

CS 4641 Homework 4

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1 Problem 1

(a) The proposed neural network for this function:

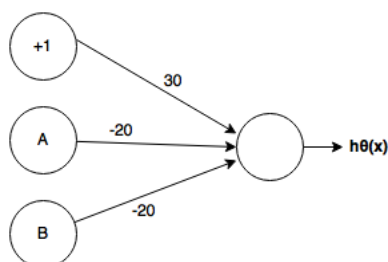


Figure 1: NAND NN

Not let's verify that the proposed neural network is correct. The formula for this neural network is:

$$h_{\theta}(X) = g(30 - 20A - 20B)$$

The truth table for the NAND function of 2 inputs:

| A | B | $\neg(A \wedge B)$ | $h_{\theta}(X)$ |
|-----|-----|--------------------|--------------------------------------|
| 0 | 0 | 1 | $g(30 + 0 + 0) = g(30) \approx 1$ |
| 0 | 1 | 1 | $g(30 - 20 + 0) = g(10) \approx 1$ |
| 1 | 0 | 1 | $g(30 + 0 - 20) = g(10) \approx 1$ |
| 1 | 1 | 0 | $g(30 - 20 - 20) = g(-10) \approx 0$ |

Proofed!

(b) My logical function to solve the problem:

$$h_{\theta}(X) = (A \oplus B) \oplus C$$

Based on the above equation, my proposed neural network for this function is:

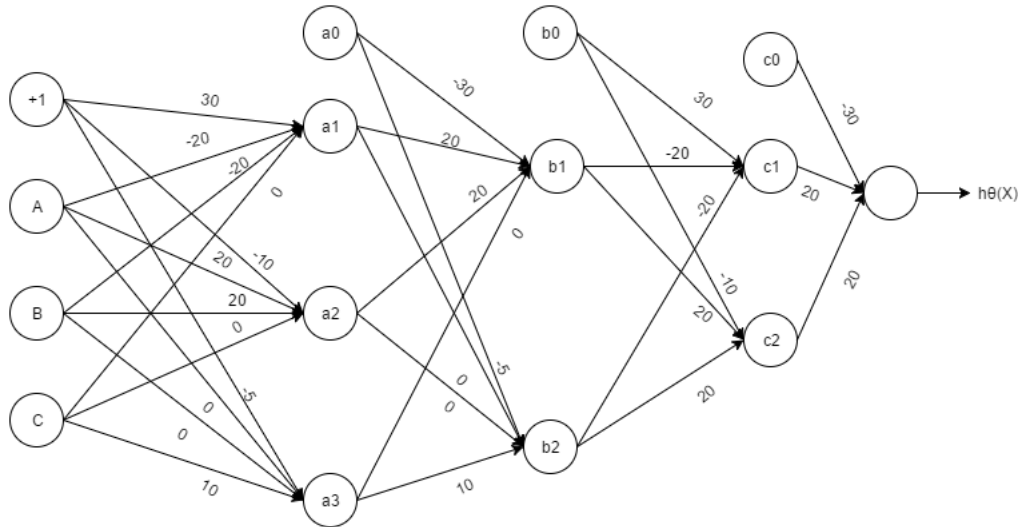


Figure 2: 3-bit Parity NN

The truth table for the even parity function of 3 inputs (The formula is only for the last layer):

| A | B | C | $(A \oplus B) \oplus C$ | $h_{\theta}(X)$ |
|-----|-----|-----|-------------------------|--------------------|
| 0 | 0 | 0 | 0 | $g(-30) \approx 0$ |
| 0 | 0 | 1 | 1 | $g(10) \approx 1$ |
| 0 | 1 | 0 | 1 | $g(10) \approx 1$ |
| 0 | 1 | 1 | 0 | $g(-10) \approx 0$ |
| 1 | 0 | 0 | 1 | $g(10) \approx 1$ |
| 1 | 0 | 1 | 0 | $g(-10) \approx 0$ |
| 1 | 1 | 0 | 0 | $g(-10) \approx 0$ |
| 1 | 1 | 1 | 1 | $g(10) \approx 1$ |

Proofed!

2 Problem 2

In this problem I will provide all calculation step by step until I calculated the weights after first 2 epochs:

$$\theta = [0.1, 0.1, 0.1], [0.1, 0.1]$$

FIRST EPOCH:

First training set:

$$a_1 = [1, 1, 0]$$

$$a_2 = g(0.1 \times 1 + 0.1 \times 0 + 0.1 \times 1) = g(0.2) = 0.549$$

$$a_3 = g(0.1 \times 1 + 0.1 \times 0.549) = g(0.1549) = 0.538$$

$$\delta_3 = a_3 - y = 0.538 - 1 = -0.461$$

$$\delta_2 = \theta^T \times \delta_3 \cdot g'(z_2)$$

$$\delta_2 = -0.0113$$

$$\Delta^{11} = a_1 \delta_2 = [-0.0113, -0.0113, 0]$$

$$\Delta^{12} = a_2 \delta_3 = [-0.461, -0.253]$$

Second training set:

$$a_1 = [1, 0, 1]$$

$$a_2 = g(0.1 \times 1 + 0.1 \times 0 + 0.1 \times 1) = g(0.2) = 0.549$$

$$a_3 = g(0.1 \times 1 + 0.1 \times 0.549) = g(0.1549) = 0.538$$

$$\delta_3 = a_3 - y = 0.538 - 0 = 0.538$$

$$\delta_2 = \theta^T \times \delta_3 \cdot g'(z_2)$$

$$\delta_2 = -0.0113$$

$$\Delta^{21} = a_1 \delta_2 = [0.0113, 0, 0.0113]$$

$$\Delta^{22} = a_2 \delta_3 = [0.538, 0.295]$$

Combining both Deltas from both training set:

$$\Delta^1 = \Delta^{11} + \Delta^{21} = [0.002, -0.0113, 0.0113]$$

$$\Delta^2 = \Delta^{12} + \Delta^{22} = [0.077, 0.0424]$$

$$D_1 = 0.5 \times \Delta^1 = [0.001, 0.00565, 0.00665]$$

$$D_2 = 0.5 \times \Delta^2 = [0.0385, 0.0212]$$

Update to the weight after first epoch:

$$\theta_1 = [0.1, 0.1, 0.1] - 0.3[0.001, -0.0056, 0.0066] = [0.099, 0.1016, 0.098]$$

$$\theta_2 = [0.1, 0.1] - 0.3[0.038, 0.021] = [0.884, 0.093]$$

SECOND EPOCH:

First training set:

$$a_1 = [1, 1, 0]$$

$$a_2 = g(0.0997 \times 1 + 0.101695 \times 1) = g(0.2013) = 0.55017$$

$$a_3 = g(0.08845 \times 1 + 0.0936 \times 0.55017) = g(0.1399) = 0.5349$$

$$\delta_3 = a_3 - y = 0.5349 - 1 = -0.46506$$

$$\delta_2 = \theta^T \times \delta_3 \cdot g'(z_2)$$

$$\delta_2 = -0.01077$$

$$\Delta^{11} = a_1 \delta_2 = [-0.01077, -0.01077, 0]$$

$$\Delta^{12} = a_2 \delta_3 = [-0.46506, -0.25586]$$

Second training set:

$$a_1 = [1, 0, 1]$$

$$a_2 = g(0.0997 \times 1 + 0.098 \times 1) = g(0.1977) = 0.54926$$

$$a_3 = g(0.08845 \times 1 + 0.0936 \times 0.549) = g(0.13988) = 0.534$$

$$\delta_3 = a_3 - y = 0.534 - 0 = 0.534$$

$$\delta_2 = \theta^T \times \delta_3 \cdot g'(z_2)$$

$$\delta_2 = 0.0124$$

$$\Delta^{21} = a_1 \delta_2 = [0.0124, 0, 0.0124]$$

$$\Delta^{22} = a_2 \delta_3 = [0.534, 0.2938]$$

Combining both Deltas from both training set:

$$\Delta^1 = \Delta^{11} + \Delta^{21} = [0.00216307, -0.01077, 0.0124]$$

$$\Delta^2 = \Delta^{12} + \Delta^{22} = [0.06985, 0.0379]$$

$$D_1 = 0.5 \times \Delta^1 = [0.000815, -0.00538, 0.0062]$$

$$D_2 = 0.5 \times \Delta^2 = [0.0349, 0.0189]$$

Update to the weight after first epoch:

$$\theta_1 = \theta_1 - 0.3[0.000815, -0.00538, 0.0062] + 0.9[0.001, -0.00565, 0.00665] = [0.10035, 0.0982, 0.1021]$$

$$\theta_2 = \theta_2 - 0.3[0.0349, 0.0189] + 0.9[0.0335, 0.021] = [0.11262, 0.107]$$

Theta after first epoch:

$$\theta = [0.1016, 0.098, 0.099, 0.093, 0.884]$$

Theta after second epoch:

$$\theta = [0.0982, 0.1021, 0.10035, 0.107, 0.11262]$$

3 Problem 3 (Text Classification Problem)

Now let's see the head-to-head performance comparison(the values here are all out of 1) between Naive Bayes and SVM with cosine similarity kernel:

(Note that for Naive Bayes, I used CountVectorizer combined with TF-IDF feature vectors, lowercased all terms and removed stop words, used log-scaled term counts for TF and inversed the document frequency over the training data only):

| CLASSIFICATION REPORT FOR NAIVE BAYES CLASSIFIER: | | |
|---|--------|--------|
| Metric | Train | Test |
| Accuracy | 0.959 | 0.819 |
| Precision | 0.963 | 0.842 |
| Recall | 0.950 | 0.804 |
| Training time | 4.714s | 4.714s |

| CLASSIFICATION REPORT FOR SVM CLASSIFIER WITH COSINE SIMILARITY KERNEL: | | |
|---|---------|---------|
| Metric | Train | Test |
| Accuracy | 0.996 | 0.846 |
| Precision | 0.996 | 0.849 |
| Recall | 0.996 | 0.839 |
| Training time | 15.662s | 15.662s |

Figure 3: ML showdown!

Analysis:

From the table I will say SVM is better than NB. Although it is true that SVM has a significantly longer training time compared to NB, the testing accuracy of SVM is higher than NB's.

4 Problem 4 (Neural Network + Challenge)

Here are the optimal parameters I got after running and tuning the Neural Network:

- (1) Training performance: 0.9836 (out of 1)
- (2) Regularization parameter: 0
- (3) Learning rate: 2
- (4) NumEpoch: 1500

Here is my visualization of the hidden layer with the specified number of epoch:

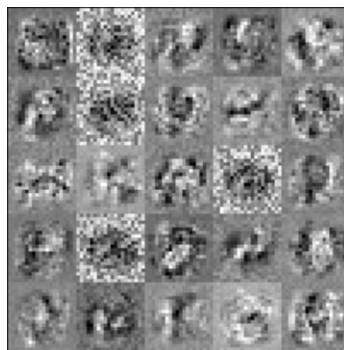


Figure 4: Hidden layer visualization