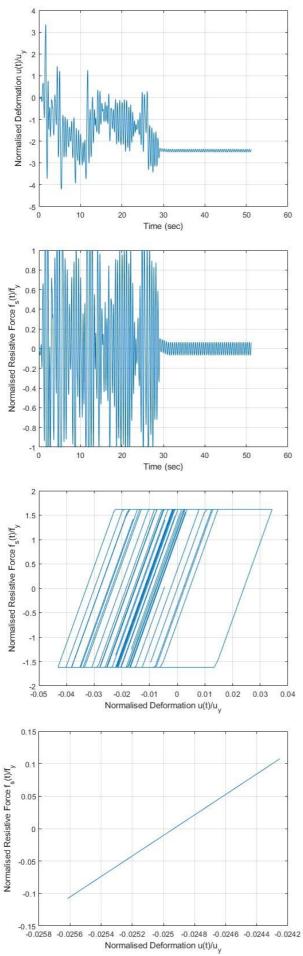
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```
(Wn*del_t))*cos(Wd*del_t)))/Wn^2;
Al=-exp(-Z*Wn*del_t)*((Wn/sqrt(1-Z^2))*sin(Wd*del_t));
Bl=exp(-Z*Wn*del_t)*(cos(Wd*del_t)-(Z/sqrt(1-Z^2))*sin(Wd*del_t));
Cl=((-1/del_t)+exp(-Z*Wn*del_t)*(((Wn/(sqrt(1-Z^2)))+(Z/(del_t*sqrt(1-Z^2))))*sin*
(Wd*del_t)+(cos(Wd*del_t)/del_t)))/Wn^2;
Dl=(1-exp(-Z*Wn*del_t)*((Z/sqrt(1-Z^2)))*sin(Wd*del_t)+cos(Wd*del_t)))/(Wn^2*del_t);
u=zeros(length(a_g1),1); %Initialising displacement response vector of the SDOF system v=zeros(length(a_g1),1); %Initialising velocity response vector of the SDOF system
```

```
for i=1:length(a_g1)-1
    u(i+1) = A*u(i) + B*v(i) - C*a g1(i) - D*a g1(i+1);
    v(i+1)=A1*u(i)+B1*v(i)-C1*a g1(i)-D1*a g1(i+1);
    acc(i+1)=-a_g1(i+1)-2*Z*Wn*v(i+1)-Wn^2*u(i+1);
end
a t=a g1+acc;
umax=abs(max(u));
f_0=k*umax; %Max. Force for system to remain Linear Elastic
% Performing Inelastic Response Analysis
u epp=zeros(length(a g1),1);
v_epp=zeros(length(a_g1),1);
a_epp=zeros(length(a_g1),1);
%Initial calculations:
fs=zeros(length(a_g1),1);
fs(1)=k*u_epp(1);
Ry=8; %Yield Strength reduction factor
fy=f_0/Ry; %yield strength of the system
u_0=u_epp(1)-dt*v_epp(1)+0.5*dt^2*a_epp(1);
k_{\text{hat}} = (m/dt^2) + ((m*Z*Wn)/dt); %effective stiffness
a=(m/dt^2)-((m*Z*Wn)/dt); %Integration parameter
b=(2*m)/dt^2; %Integration parameter
p_hat=0;du=0;fst=0;
for i=1:length(a_g1)-1
   if i==1
        p_hat=-m*a_g1(1)-a*u_0-fs(1)+b*u_epp(1);
        u_epp(2)=p_hat/k_hat;
        v_{epp}(1) = (u_{epp}(2) - u_0) / (2*dt);
        a_{\tt epp\,(1)} = (u_{\tt epp\,(2)} - 2 * u_{\tt epp\,(1)} + u_{\tt 0}) / dt^2;
    else
        {\tt p\_hat = -m*a\_g1(i) - a*u\_epp(i-1) - fs(i) + b*u\_epp(i);}\\
        u_epp(i+1)=p_hat/k_hat;
        v_{epp}(i) = (u_{epp}(i+1) - u_{epp}(i-1)) / (2*dt);
        \verb"a_epp"(i) = (\verb"u_epp"(i+1) - 2*"u_epp"(i) + \verb"u_epp"(i-1)") / dt^2;
    end
    du=u_epp(i+1)-u_epp(i);
    fst=fs(i)+k*du;
    if abs(fst)>fy
       fs(i+1)=sign(fst)*fy;
    else
       fs(i+1)=fst;
    end
u m=max(abs(u epp)); %Maximum displacement
meu=u_m/(fy/k);
%Finding the residual displacement
```

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```
if fs(end)>0
    u_r=u_epp(end)-(fs(end)/k);
elseif fs(end)<0
    u_r=u_epp(end)+(fs(end)/k);
end
figure(1)
title('Normalised Time history of deformation response')
plot(t1,u_epp./(fy/k))
xlabel('Time (sec)');
ylabel('Normalised Deformation u(t)/u {y}');
grid on
figure(2)
title('Normalised Time History of Resistive Force')
plot(t1,fs./fy);
xlabel('Time (sec)');
vlabel('Normalised Resistive Force f {s}(t)/f {y}');
grid on
figure(3)
title ('Normalised Force vs Normalised Deformation Hysteritic response')
plot(u epp,fs);
xlabel('Normalised Deformation u(t)/u {y}');
ylabel('Normalised Resistive Force f_{s}(t)/f_{y}');
grid on
figure (4)
title('Normalised Force vs Normalised Deformation Hysteritic response for free\ell
vibration phase only');
plot(u_epp(6238:(end),1),fs(6238:(end),1));
xlabel('Normalised Deformation u(t)/u_{y}');
ylabel('Normalised Resistive Force f {s}(t)/f {y}');
fprintf('Ductility Demand=%8.3e\n',meu);
fprintf('Normalised Permanent Deformation=\88.3e',u_r);
```



The calculated Ductility Demand (μ) = 4.204 Residual Normalized Deformation (Ur/Uy)= 2.453

1)b EPP system using KR- $\!\alpha$ Method:

EQ_HW2...

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```
%Assignment #2 P1b-Inelastic response of SDOF system using
%KR-Alpha Scheme
clc
fid = fopen('El Centro Ground Motion data.txt') ; % open the text file
S = textscan(fid,'%s'); % text scan the data
                  % close the file
fclose(fid);
S = S\{1\};
a g = cellfun(\theta(x)str2double(x), S); % convert the cell array to double
% Remove NaN's which were strings earlier
a_g(isnan(a_g))=[];
col = 2;
count = 0;
temp_arr =[];
temp_row = [];
for i = 1:length(a g)
   if count == col
        temp_arr = [temp_arr;
                   temp_row];
        count = 0;
       temp_row = [];
    end
    temp_row = [temp_row,a_g(i)];
   count = count +1;
end
temp_arr = [temp_arr;
           temp_row];
a_g = temp_arr(:,2:end);
a_g=a_g.*9.81;
clear temp_arr temp_row S;
% Creating Time axis with zero padding of 20 sec
t=zeros(length(a_g),1);
for i=2:length(a_g)+(20/0.02)
   t(i)=t(i-1)+0.02;
end
t1=0:0.005:51.180; % Refning the time axis with dt=0.005
a_g=[a_g;zeros((20/0.02),1)]; % appneding the a_g vector with zeros for the next 20 \checkmark
Tn=0.5; %Natural Period of the system
Z=0.0; %Damping ratio
m=1; %Considering unit mass
Wn=(2*pi)/Tn; %Natural Frequency
k=m*Wn^2; %Linear elastic Stiffness
f_0=k*0.082; %Using the maximum displacement value for this system from the previous {m \ell}
LE analysis
% Performing Inelastic Response Analysis
% interpolating the acceleration values within the refined time range
a_g1=interp1(t,a_g,t1);
u_epp=zeros(length(a_g1),1);
v_epp=zeros(length(a_g1),1);
a_epp=zeros(length(a_g1),1);
dt=0.005; % Time step for EPP analysis
%Initial calculations:
fs=zeros(length(a_g1),1);
fs(1)=k*u_epp(1); %Initial resistive force
Ry=8; %Yield Strength reduction factor
```

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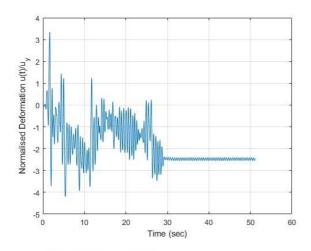
```
fy=f 0/Ry; %yield strength of the system
 a_{epp}(1) = (-m*a_g1(1) - 2*m*Z*Wn*v_{epp}(1) - fs(1)) / m; \$Initial acceleration 
%Defining the constants to be used
p inf=1;
am=(2*p_inf-1)/(p_inf+1); af=p_inf/(p_inf+1);
Y=0.5-am+af; B=0.25*(0.5+Y)^2;
a1=m/(m+Y*dt*2*Z*m*Wn+B*dt^2*k);
a2=a1*(0.5+Y);
a3=(am*m+af*Y*dt*2*Z*m*Wn+af*B*dt^2*k)/(m+Y*dt*2*Z*m*Wn+B*dt^2*k);
for i=1:length(a_g1)-1
    v_epp(i+1)=v_epp(i)+dt*a1*a_epp(i);
u_epp(i+1)=u_epp(i)+dt*v_epp(i)+dt^2*a2*a_epp(i);
    du=u epp(i+1)-u epp(i);
    fst=fs(i)+k*du;
    if abs(fst)>fy %state determination
        fs(i+1)=sign(fst)*fy;
```

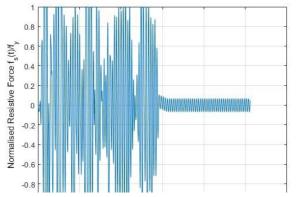
```
intvel=(1-af)*v_epp(i+1)+af*v_epp(i);
    intf=(1-af)*fs(i+1)+af*fs(i);
    intp=(1-af)*(-m*a_g1(i+1))+af*(-m*a_g1(i));
    a hat=(intp-2*Z*m*Wn*intvel-intf)/m;
    a_epp(i+1) = (a_hat-a3*a_epp(i))/(1-a3);
end
u_m=max(abs(u_epp)); %Maximum displacement
meu=u m/(fy/k);
%Finding the residual displacement
if fs(end)>0
   u_r=u_epp(end)-(fs(end)/k);
elseif fs(end)<0
   u_r=u_epp(end)+(fs(end)/k);
figure(1)
title('Normalised Time history of deformation response')
plot(t1,u_epp./(fy/k))
xlabel('Time (sec)');
ylabel('Normalised Deformation u(t)/u_{y}');
figure(2)
title('Normalised Time History of Resistive Force')
plot(t1,fs./fy);
xlabel('Time (sec)');
ylabel('Normalised Resistive Force f_{s}(t)/f_{y}');
grid on
figure(3)
title('Normalised Force vs Normalised Deformation Hysteritic response')
plot(u_epp,fs);
xlabel('Normalised Deformation u(t)/u {y}');
{\tt ylabel('Normalised\ Resistive\ Force\ f_{s}(t)/f_{y}');}
grid on
figure (4)
title('Normalised Force vs Normalised Deformation Hysteritic response for free≰
vibration phase only');
plot(u_epp(6238:(end),1),fs(6238:(end),1));
```

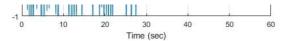
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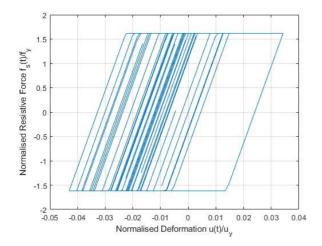
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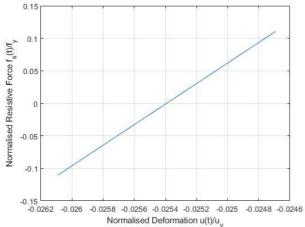
EQ HW2 P1b.m











The calculated Ductility Demand (μ) = 4.200 Residual Normalized Deformation (Ur/Uy)= 2.48

1)C EPP system using Newmark-Beta with Newton Raphson Iteration



EQ_HW2...

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EQ_HW2_P1c.m

```
%Assignment #2 P1b-Inelastic response of SDOF system using
%KR-Alpha Scheme
clc
fid = fopen('El Centro Ground Motion data.txt') ; % open the text file
S = textscan(fid,'%s'); % text scan the data
                   % close the file
fclose(fid) ;
S = S\{1\};
a_g = cellfun(\theta(x)str2double(x), S); % convert the cell array to double
% Remove NaN's which were strings earlier
a_g(isnan(a_g))=[];
col = 2;
count = 0;
temp_arr =[];
temp_row = [];
for i = 1:length(a_g)
    if count == col
        temp_arr = [temp_arr;
                    temp_row];
        count = 0;
        temp_row = [];
    end
    temp_row = [temp_row,a_g(i)];
    count = count +1;
end
temp_arr = [temp_arr;
           temp_row];
a_g = temp_arr(:,2:end);
a_g=a_g.*9.81;
clear temp_arr temp_row S;
% Creating Time axis with zero padding of 20 sec
t=zeros(length(a_g),1);
```

```
for i=2:length(a_g)+(20/0.02)
   t(i)=t(i-1)+0.02;
end
t1=0:0.005:51.180; % Refning the time axis with dt=0.005
\texttt{a\_g=[a\_g;zeros((20/0.02),1)]; \$ appneding the a\_g vector with zeros for the next 20 \textit{\textbf{x}'}}
sec.
Tn=0.5; %Natural Period of the system
Z=0.0; %Damping ratio
m=1; %Considering unit mass
Wn=(2*pi)/Tn; %Natural Frequency
k=m*Wn^2; %Linear elastic Stiffness
c=2*Z*Wn*m; % Damping coefficient
f 0=k*0.082; %Using the maximum displacement value for this system from the previous ✓
LE analysis
% Performing Inelastic Response Analysis
% interpolating the acceleration values within the refined time range
a_g1=interp1(t,a_g,t1);
u epp=zeros(length(a g1),1);
v epp=zeros(length(a g1),1);
a_epp=zeros(length(a_g1),1);
dt=0.005; % Time step for EPP analysis
%Initial calculations:
fs=zeros(length(a_g1),1);
fs(1)=k*u_epp(1); %Initial resistive force
```

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EQ HW2 P1c.m

```
Ry=8; %Yield Strength reduction factor
fy=f_0/Ry; %yield strength of the system
a_{pp}(1) = (-m*a_g1(1) - c*v_pp(1) - fs(1))/m;  %Initial acceleration
%Defining the constants to be used
Y=1/2; B=1/4; % Gamma and Beta for Newmark's Constant Avg Acc. method
a1 = (1/(B*dt^2))*m+(Y/(B*dt))*c;
a2 = (1/(B*dt))*m+(Y/B-1)*c;
a3 = (1/(2*B)-1)*m+dt*(Y/(2*B)-1)*c;
kt=zeros(length(a_g1),1);
kt(i)=k; %Initial tangent stiffness equal to the LE stiffness
k hat=zeros(length(a_g1),1);
p_hat=zeros(length(a_g1),1);
p resi=zeros(length(a g1),1);
for i=1:length(a g1)-1
   u_epp(i+1)=u_epp(i);fs(i+1)=fs(i);kt(i+1)=kt(i);
   p_hat(i+1)=-m*a_g1(i+1)+a1*u_epp(i)+a2*v_epp(i)+a3*a_epp(i);
   p_resi(i+1)=p_hat(i+1)-fs(i+1)-a1*u_epp(i+1);
   while abs(p_resi(i+1))>0.001
       k_hat(i+1)=kt(i+1)+a1;
       du=p resi(i+1)/k hat(i+1);
       u epp(i+1)=u epp(i+1)+du;
       fst=fs(i+1)+kt(i+1)*du;
       if abs(fst)>fy %state determination
           fs(i+1)=sign(fst)*fy;
           kt(i+1)=0;
          fs(i+1)=fst;
           kt(i+1)=k;
       p resi(i+1)=p hat(i+1)-fs(i+1)-a1*u epp(i+1);
   *a epp(i);
end
u_m=max(abs(u_epp)); %Maximum displacement
meu=u m/(fy/k);
%Finding the residual displacement
if fs(end)>0
   u_r=abs(u_epp(end)-(fs(end)/k))/(fy/k);
elseif fs(end)<0
   u_r=abs(u_epp(end)+(fs(end)/k))/(fy/k);
end
figure (1)
title('Normalised Time history of deformation response')
plot(t1,u epp./(fv/k))
xlabel('Time (sec)');
ylabel('Normalised Deformation u(t)/u {y}');
grid on
figure(2)
title('Normalised Time History of Resistive Force')
plot(t1,fs./fy);
xlabel('Time (sec)');
ylabel('Normalised Resistive Force f_{s}(t)/f_{y}');
```

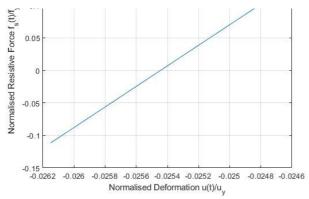
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Normalised Deformation u(t)/u

Normalised Resistive Force f_(t)/f

Normalised Resistive Force f_s(t)/f

```
grid on
  figure(3)
  title('Normalised Force vs Normalised Deformation Hysteritic response')
  plot(u_epp,fs);
  xlabel('Normalised Deformation u(t)/u_{y}');
ylabel('Normalised Resistive Force f_(s)(t)/f_{y}');
  grid on
  figure (4)
  title('Normalised Force vs Normalised Deformation Hysteritic response for free
  vibration phase only');
  plot(u_epp(6238:(end),1),fs(6238:(end),1));
  xlabel('Normalised Deformation u(t)/u_{y}');
  ylabel('Normalised Resistive Force f_{s}(t)/f_{y}');
  fprintf('Ductility Demand=%8.3e\n',meu);
  fprintf('Normalised Permanent Deformation=%8.3e',u_r);
  3
 -2
  -4
 -5 L
0
            10
                     20
                               30
                                        40
                                                  50
                                                           60
                           Time (sec)
0.8
0.6
0.4
0.2
  0
-0.2
-0.4
-0.6
-0.8
                           Time (sec)
  2
1.5
0.5
 0
-0.5
  -2
-0.05
        -0.04
                    -0.02 -0.01
              -0.03
                                  0
                                       0.01
                                             0.02
                                                   0.03 0.04
                  Normalised Deformation u(t)/u<sub>v</sub>
0.15
```



The calculated Ductility Demand (μ) = 4.207 Residual Normalized Deformation (Ur/Uy)= 2.482

Comments:

We observe that the 3 methods give very similar results for the EPP system. The CDM and the KR- α method are both explicit whereas the Newton-Raphson driven Newmark-Beta method is implicit.