

$$E = \epsilon \quad 1. \quad \lim_{x \rightarrow 3} 2x + 1 = 7$$

$$\frac{7-E}{-1} < 2x+1 < \frac{7+E}{-1}$$

$$\frac{6-E}{2} < \frac{2x}{2} < \frac{6+E}{2}$$

$$\frac{6-E}{2} < x < \frac{6+E}{2}$$

$$3 - \frac{E}{2} < x < 3 + \frac{E}{2}$$

$$E = 1$$

$$3 - \frac{1}{2} < x < 3 + \frac{1}{2}$$

"

$$2.5 < x < 3.5$$

If  $x$  is within 0.5 units of 3

$$E = 0.6$$

$$3 - \frac{0.6}{2} < x < 3 + \frac{0.6}{2}$$

"

$$2.7 < x < 3.3$$

If  $x$  is within 0.3 of units of 3

$$E = 0.04$$

$$3 - \frac{0.04}{2} < x < 3 + \frac{0.04}{2}$$

"

$$2.98 < x < 3.02$$

If  $x$  is within 0.02 units of 3



$$\lim_{x \rightarrow 3} 2x - 1 = 5$$

$$5 - 1 = 4$$

$$5 + 1 = 6$$

$$[4, 6]$$

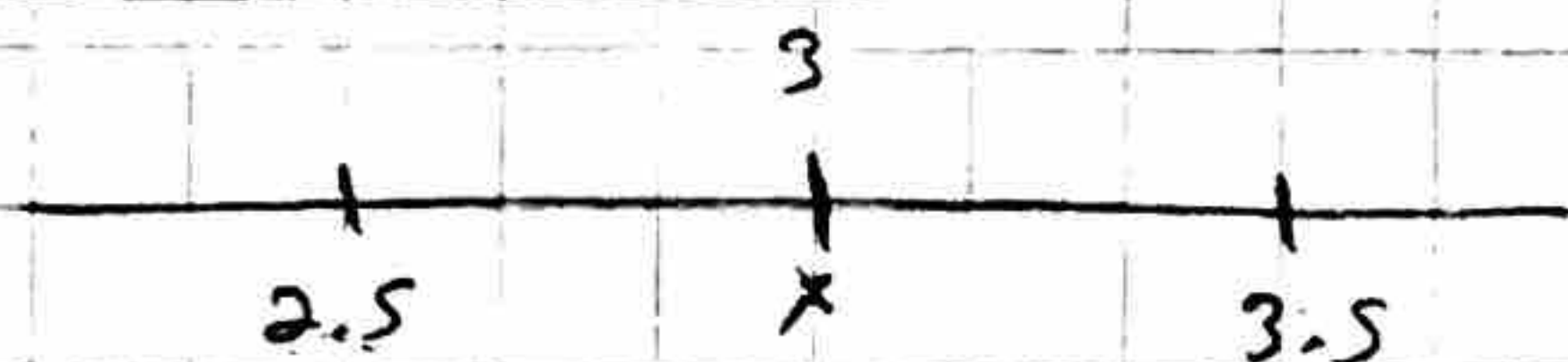
$$4 < 2x - 1 < 6$$

$$+1 \quad +1 \quad +1$$

$$\frac{5}{2} < \frac{2x}{2} < \frac{7}{2}$$

"

$$2.5 < x < 3.5$$



$$5 - \epsilon < 2x - 1 < 5 + \epsilon$$

$$+1 \quad +1 \quad +1$$

$$\frac{6 - \epsilon}{2} < \frac{2x}{2} < \frac{6 + \epsilon}{2}$$

"

$$\frac{6}{2} - \frac{\epsilon}{2}$$

$$\frac{6}{2} + \frac{\epsilon}{2}$$

"

$$3 - \frac{\epsilon}{2}$$

$$3 + \frac{\epsilon}{2}$$

"

$$\frac{3 - \epsilon}{2}$$

$$\frac{3 + \epsilon}{2}$$



$$\epsilon = \epsilon$$

$$3 - \frac{\epsilon}{2} < x < 3 + \frac{\epsilon}{2}$$

"

$$\frac{\left(3 + \frac{\epsilon}{2}\right) - \left(3 - \frac{\epsilon}{2}\right)}{2}$$



$$\frac{3 + \frac{\epsilon}{2} - 3 + \frac{\epsilon}{2}}{2}$$

$$\frac{3 - 3 + \frac{\epsilon}{2} + \frac{\epsilon}{2}}{2}$$

$$\frac{\frac{\epsilon}{2} + \frac{\epsilon}{2}}{2}$$

"

$$\frac{2\epsilon}{2}$$

"

$$\frac{2\epsilon}{2} \div \frac{2}{1}$$

"

$$\frac{2\epsilon}{2} \cdot \frac{1}{2}$$

"

$$\frac{\epsilon}{2}$$

$x$  is within  $\epsilon/2$  units of 3

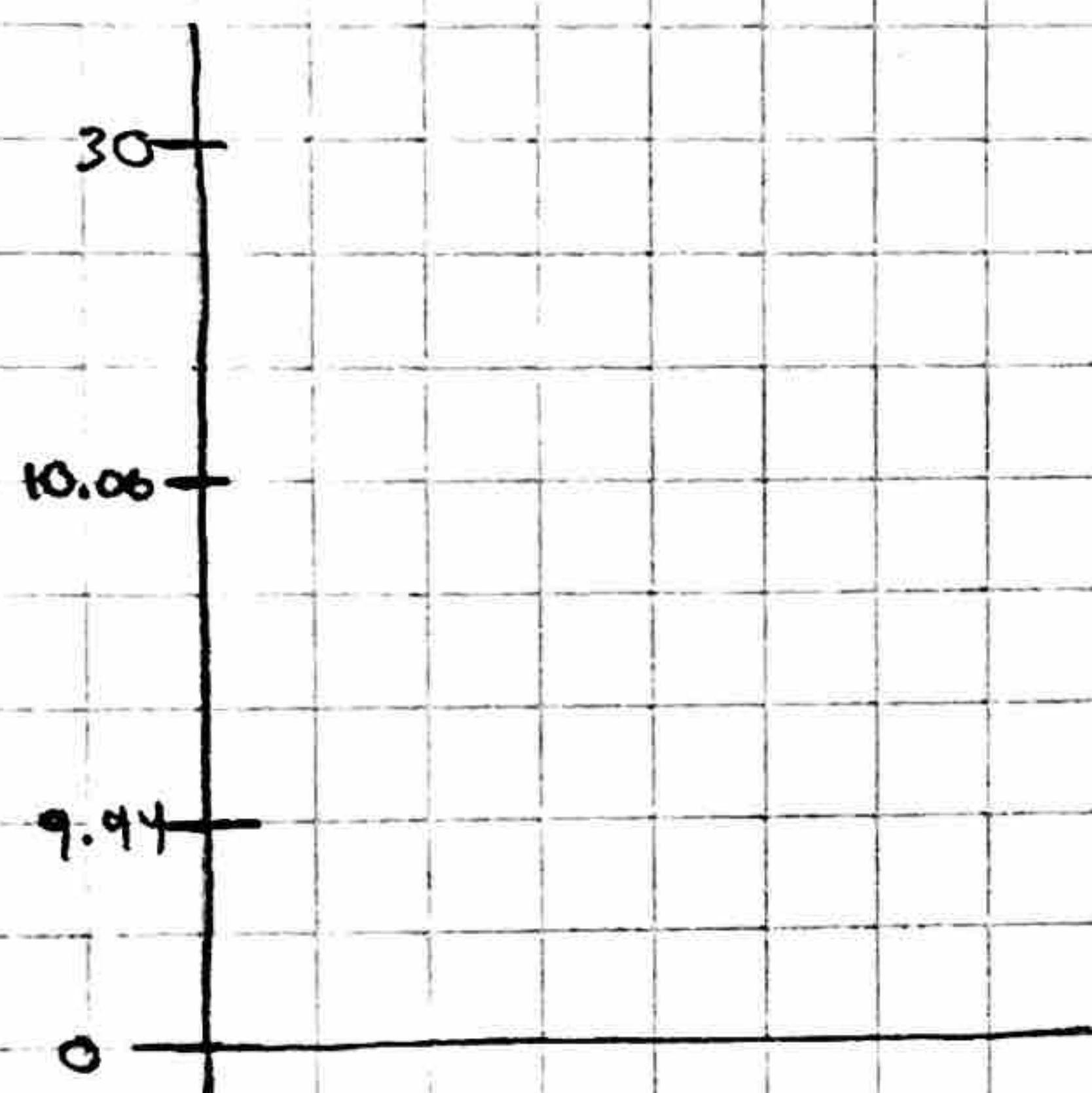


7.

$$f(x) = x + 1$$

$$\lim_{x \rightarrow ?} x + 1 = 10$$

$$x \rightarrow ?$$



within 0.06

$$10 + 0.06$$

$$10 - 0.06$$

$$10.06$$

$$9.94$$

$$10 - E < x + 1 < 10 + E$$

$$9 - E < x < 9 + E$$

$$9 - 0.06 < x < 9 + 0.06$$

$$8.94 < x < 9.06$$

$$x = 0.06$$

$$0.06 / 3$$

0.02 inches of the 10 inches of each bond



13.  $\lim_{x \rightarrow -1} x + 1 = 5$        $f(x) = x + 1$  or  $f(x) = x^2$

within 0.06 inches

$$\begin{array}{ccc} S - E & < & x + 1 < S + E \\ -1 & & -1 \quad -1 \end{array}$$

$$\hline 4 - E < x < 4 + E$$

$$4 - 0.06 < x < 4 + 0.06$$

$$3.94 < x < 4.06$$

$$x = 0.06$$

$$S + E$$

$$S - E$$

$$\sqrt{S - E} < \sqrt{x^2} < \sqrt{S + E}$$

$$\sqrt{S - E} < x < \sqrt{S + E}$$

$$2.22261 < x < 2.24944$$

$$x = .013415$$