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## Problem 2

11 January 2022 09:59 AM





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%Problem #2 Response Spectrum analysis for various cases of Damping
fid = fopen('El Centro Ground Motion data.txt') ; % open the text file
S = textscan(fid,'%s'); % text scan the data
fclose(fid) ;
                   % close the file
S = S\{1\};
a_g = cellfun(\theta(x)str2double(x), S); % convert the cell array to double
% Remove NaN's which were strings earlier
a_g(isnan(a_g))=[];
col = 2;
count = 0:
temp_arr =[];
temp_row = [];
for i = 1:length(a_g)
    if count == col
        temp_arr = [temp_arr;
                      temp row];
        count = 0;
        temp_row = [];
    temp_row = [temp_row,a_g(i)];
    count = count +1;
end
temp_arr = [temp_arr;
            temp_row];
a g = temp arr(:,2:end);
a_g=a_g.*9.81;
clear temp_arr temp_row S;
% Creating Time axis
t=zeros(length(a g),1);
for i=2:length(a_g)
    t(i)=t(i-1)+0.02;
end
del t=t(2)-t(1);
%Producing ground velocity data
v_g=zeros(length(a_g),1);
for i=1:length(a_g)-1
   v_g(i+1)=v_g(i)+(del_t*(a_g(i+1)+a_g(i)))/2;
%Producing ground displacement data
u_g=zeros(length(a_g),1);
for i=1:length(a_g)-1
     u_g(i+1) = u_g(i) + del_t * v_g(i) + del_t * del_t * ((a_g(i+1)/6) + (a_g(i)/3)); 
end
%Producing System response data
{\tt Tn=zeros\,(300,1);} %vector storing the natural periods of the system {\tt z=[0,0.02,0.05,0.1,0.2];} %vector storing the damping ratios
m=1: %mass of the system as unity
SD=zeros(300,length(z));
PSV=zeros(300,length(z));
PSA=zeros(300,length(z));
```

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for l=1:length(z)
  cnt=1;
  for j=0.01:0.01:3
      Tn(cnt)=j; %Natural Period of the system
      Z=z(1);
      Wn=(2*pi)/j; %Natural Frequency
      Wd=Wn*sqrt(1-Z^2); %Damped Natural Frequency
      %Defining Parameters required A,B,C,D & A1,B1,C1,D1
      A=exp(-Z*Wn*del_t)*((Z/sqrt(1-Z^2))*sin(Wd*del_t)+cos(Wd*del_t));
      B=exp(-Z*Wn*del_t)*(sin(Wd*del_t)/Wd);
```

```
\texttt{C=(((2*Z)/(Wn*del_t))+exp(-Z*Wn*del_t)*(((1-2*Z^2)/(Wd*del_t)-(Z/sqrt(1-Z^2))))} \, \textbf{\textit{x}}
*sin(Wd*del_t)-(1+((2*Z)/(Wn*del_t)))*cos(Wd*del_t)))/Wn^2;
        D = \frac{1 - ((2*Z) / (Wn*del_t)) + exp(-Z*Wn*del_t) * (((2*Z^2-1) / (Wd*del_t)) * sin(Wd*del_t) + k')}{2 + k'}
((2*Z)/(Wn*del_t))*cos(Wd*del_t)))/Wn^2;
        A1=-exp(-Z*Wn*del_t)*((Wn/sqrt(1-Z^2))*sin(Wd*del_t));
        B1=exp(-Z*Wn*del_t)*(cos(Wd*del_t)-(Z/sqrt(1-Z^2))*sin(Wd*del_t));
        C1=((-1/del_t)+exp(-Z*Wn*del_t)*(((Wn/(sqrt(1-Z^2)))+(Z/(del_t*sqrt(1-Z^2))))*sin√
(Wd*del_t)+(cos(Wd*del_t)/del_t)))/Wn^2;
        D1=(1-exp(-Z*Wn*del t)*((Z/sqrt(1-Z^2))*sin(Wd*del t)+cos(Wd*del t)))/
(Wn^2*del t);
        system
        v{=}zeros\,(length\,(a\_g)\,,1)\,;\,\,\$Initial ising\,\,velocity\,\,response\,\,vector\,\,of\,\,the\,\,SDOF\,\,system
        a = zeros (length(a\_g), 1); \ \$Initialising \ Acceleration \ response \ vector \ for \ the \ SDOF \textbf{\textit{v}}
system
        for i=1:length(a_g)-1
            u(i+1) = A*u(i) + B*v(i) - C*a_g(i) - D*a_g(i+1);
            v(i+1) = A1*u(i) + B1*v(i) - C1*a_g(i) - D1*a_g(i+1);
            a(i+1) = -a_g(i+1) - 2*Z*Wn*v(i+1) - Wn^2*u(i+1);
        end
        SD(cnt,1)=max(abs(u)); %spectral displacement
        PSV(cnt,1)=max(abs(Wn*u)); %Pseudo Spectral Velocity
        PSA(cnt,1)=max(abs(Wn^2*u)); %Pseudo Spectral acceleration
        cnt=cnt+1:
    end
end
%plotting SD response Spectra
figure(1)
title('Spectral Displacement(SD) Response Spectra')
plot(Tn.SD(:.1).'red');
hold on
plot(Tn, SD(:,2), 'blue');
hold on
plot(Tn,SD(:,3), 'magenta');
hold on
plot(Tn,SD(:,4), 'green');
plot(Tn,SD(:,5),'black');
hold on
xlabel('Natural Period(sec)');
ylabel('SD(m)');
```

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```
legend('0%Damping','2%Damping','5%Damping','10%Damping','20%Damping');
%Plotting PSV response spectra
figure(2)
title('Pseudo Spectral Velocity(PSV) Response Spectra')
plot(Tn, PSV(:,1), 'red');
hold on
plot(Tn, PSV(:,2), 'blue');
hold on
plot(Tn, PSV(:,3), 'magenta');
hold on
plot(Tn, PSV(:,4), 'green');
hold on
plot(Tn, PSV(:,5), 'black');
hold on
xlabel('Natural Period(sec)');
ylabel('PSV(m/s)');
legend('0%Damping','2%Damping','5%Damping','10%Damping','20%Damping');
%Plotting PSA response spectra
figure(3)
title('Pseudo Spectral Acceleration(PSA) Response Spectra')
plot(Tn, PSA(:,1)./9.81, 'red');
hold on
plot(Tn, PSA(:,2)./9.81, 'blue');
hold on
plot(Tn, PSA(:,3)./9.81, 'magenta');
hold on
plot(Tn, PSA(:,4)./9.81, 'green');
hold or
plot(Tn, PSA(:,5)./9.81, 'black');
hold on
xlabel('Natural Period(sec)');
ylabel('PSA(g)');
legend('0%Damping','2%Damping','5%Damping','10%Damping','20%Damping');
```

0.7 — 0%Damping — 2%Damping