COMP IV PS6: Random Writer Dr. Rykalova

# **PS6: Random Writer**

# Global Sequence Alignment

### We will:

- Analyze an input text for transitions between k-grams (a fixed number of characters) and the following letter.
- Produce a probabilistic model of the text: given a particular k-gram series of letters, what letters follow at what probabilities?
- Use the model to generate nonsense text that's surprisingly reasonable.

### **Background**

In the 1948 landmark paper *A Mathematical Theory of Communication*, Claude Shannon founded the field of information theory and revolutionized the telecommunications industry, laying the groundwork for today's Information Age. In this paper, Shannon proposed using a Markov chain to create a statistical model of the sequences of letters in a piece of English text. Markov chains are now widely used in speech recognition, handwriting recognition, information retrieval, data compression, and spam filtering. They also have many scientific computing applications including the GeneMark algorithm for gene prediction, the Metropolis algorithm for measuring thermodynamical properties, and Google's PageRank algorithm for Web search. For this assignment, we consider a whimsical variant: generating stylized pseudorandom text.

### Markov model of natural language

Claude Shannon proposed a brute-force scheme to generate text according to a Markov model of **order 1**:

"To construct [a Markov model of order 1], for example, one opens a book at random and selects a letter at random on the page. This letter is recorded. The book is then opened to another page and one reads until this letter is encountered. The succeeding letter is then recorded. Turning to another page this second letter is searched for and the succeeding letter recorded, etc. It would be interesting if further approximations could be constructed, but the labor involved becomes enormous at the next stage."

Shannon approximated the statistical structure of a piece of text using a simple mathematical model known as a *Markov model*. A Markov model of *order* 0 predicts that each letter in the alphabet occurs with a fixed probability. We can fit a Markov model of order 0 to a specific piece of text by counting the number of occurrences of each letter in that text, and using these frequencies as probabilities. For example, if the input text is "gagggagagagagagagagaaa", the Markov model of order 0 predicts that each letter is 'a' with probability 7/17, 'c' with probability 1/17, and 'g' with probability 9/17 because these are the fraction of times each letter occurs. The following sequence of characters is a typical example generated from this model:

#### qaqqcqaqaaqaaqaaqaqaqaaqaqaaq...

A Markov model of order 0 assumes that each letter is chosen independently. This independence does not coincide with statistical properties of English text because there a high correlation among successive characters in a word or sentence. For example, 'w' is more likely to be followed with 'e' than with 'u', while 'g' is more likely to be followed with 'u' than with 'e'.

#### Order-k

An order-k Markov model uses strings of k-letters to predict text, these are called k-grams. An order-2 Markov model uses two-character strings or bigrams to calculate probabilities in generating random letters. For example, suppose that in the text we're using for generating random letters using an order-2 Markov model the bigram "th" is followed 50 times by the letter 'e', 20 times by the letter 'a', and 30 times by the letter 'o', because the sequences "the", "tha" and "tho" occur 50, 20, and 30 times, respectively while there are no other occurrences of "th" in the text we're modeling.

Now suppose that in generating random text we generate the bigram "th" and based on this we must generate the next random character using the order-2 model. The next letter will be an 'e' with a probability of 0.5 (50/100); will be an 'a' with probability 0.2 (20/100); and will be an 'o' with probability 0.3 (30/100). If 'e' is chosen, then the next bigram used to calculate random letters will be "he" since the last part of the old bigram is combined with the new letter to create the next bigram used in the Markov process.

#### more examples

Imagine taking a book (say, *Tom Sawyer*) and determining the probability with which each character occurs. You'd probably find that spaces are the most common, that the character 'e' is fairly common, and that the character 'q' is rather uncommon. After completing this 0 analysis, you'd be able to produce random *Tom Sawyer* text based on character probabilities. It wouldn't have much in common with the real thing, but at least the characters would tend to occur in the proper proportion. In fact, here's an example of what you might produce:

Order 0 rla bsht eS ststofo hhfosdsdewno oe wee h .mr ae irii ela iad o r te u t mnyto onmalysnce, ifu en c fDwn oee iteo

Now imagine doing a slightly more sophisticated order 1 analysis by determining the probability with which each character follows every other character. You would probably discover that 'h' follows 't' more frequently than 'x' does, and you would probably discover that a space follows '.' more frequently that ',' does. You could now produce some randomly generated *Tom Sawyer* by picking a character to begin with and then always choosing the next character based on the previous one and the probabilities revealed by the analysis. Here's an example:

Order 1 "Shand tucthiney m?" le ollds mind Theybooure He, he s whit Pereg lenigabo Jodind alllld ashanthe ainofevids tre lin--p asto oun theanthadomoere

Now imagine doing an order k analysis by determining the probability with which each character follows every possible sequence of characters of length k. An order 5 analysis of  $Tom\ Sawyer$  for example, would reveal that 'r' follows "Sawye" more frequently than any other character. After an order k analysis, you'd be able to produce random  $Tom\ Sawyer$  by always choosing the next character based on the previous k characters (the seed) and the probabilities revealed by the analysis.

At only a moderate order of analysis (say, orders 5--7), the randomly generated text begins to take on many of the characteristics of the source text. It probably won't make complete sense, but you'll be able to tell that it was derived from *Tom Sawyer* as opposed to, say, *The Sound and the Fury*. Here are some more examples:

- Order 2 "Yess been." for gothin, Tome oso; ing, in to weliss of an'te cle -- armit. Papper a comeasione, and smomenty, fropeck hinticer, sid, a was Tom, be suck tied. He sis tred a youck to themen
- Order 4 en themself, Mr. Welshman, but him awoke, the balmy shore. I'll give him that he couple overy because in the slated snufflindeed structure's kind was rath. She said that the wound the door a fever eyes that WITH him.
- Order 6 people had eaten, leaving. Come -- didn't stand it better judgment; His hands and bury it again, tramped herself! She'd never would be. He found her spite of anything the one was a prime feature sunset, and hit upon that of the forever.
- Order 8 look-a-here -- I told you before, Joe. I've heard a pin drop. The stillness was complete, however, this is awful crime, beyond the village was sufficient. He would be a good enough to get that night, Tom and Becky.

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Order 10 you understanding that they don't come around in the cave should get the word "beauteous" was over-fondled, and that together" and decided that he might as we used to do -- it's nobby fun. I'll learn you."

# **Overview of Assignment**

Your task is to write a program to automate this laborious task in a more efficient way — Shannon's brute-force approach is prohibitively slow when the size of the input text is large.

### **Implementation**

Begin by implementing the following class:

```
class RandWriter
  // Note: all of the below constructors/methods should be public.
  // -----
  // create a Markov model of order k from given text
RandWriter(string text, int k) // Assume that text has length at least k.
  // -----
int orderK() const
                // order k of Markov model
  // -----
  // number of occurrences of kgram in text
int freq(string kgram) const // throw an exception if kgram is not of
length k
  // -----
  // number of times that character c follows kgram
  // if order=0, return num of times char c appears
  // (throw an exception if kgram is not of length k)
int freq(string kgram, char c) const
  // -----
  // random character following given kgram
  // (Throw an exception if kgram is not of length k.
  // Throw an exception if no such kgram.)
char kRand (string kgram)
  // -----
  // generate a string of length L characters
  // by simulating a trajectory through the corresponding
  // Markov chain. The first k characters of the newly
  // generated string should be the argument kgram.
  // Throw an exception if kgram is not of length k.
  // Assume that L is at least k.
string generate(string kgram, int L)
  // -----
     // overload the stream insertion operator and display
     // the internal state of the Markov Model. Print out
     // the order, the alphabet, and the frequencies of
     // the k-grams and k+1-grams.
```

- Constructor. To implement the data type, create a symbol table, whose keys will be String k-grams. You may assume that the input text is a sequence of characters over the ASCII alphabet char so that all values are between 0 and 127. The value type of your symbol table needs to be a data structure that can represent the frequency of each possible next character. The frequencies should be tallied as if the text were circular (i.e., as if it repeated the first k characters at the end).
- Order. orderK() returns the order k of the Markov Model.
- **Frequency**. There are two frequency methods.
  - o freg (kgram) returns the number of times the k-gram was found in the original text.
  - o freq (kgram, c) returns the number of times the *k*-gram was followed by the character c in the original text.
  - o For either frequency method, when the k-gram is not found, return 0.
- Randomly generate a character. Return a character. It must be a character that followed the k-gram in the original text. The character should be chosen randomly, but the results of calling kRand(kgram) several times should mirror the frequencies of characters that followed the k-gram in the original text.
- Generate pseudo-random text. Return a String of length L that is a randomly generated stream of characters whose first k characters are the argument kgram. Starting with the argument kgram, repeatedly call kRand() to generate the next character. Successive k-grams should be formed by using the most recent k characters in the newly generated text.

To avoid dead ends, treat the input text as a **circular** string: the last character is considered to precede the first character.

#### Additional notes

Consider the behavior of a 0-order model. This model will generate new characters with a distribution proportional to the ratio they appear in the input text. This model is context-free; it does not use an input kgram (representing the current state of the model) when generating a new character. As such:

- The freq(string kgram) method takes an empty string as its input kgram (length of kgram must equal the order of the model).
- This method call should produce as a result the length of the original input text (given in the constructor).
- The freq(string kgram, char c) also will take a null string as input. It should produce as output the number of times the character c appears in the original input text.

Consider using a C++ map (<a href="http://www.cplusplus.com/reference/map/map/">http://www.cplusplus.com/reference/map/map/</a>) to store frequency counts of each kgram and "k+1"-gram as it's encountered when you traverse the string in the constructor.

Make sure to wrap around the end of the string during traversal, as described above.

At construction time, it is highly recommended to build up a string that represents the active alphabet and store it as a private class member variable. This will be useful when implementing the  $k\_Rand$  method, so that you can produce all of the k+1-grams that will follow the provided  $k\_gram$ , test for the frequency of each k+1-gram, and then produce output characters with proportional frequencies.

Overload stream insertion operator to display internal state of Markov model: See these sample instructions for how to do the overload. You should print out all of the k-gram and k+1-gram frequencies, the order of the model, and its alphabet. See attached file for sample instructions for how to build an iterator over the map of k-gram and k+1-gram keys.

#### **Text Generator**

Write a client program **TextWriter** that takes two command-line integers **k** and **L**, reads the input text from standard input and builds a Markov model of order **k** from the input text; then, starting with

the k-gram consisting of the **first** k **characters of the input text**, prints out L characters generated by simulating a trajectory through the corresponding Markov chain. You may assume that the text has length at least k, and also that  $L \ge k$ .

```
./TextWriter 2 11 < input17.txt
```

### **Debugging and testing**

- You should write a test.cpp file that uses the Boost functions

  BOOST\_REQUIRE\_THROW and BOOST\_REQUIRE\_NO\_THROW to verify that your code properly throws the specified exceptions when appropriate (and does not throw an exception when it shouldn't). As usual, use BOOST\_REQUIRE to exercise all methods of the class.
- Make sure you throw std::runtime error's in the methods per the spec.
- Your test file must exercise all methods of your RandWriter class.

### **Additional Files**

Produce and turn in a Makefile which must build an executable named TextWriter.

Turn in a ps6-readme.txt file that explains what you have done.

## **Submit your work**

You should be submitting at least five files:

- 1. RandWriter.cpp
- 2. RandWriter.h
- 3. test.cpp
- 4. Makefile
- 5. TextWriter.cpp
- 6. ps6 readme.txt

Submit the archive on Blackboard.

# **Grading rubric**

Feature	Value	Comment
RandWriter	4	full & correct implementation = 4 pts; nearly complete = 3pts;
implementation		part way=2 pts; started=1 pt
TextWriter	2	full & correct implementation = 2 pts; part way =1 pt; not =0 pt
implementation		
Makefile	1	Makefile included
your own test.cpp	4	should test ALL Functions in RandWriter
cpplint	1	Your source files pass the style checks implemented in cpplint
Lambda expression	2	Must pass a lambda as an argument and document in readme
Exceptions	2	full & correct implementation=2 pts; part way=1 pt; not=0 pt
implementation		
readme	2	Readme should say something meaningful about what you
		accomplished
		1 point for explaining how you tested your implementation
		1 point for explaining the exceptions you implemented
Total	18	
	3	Write a new random-text generation program WordWriter based
		on words rather than character