

Example 12

Graph Sketch

Sketch a possible graph of a function f that satisfies the following

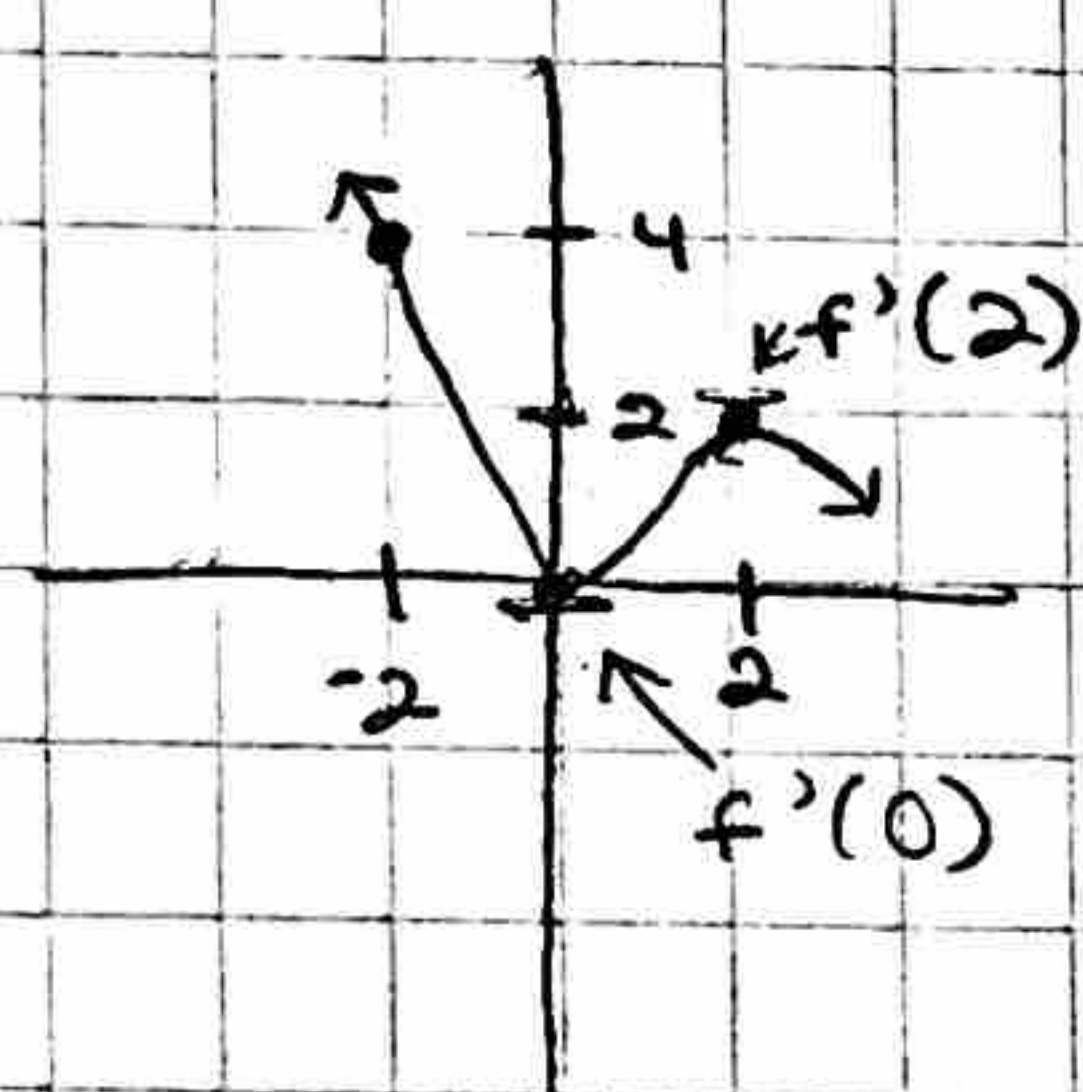
Condition 1

$$f(-2) = 4$$

$$f(0) = 0$$

$$f(2) = 2$$

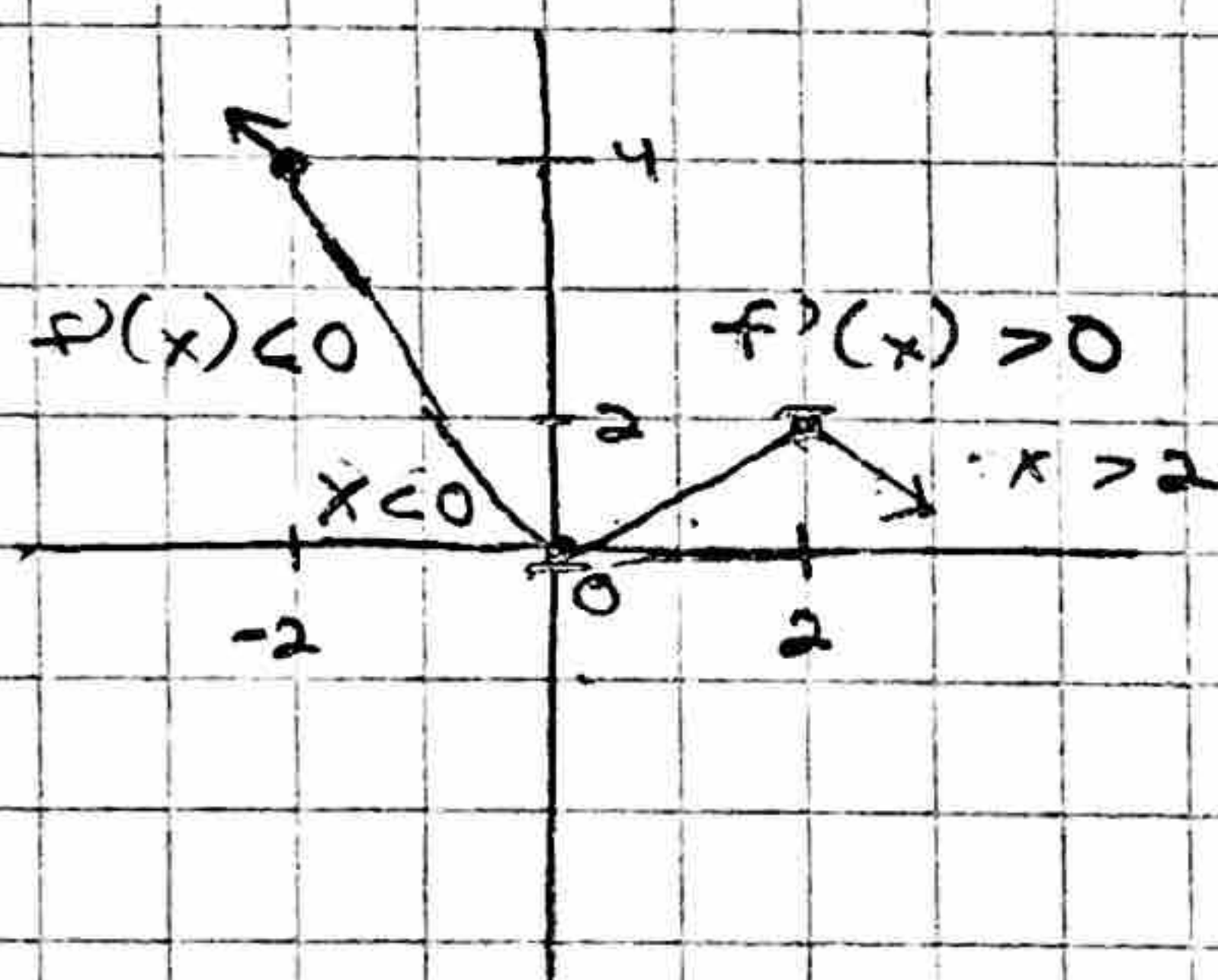
$$f'(0) = f'(2) = 0$$



Condition 2

$$f'(x) > 0 \quad \text{for} \quad 0 < x < 2$$

$$f'(x) < 0 \quad \text{for} \quad x < 0 \text{ and } x > 2$$



Where $f'(x) > 0$ for $0 < x < 2$, f is increasing on $(0, 2)$

Where $f'(x) < 0$ for $x < 0$ and $x > 2$, f is decreasing on $(-\infty, 0) \cup (2, \infty)$

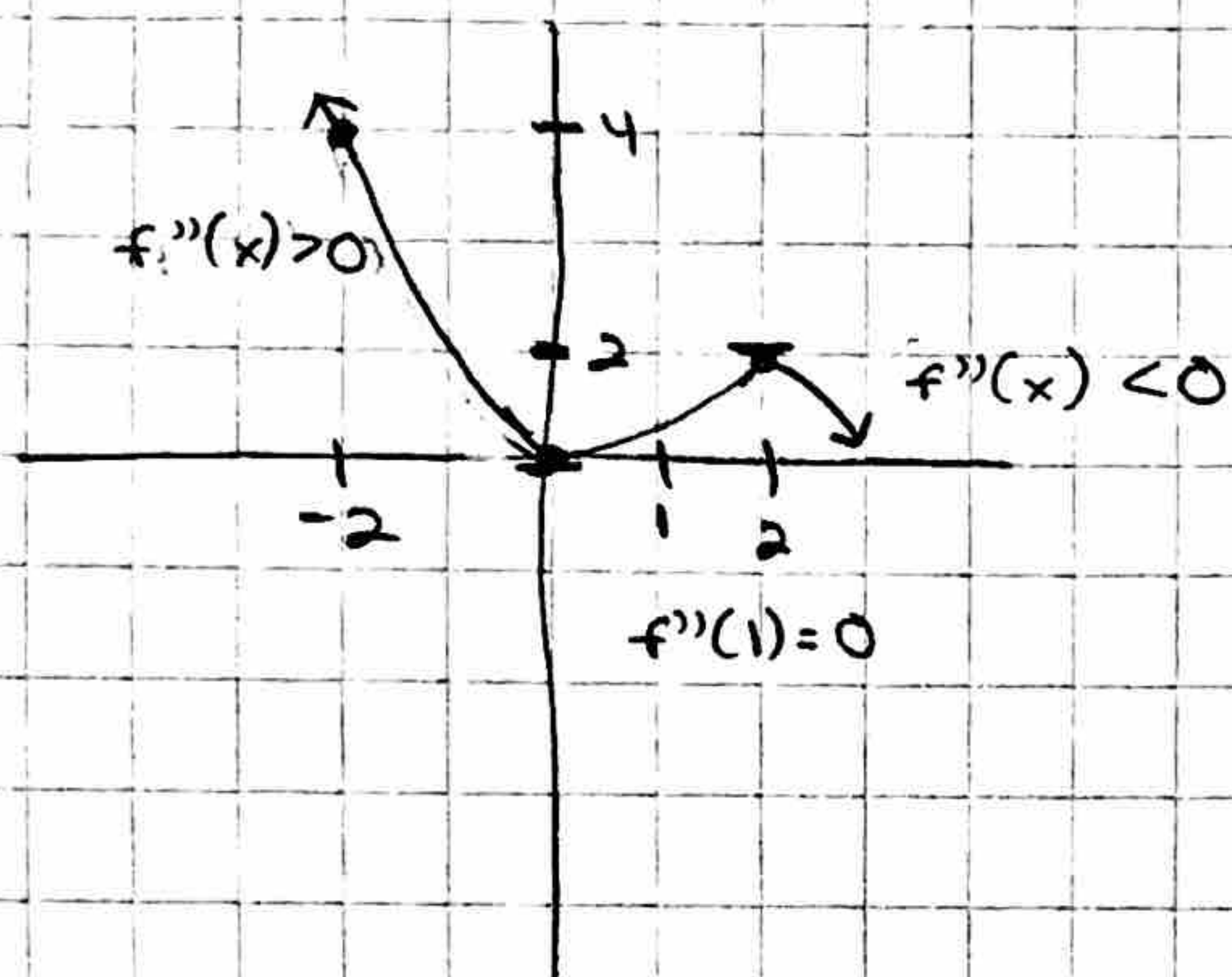
Condition 3

$$f''(x) > 0 \text{ for } x < 1$$

$$f''(x) < 0 \text{ for } x > 1$$

$$f''(1) = 0$$

③ Determine Concavity



Where $f''(x) > 0$ for $x < 1$, f concaves upward

Where $f''(x) < 0$ for $x > 1$, f concaves downward

Where $f''(1) = 0$, $x = 1$ is an inflection point