

1. Find  $dy/dx$  by implicit differentiation.

$$y \cos x = x^2 + y^2$$

2. Consider the equation

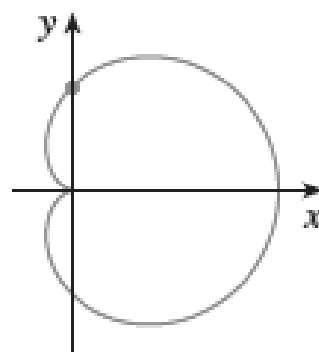
$$\sqrt{x} + \sqrt{y} = 1 \tag{*}$$

- (a) Find  $y'$  by implicit differentiation.
- (b) Solve (\*) explicitly for  $y$  and differentiate to get  $y'$  in terms of  $x$ .
- (c) Check that your solutions in (a) and (b) are consistent.

3. (A §3.4 question.) For what values of  $r$  does the function  $y = e^{rt}$  satisfy the differential equation  $y'' - 4y' + y = 0$ ?

4. For the “cardioid” shown, with the equation and point given, find an equation of the tangent line.

$$x^2 + y^2 = (2x^2 + 2y^2 - x)^2, \quad \left(0, \frac{1}{2}\right)$$



5. If  $xy + e^y = e$ , find the value of  $y''$  at the point where  $x = 0$ .