- 1.  $\overline{AB} \cong \overline{DE}$ ,  $\overline{BC} \cong \overline{EF}$  and  $\overline{AC} \cong \overline{DF}$
- 14. HL
- 2.  $\overline{ST} \cong \overline{VW}$ ,  $\overline{TU} \cong \overline{WX}$  and  $\overline{SU} \cong \overline{VX}$
- Vertical angles are congruent, so we have AAS.

3. ∧CDE ≃ ∧HGF

If you have AAS, then you know that all three angles are congruent.

4.  $\Delta XYZ \cong \Delta LMN$ 

If all 3 angles are congruent, then we have ASA.

- 5.  $\angle A \cong \angle D$ ,  $\angle B \cong \angle E$  and  $\angle C \cong \angle F$
- 16. Not necessarily congruent.
- 6.  $\angle R \cong \angle X$ ,  $\angle S \cong \angle Y$  and  $\angle T \cong \angle Z$
- 17. ASA

7. SSS

18. Not necessarily congruent.

8. SAS

19. All the angles are congruent but the sides may not be congruent, thus these triangles are not congruent.

9. ASA

There is no AAA property for showing congruence.

10. SSS

Note: These triangles are similar because all the angles are equal.

11. Not necessarily congruent.

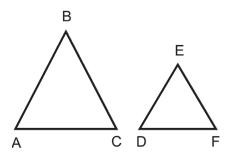
20. SAS

- 12. SAS or SSS
- 13. SAS

21. Prove Theorem 2.2.2: The ratio of the lengths of corresponding sides of two triangles are equal if and only of the triangles are similar.

Two proofs are needed to prove the "if and only if" statement.

Part 1: Show If the two triangles are similar, then the ratio of the lengths of corresponding sides of two triangles are equal.



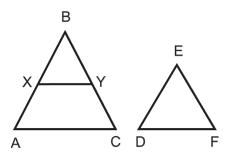
Given:  $\triangle ABC \sim \triangle DEF$ 

Prove:  $\frac{DE}{AB} = \frac{EF}{BC} = \frac{DF}{AC}$ 

Statement	Reason
1. $\triangle ABC \sim \triangle DEF$	1. Given.
2. $\frac{DE}{AB} = \frac{EF}{BC} = \frac{DF}{AC}$	2. Definition of similar triangle.

Part 2: Show if the ratio of the lengths of corresponding sides of two triangles are equal, then the triangles are similar.

## 21. Continued:



Given: 
$$\frac{DE}{AB} = \frac{EF}{BC} = \frac{DF}{AC}$$

Prove:  $\triangle ABC \sim \triangle DEF$ 

Statement	Reason
1. $\frac{DE}{AB} = \frac{EF}{BC} = \frac{DF}{AC}$	1. Given.
2. Locate x on $\overline{AB}$ so that $\overline{XB} \cong \overline{DE}$ .	2. Definition of congruent line segments.
3. Draw $\overline{XY}$ so that $\overline{XY} \parallel \overline{AC}$ .	3. Postulate 1.6.2: Given a line and a point not on the line, there is exactly one line through the point that is parallel to the given line.
4. ∠BXY ≅ ∠A & ∠BYX ≅ ∠C	4. Postulate 1.6.1: If two parallel lines are cut by a transversal, then the corresponding angles are congruent.
5. $\triangle ABC \sim \triangle XBY$	5. AA similarity.
6. $\frac{XB}{AB} = \frac{BY}{BC} = \frac{XY}{AC}$	6. Definition of similar triangles.
7. XB = DE	7. From line 2.
$8. \ \frac{XB}{AB} = \frac{EF}{BC} = \frac{DF}{AC}$	8. Substitution from lines 1 and 7.
9. $\frac{EF}{BC} = \frac{BY}{BC}$ & $\frac{DF}{AC} = \frac{XY}{AC}$	9. Substitution from lines 6 and 8.
10. EF = BY & DF = XY	10. Multiplication.
11. $\overline{EF} \cong \overline{BY} \& \overline{DF} \cong \overline{XY}$	11. Definition of congruent line segments.

## 21. Continued:

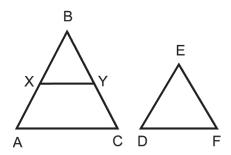
12. $\overline{XB} \cong \overline{DE}$	12. From line 2.
13. ΔXBY ≅ ΔDEF	13. SSS
14. ∠B ≅ ∠E & ∠BXY ≅ ∠D	14. CPCTC
15. ∠BXY ≅ ∠A & ∠BXY ≅ ∠D	15. Lines 4 and 14.
16. ∠A ≅ ∠D	15. Substitution from line 15.
17. $\triangle ABC \sim \triangle DEF$	16. AA similarity.

22. Prove Theorem 2.2.3: If two ratios of the lengths of corresponding sides of two triangles are equal and the included angles are congruent, then the triangles are similar.

Given:  $\frac{DE}{AB} = \frac{EF}{BC}$ 

 $\angle B \cong \angle E$ 

Prove:  $\triangle ABC \sim \triangle DEF$ 



## 22. Continued:

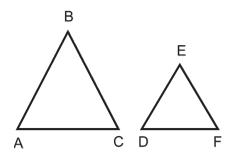
Statement	Reason
<sub>1</sub> DE _ EF	1. Given.
1. $\frac{BE}{AB} = \frac{EE}{BC}$	
2. Locate X on $\overline{AB}$ so that $\overline{XB} \cong \overline{DE}$	2. Definition of congruent line segments.
3. Draw XY so that XY    AC	3. Postulate 1.6.2: Given a line and a point
	not on the line, there is exactly one line through the point that is parallel to the given line.
4. ∠BXY ≅ ∠A & ∠BYX ≅ ∠C	4. Postulate 1.6.1: If two parallel lines are
	cut by a transversal, then the corresponding
	angles are congruent.
5. $\triangle ABC \sim \triangle XBY$	5. AA similarity.
6. $\frac{XB}{B} = \frac{BY}{BY} = \frac{XY}{BY}$	6. Definition of similar triangles.
6. $\frac{XB}{AB} = \frac{BY}{BC} = \frac{XY}{AC}$	
7. XB = DE	7. From line 2.
, XB EF	8. Substitution from lines 1 and 7.
8. $\frac{XB}{AB} = \frac{EF}{BC}$	
e EF BY	9. Substitution from lines 6 and 8.
9. $\frac{BC}{BC} = \frac{BC}{BC}$	

10. EF = BY	10. Multiplication.
11. EF ≅ BY	11. Definition of congruent line segments.
12. $\overline{XB} \cong \overline{DE}$	12. From line 2.
13. ∠B ≅ ∠E	13. Given.
14. ΔXBY ≅ ΔDEF	14. SAS
15. ∠BXY ≅ ∠D	15. CPCTC
16. ∠A ≅ ∠D	16. Transitive from lines 4 and 15.
17. $\triangle ABC \sim \triangle DEF$	17. AA similarity.

23. Prove Theorem 2.2.1: Two triangles are similar if and only if their corresponding angles are congruent.

Two proofs are needed to prove the "if and only if" statement.

Part 1: Show if two triangles are similar, then their corresponding angles are congruent.



Given:  $\triangle ABC \sim \triangle DEF$ 

Prove;  $\angle A \cong \angle D$ ,  $\angle B \cong \angle E$  and  $\angle C \cong \angle F$ 

Statement	Reason
1. $\triangle ABC \sim \triangle DEF$	1. Given.
2. $\angle A \cong \angle D$ , $\angle B \cong \angle E$ and $\angle C \cong \angle F$	2. Definition of similar triangles.

Part 2: Show if two triangles have corresponding congruent angles, then the triangles are similar.

Given:  $\angle A \cong \angle D$ ,  $\angle B \cong \angle E$  and  $\angle C \cong \angle F$ 

Prove:  $\triangle ABC \sim \triangle DEF$ 

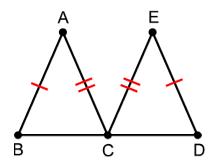
Statement	Reason
1. $\angle A \cong \angle D$ , $\angle B \cong \angle E$ and $\angle C \cong \angle F$	1. Given.
2. $\triangle ABC \sim \triangle DEF$	2. Postulate 2.2.1: If two angles of a triangle are congruent to two angles of another triangle, then the triangles are similar.

Given:  $\overline{AB} \cong \overline{ED}$ 

 $\overline{AC}\cong\overline{EC}$ 

C is the midpoint of  $\overline{\mbox{BD}}$ 

Prove:  $\triangle ABC \cong \triangle EDC$ 



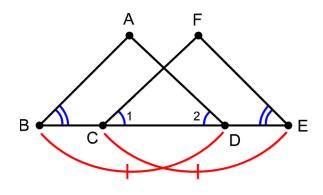
Statement	Reason
1. $\overline{AB} \cong \overline{ED}$	1. Given.
$\overline{AC}\cong\overline{EC}$	
2. C is the midpoint of BD	2. Given.
3. BC ≅ DC	3. Definition of midpoint.
4. $\triangle ABC \cong \triangle EDC$	4. SSS

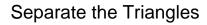
Given:  $\angle B \cong \angle E$ 

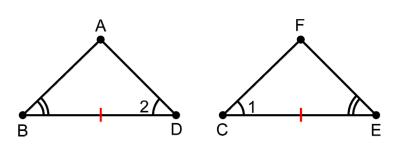
∠1 ≅ ∠2

 $\overline{\mathsf{BD}} \cong \overline{\mathsf{CE}}$ 

Prove:  $\triangle ABD \cong \triangle FEC$ 







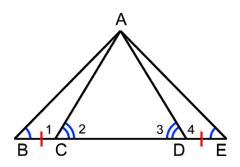
Statement	Reason
1. ∠B ≅ ∠E	1. Given. (A) & (A)
<b>∠1</b> ≅ <b>∠2</b>	
2. BD ≅ CE	2. Given. (S)
3. $\triangle ABD \cong \triangle FEC$	3. ASA

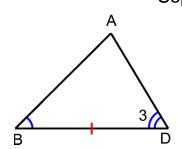
Given:  $\angle B \cong \angle E$ 

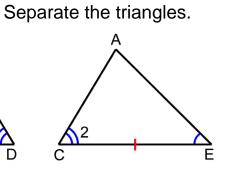
 $\angle 2\cong \angle 3$ 

 $\overline{BC}\cong\overline{DE}$ 

Prove:  $\triangle ABD \cong \triangle AEC$ 





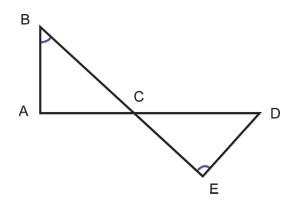


Statements	Reasons
1. ∠B ≅ ∠E	1. Given
∠2 ≅ ∠3	
2. BC ≅ DE	2. Given
3. $\overline{CD} \cong \overline{CD}$	3. Reflexive
4. $\overline{BC} + \overline{CD} \cong \overline{DE} + \overline{CD}$	4. Additive Property
5. $\overline{BC} + \overline{CD} = \overline{BD}$	5. Definition of segment addition
$\overline{DE} + \overline{CD} = \overline{EC}$	
6. BD ≅ EC	6. Substitution from lines 4 and 5.
7. $\triangle ABD \cong \triangle AEC$	7. ASA

Given: C is the midpoint of  $\overline{BE}$  $\angle B \cong \angle E$ 

$$\angle B \cong \angle E$$

Prove:  $\triangle BCA \cong \triangle ECD$ 

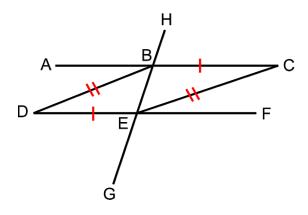


Statement	Reason
1. C is the midpoint of BE.	1. Given.
2. BC ≅ CE	2. Definition of midpoint. (S)
3. ∠ACB & ∠ECD are vertical angles.	3. Definition of vertical angles.
4. ∠ACB ≅ ∠ECD	4. Theorem 1.2.1: If two angles are vertical angles, then they are congruent.  (A)
5. ∠B ≅ ∠E	5. Given. (A)
6. ΔBCA ≅ ΔECD	6. ASA

Given:  $\overline{DE} \cong \overline{BC}$ 

 $\overline{\mathsf{DB}}\cong\overline{\mathsf{CE}}$ 

Prove:  $\overline{AC} \parallel \overline{DF}$ 

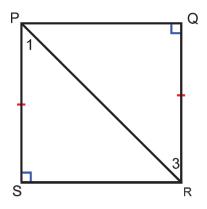


Statement	Reason
1. DE ≅ BC	1. Given.
$\overline{DB}\cong\overline{CE}$	
2. BE ≅ BE	2. Reflexive.
3. ΔBED ≅ ΔEBC	3. SSS
4. ∠BED ≅ ∠EBC	4. CPCTC
5. AC    DF	5. Theorem 1.6.4: If two lines are cut by a transversal and a pair of alternate interior angles are congruent, then the two lines are parallel.

Given:  $\angle Q$  and  $\angle S$  are right angles

 $\overline{\mathsf{RQ}} \cong \overline{\mathsf{SP}}$ 

Prove:  $\overline{PQ} \parallel \overline{SR}$ 



Statement	Reason
<ol> <li>∠Q and ∠S are right angles</li> </ol>	1. Given. (right triangle)
2. RQ ≅ SP	2. Given. (L)
3. PR ≅ PR	3. Reflexive. (H)
4. ΔSPR ≅ ΔQRP	4. HL
5. ∠1 ≅ ∠3	5. CPCTC
6. PQ    SR	6. Theorem 1.6.4: If two lines are cut by a transversal and a pair of alternate interior angles are congruent, then the two lines are parallel.