

$$\begin{aligned}
 1. \quad & (2)^3 \\
 & \textcolor{blue}{(2)}\textcolor{blue}{(2)}(2) \\
 & \textcolor{blue}{(4)}(2) \\
 & \textcolor{red}{8}
 \end{aligned}$$

$$\begin{aligned}
 3. \quad & (-3)^3 \\
 & \textcolor{blue}{(-3)}\textcolor{blue}{(-3)}(-3) \\
 & \textcolor{blue}{(9)}(-3) \\
 & \textcolor{red}{-27}
 \end{aligned}$$

$$\begin{aligned}
 5. \quad & -3^3 \\
 & -\textcolor{blue}{(3)}\textcolor{blue}{(3)}(3) \\
 & -\textcolor{blue}{(9)}(3) \\
 & -(27) \\
 & \textcolor{red}{-27}
 \end{aligned}$$

$$\begin{aligned}
 7. \quad & (-2)^3 \\
 & \textcolor{blue}{(-2)}\textcolor{blue}{(-2)}(-2) \\
 & \textcolor{blue}{(4)}(-2) \\
 & \textcolor{red}{(-8)}
 \end{aligned}$$

$$\begin{aligned}
 9. \quad & (-5)^3 \\
 & \textcolor{blue}{(-5)}\textcolor{blue}{(-5)}(-5) \\
 & \textcolor{blue}{(25)}(-5) \\
 & \textcolor{red}{-125}
 \end{aligned}$$

$$\begin{aligned}
 11. \quad & (-2)^0 \\
 & \text{Anything to the power of zero equals 1.} \\
 & \textcolor{red}{1}
 \end{aligned}$$

$$\begin{aligned}
 13. \quad & (-4)^2 \\
 & (-4)(-4) \\
 & \textcolor{red}{16}
 \end{aligned}$$

$$\begin{aligned}
 15. \quad & (-5)^2 \\
 & (-5)(-5) \\
 & \textcolor{red}{25}
 \end{aligned}$$

$$\begin{aligned}
 17. \quad & (-8)^2 \\
 & (-8)(-8) \\
 & \textcolor{red}{64}
 \end{aligned}$$

$$\begin{aligned}
 19. \quad & -4^0 \\
 & \text{Anything to the power of zero is 1.} \\
 & \text{Since the power is only on the 4, the} \\
 & \text{answer is -1.} \\
 & -(4^0) \\
 & -(1) \\
 & \textcolor{red}{-1}
 \end{aligned}$$

$$\begin{aligned}
 21. \quad & -2^2 \\
 & -(2)(2) \\
 & -(4) \\
 & \textcolor{red}{-4}
 \end{aligned}$$

$$\begin{aligned}
 23. \quad & (-3)^4 \\
 & \textcolor{blue}{(-3)}\textcolor{blue}{(-3)}(-3)(-3) \\
 & \textcolor{blue}{(9)}(-3)(-3) \\
 & \textcolor{magenta}{(9)}\textcolor{magenta}{(-3)}(-3) \\
 & \textcolor{magenta}{(-27)}(-3) \\
 & \textcolor{red}{81}
 \end{aligned}$$

$$\begin{aligned}
 25. \quad & -2^3 \\
 & -\textcolor{blue}{(2)}\textcolor{blue}{(2)}(2) \\
 & -\textcolor{blue}{(4)}(2) \\
 & -(8) \\
 & \textcolor{red}{-8}
 \end{aligned}$$

$$\begin{aligned}
 27. \quad & (-2)^5 \\
 & (-2)(-2)(-2)(-2)(-2) \\
 & (4)(-2)(-2)(-2) \\
 & (4)(-2)(-2)(-2) \\
 & (-8)(-2)(-2) \\
 & (-8)(-2)(-2) \\
 & (16)(-2) \\
 & -32
 \end{aligned}$$

$$\begin{aligned}
 29. \quad & (a^8)(a^9) \\
 & a^8 \cdot a^9 \\
 & a^{8+9} \\
 & a^{17}
 \end{aligned}$$

$$\begin{aligned}
 31. \quad & (a^{12})(a^{10}) \\
 & a^{12} \cdot a^{10} \\
 & a^{12+10} \\
 & a^{22}
 \end{aligned}$$

$$\begin{aligned}
 33. \quad & (2z^8)(-2z^3) \\
 & (2)(z^8)(-2)(z^3) \\
 & (2)(-2)(z^8)(z^3) \\
 & -4 \cdot z^8 \cdot z^3 \\
 & -4 \cdot z^{8+3} \\
 & -4z^{11}
 \end{aligned}$$

$$\begin{aligned}
 35. \quad & (-6w^6)(-3w^7) \\
 & (-6)(-3)(w^6)(w^7) \\
 & 18 \cdot w^6 \cdot w^7 \\
 & 18 \cdot w^{6+7} \\
 & 18w^{13}
 \end{aligned}$$

$$\begin{aligned}
 37. \quad & (-5x^3)(4x^7) \\
 & (-5)(4)(x^3)(x^7) \\
 & -20 \cdot x^3 \cdot x^7 \\
 & -20 \cdot x^{3+7} \\
 & -20x^{10}
 \end{aligned}$$

$$\begin{aligned}
 39. \quad & (x^3)^2 \\
 & x^{3 \cdot 2} \\
 & x^6
 \end{aligned}$$

$$\begin{aligned}
 41. \quad & (-3x^2y^4)^2 \\
 & (-3x^2y^4)(-3x^2y^4) \\
 & 9 \cdot x^2 \cdot x^2 \cdot y^4 \cdot y^4 \\
 & 9 \cdot x^{2+2} \cdot y^{4+4} \\
 & 9x^4y^8
 \end{aligned}$$

$$\begin{aligned}
 43. \quad & (-5a^7b^6c^2)^3 \\
 & (-5a^7b^6c^2)(-5a^7b^6c^2)(-5a^7b^6c^2) \\
 & (-125)(a^7a^7a^7)(b^6b^6b^6)(c^2c^2c^2) \\
 & -125a^{7+7+7}b^{6+6+6}c^{2+2+2} \\
 & -125a^{21}b^{18}c^6
 \end{aligned}$$

$$\begin{aligned}
 45. \quad & (-2a^5b^2c^2)^4 \\
 & (-2)^4a^{5 \cdot 4}b^{2 \cdot 4}c^{2 \cdot 4} \\
 & 16a^{20}b^8c^8
 \end{aligned}$$

47.

$$\frac{3a^3b^{10}}{27a^5b^6}$$

$$\frac{3a^3b^6b^4}{27a^3a^2b^6}$$

$$\frac{b^4}{9a^2}$$

49.

$$\frac{12a^3b^{19}c^4d}{10a^5b^9c^2d^2}$$

$$\frac{12a^3b^9b^{10}c^2c^2d}{10a^3a^2b^9c^2dd}$$

$$\frac{6b^{10}c^2}{5a^2d}$$

51.

$$\frac{(-2c^5d^6)^4}{(-4c^2d^{10})^3}$$

$$\frac{(-2)^4c^{5 \cdot 4}d^{6 \cdot 4}}{(-4)^3c^{2 \cdot 3}d^{10 \cdot 3}}$$

$$\frac{16c^{20}d^{24}}{-64c^6d^{30}}$$

$$\frac{16c^6c^{14}d^{24}}{-64c^6d^{24}d^6}$$

$$\frac{c^{14}}{-4d^6}$$

53.

$$\frac{(x+y)^6}{(x+y)^6}$$

Anything (except zero)
divided by itself is 1.

1

55.

$$\frac{(7a^3)^4}{(7a^3)^6}$$

$$\frac{7^4a^{12}}{7^6a^{18}}$$

$$\frac{1}{7^2a^6}$$

$$\frac{1}{49a^6}$$

57.

$$\frac{32^2}{8^5}$$

$$\frac{32 \cdot 32}{8 \cdot 8 \cdot 8 \cdot 8 \cdot 8}$$

$$\frac{8 \cdot 4 \cdot 8 \cdot 4}{8 \cdot 8 \cdot 8 \cdot 2 \cdot 4 \cdot 2 \cdot 4}$$

$$\frac{1}{8 \cdot 2 \cdot 2}$$

$$\frac{1}{32}$$

61. $(a^2)^5$

$a^{2 \cdot 5}$

a^{10}

63. $(c^2)^4$

$c^{2 \cdot 4}$

c^8

65. $(m^7)^3$

$m^{7 \cdot 3}$

m^{21}

67. $(a^2b^3)^4$

$a^{2 \cdot 4}b^{3 \cdot 4}$

a^8b^{12}

69. $(b^7b^2)^3$

$(b^{7+2})^3$

$(b^9)^3$

$b^{9 \cdot 3}$

b^{27}

71. $(-2c^2b^6)^2$

$(-2)^2c^{2 \cdot 2}b^{6 \cdot 2}$

$4c^4b^{12}$

73. $(-4x^6y)^2$

$(-4)^2x^{6 \cdot 2}y^2$

$16x^{12}y^2$

75. $(-2x^2y^4)^5$

$(-2)^5x^{2 \cdot 5}y^{4 \cdot 5}$

$-32x^{10}y^{20}$

77. $(2x^4y^8)^5$

$(2)^5x^{4 \cdot 5}y^{8 \cdot 5}$

$32x^{20}y^{40}$

79. $-2(m^5n^4)^2$

$-2(m^{5 \cdot 2}n^{4 \cdot 2})$

$-2(m^{10}n^8)$

$-2m^{10}n^8$

81. $6(x^9y^{10})^3$

$6(x^{9 \cdot 3}y^{10 \cdot 3})$

$6(x^{27}y^{30})$

$6x^{27}y^{30}$

83. $3^0(a^6b^{14})^2$

$3^0(a^{6 \cdot 2}b^{14 \cdot 2})$

$3^0(a^{12}b^{28})$

$1(a^{12}b^{28})$

$a^{12}b^{28}$

85.

$$\frac{(-3p^3q^2)^3}{(-6p^4q^{10})^2}$$

$$\frac{(-3)^3 p^{3 \cdot 3} q^{2 \cdot 3}}{(-6)^2 p^{4 \cdot 2} q^{10 \cdot 2}}$$

$$\frac{-27p^9q^6}{36p^8q^{20}}$$

$$\frac{-3p}{4q^{14}}$$

87.

$$\frac{(y+z)^0}{(y+z)^2}$$

Anything to the power of zero is 1.

$$\frac{1}{(y+z)^2}$$

89.

$$\frac{-36a^{12}b^4}{9a^3b^9}$$

$$\frac{-4 \cdot 9a^9a^3b^4}{9a^3b^5b^4}$$

$$\frac{-4a^9}{b^5}$$

91.

$$\frac{(-3x^4y^2)^{12}}{(-3x^4y^2)^{10}}$$

$$\frac{(-3x^4y^2)^{10}(-3x^4y^2)^2}{(-3x^4y^2)^{10}}$$

$$(-3)^2 x^{4 \cdot 2} y^{2 \cdot 2}$$

$$9x^8y^4$$

93.

$$-\frac{(-2x^4y^3)^2}{(-3x^5y^7)^3}$$

$$-\frac{(-2)^2 x^{4 \cdot 2} y^{3 \cdot 2}}{(-3)^3 x^{5 \cdot 3} y^{7 \cdot 3}}$$

$$\frac{4x^8y^6}{27x^{15}y^{21}}$$

$$\frac{4x^8y^6}{27x^8x^7y^6y^{15}}$$

$$-\frac{4}{27x^7y^{15}}$$

95.

$$\left(\frac{2x^3y^8}{-3x^6y^4} \right)^5$$

$$\frac{(2x^3y^8)^5}{(-3x^6y^4)^5}$$

$$\frac{(2)^5 x^{3 \cdot 5} y^{8 \cdot 5}}{(-3)^5 x^{6 \cdot 5} y^{4 \cdot 5}}$$

$$\frac{32x^{15}y^{40}}{-243x^{30}y^{20}}$$

$$\frac{-32y^{20}}{243x^{15}}$$

97.

$$\left(\frac{4a^3b^3}{-3a^6b} \right)^6$$

$$\frac{(4a^3b^3)^6}{(-3a^6b)^6}$$

$$\frac{(4)^6 a^{3 \cdot 6} b^{3 \cdot 6}}{(-3)^6 a^{6 \cdot 6} b^6}$$

$$\frac{4096a^{18}b^{18}}{729a^{36}b^6}$$

$$\frac{4096b^{12}}{729a^{18}}$$

$$\begin{aligned} 99. \quad & 2^2 + 3^2 - 4^2 \\ & (2)(2) + (3)(3) - (4)(4) \\ & \quad 4 + 9 - 16 \\ & \quad 13 - 16 \\ & \quad -3 \end{aligned}$$

$$\begin{aligned} 101. \quad & -3^2 - 2^2 \\ & -(3)(3) - (2)(2) \\ & \quad -9 - 4 \\ & \quad -13 \end{aligned}$$

$$\begin{array}{l}
 103. \quad (-3)^2 - 3^2 \\
 (-3)(-3) - (3)(3) \\
 9 \quad - \quad 9 \\
 0
 \end{array}$$

$$\begin{array}{l}
 115. \quad y^{12} \cdot y^4 \\
 y^{12+4} \\
 y^{16}
 \end{array}$$

$$\begin{array}{l}
 105. \quad (-2)^2 - 3^2 \\
 (-2)(-2) - (3)(3) \\
 4 \quad - \quad 9 \\
 -5
 \end{array}$$

$$\begin{array}{l}
 117. \quad 3^2 \cdot 3^4 \\
 3^{2+4} \\
 3^6 \\
 729
 \end{array}$$

$$\begin{array}{l}
 107. \quad (-3)^3 - 2^3 \\
 (-3)(-3)(-3) - (2)(2)(2) \\
 -27 \quad - \quad 8 \\
 -35
 \end{array}$$

$$\begin{array}{l}
 119. \quad (5y^4)(-2y^2) \\
 -10y^{4+2} \\
 -10y^6
 \end{array}$$

$$\begin{array}{l}
 109. \quad (10^3)^2 \\
 (10^3)(10^3) \\
 [(10)(10)(10)][(10)(10)(10)] \\
 [1000][1000] \\
 1,000,000
 \end{array}$$

$$\begin{array}{l}
 121. \quad (-4m^2)(-2m^2) \\
 8m^{2+2} \\
 8m^4
 \end{array}$$

$$\begin{array}{l}
 111. \quad (10^3)^3 \\
 10^{3 \cdot 3} \\
 10^9 \\
 1,000,000,000
 \end{array}$$

$$\begin{array}{l}
 123. \quad (a)(a) \\
 (a^1)(a^1) \\
 a^{1+1} \\
 a^2
 \end{array}$$

$$\begin{array}{l}
 113. \quad a^3 \cdot a^{10} \\
 a^{3+10} \\
 a^{13}
 \end{array}$$

125.

1st week, 3 letters.2nd week, 9 letters

(3 people each send 3 letters)

3rd week, 27 letters

(9 people each send 3 letters)

4th week, 81 letters

(27 people each send 3 letters)

5th week, 243 letters

(81 people each send 3 letters)

On the 5th week, there are 3⁵ or 243 letters sent.

129.

1st second, 3 dominos fall2nd second, 9 dominos fall

(3 dominos each knocks down

3)

3rd second, 27 dominos fall

(9 dominos each knocks down

3)

4th second, 81 dominos fall

(27 dominos each knocks down 3)

On the 4th second, 3⁴ or 81 dominos fall.

127.

1st week, 2 letters2nd week, 4 letters

(2 people each send 2 letters)

3rd week, 8 letters

(4 people each send 2 letters)

4th week, 16 letters

(8 people each send 2 letters)

5th week, 32 letters

(16 people each send 2 letters)

6th week, 64 letters

(32 people each send 2 letters)

7th week, 128 letters

(64 people each send 2 letters)

On the 7th week, there are 2⁷ or 128 letters sent.