

Lab Nr. 6, Probability and Statistics

Random Number Generators; RND;

Computer Simulations of Discrete Random Variables

1. Function **rnd** in Statistics Toolbox; special functions **rand** and **randn**.

2. Using a $\mathcal{U}(0, 1)$ (standard uniform) random number generator, write Matlab codes that simulate the following common discrete probability distributions:

a. **Bernoulli Distribution** $Bern(p)$, with parameter $p \in (0, 1)$: $X \begin{pmatrix} 0 & 1 \\ 1-p & p \end{pmatrix}$;

b. **Binomial Distribution** $Bino(p)$, with parameters $n \in \mathbb{N}, p \in (0, 1)$: $X \begin{pmatrix} k \\ C_n^k p^k q^{n-k} \end{pmatrix}_{k=0, \overline{n}}$;

Hint: A binomial $Bino(n, p)$ variable is the sum of n independent $Bern(p)$ variables;

c. **Geometric Distribution** $Geo(p)$, with parameter $p \in (0, 1)$: $X \begin{pmatrix} k \\ pq^k \end{pmatrix}_{k \in \mathbb{N}}$;

Hint: A geometric $Geo(p)$ variable represents the number of failures (i.e. the number of Bernoulli trials that ended up being failures) needed to get the first success;

d. **Pascal Distribution** $NB(n, p)$ with parameters $n \in \mathbb{N}, p \in (0, 1)$: $X \begin{pmatrix} k \\ C_{n+k-1}^k p^n q^k \end{pmatrix}_{k \in \mathbb{N}}$;

Hint: A Pascal $NB(n, p)$ variable is the sum of n independent $Geo(p)$ variables;