

Table of Indefinite Integrals

$$\int cf(x) dx = c \int f(x) dx \qquad \int [f(x) + g(x)] dx = \int f(x) dx + \int g(x) dx$$

$$\int k dx = kx + C$$

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C (n \neq -1) \qquad \int \frac{1}{x} dx = \ln|x| + C$$

$$\int e^x dx = e^x + C \qquad \int b^x dx = \frac{b^x}{\ln b} + C$$

$$\int \sin x dx = -\cos x + C \qquad \int \cos x dx = \sin x + C$$

$$\int \sec^2 x dx = \tan x + C \qquad \int \csc^2 x dx = -\cot x + C$$

$$\int \sec x \tan x dx = \sec x + C \qquad \int \csc x \cot x dx = -\csc x + C$$

$$\int \frac{1}{x^2 + 1} dx = \tan^{-1} x + C \qquad \int \frac{1}{\sqrt{1 - x^2}} dx = \sin^{-1} x + C$$

1. For the following integrals, decide if you would use a *u*-substitution. If so, just <u>write</u> down the *u*-substitution. If not, evaluate the integral.

(a)
$$\int e^{\cos x} \sin x \, dx = \underbrace{U = \cos x}$$

(b) $\int \frac{dx}{ax+b} = \underbrace{\frac{1}{a} \ln |\alpha \times + b|} + C$ (or $u = \alpha \times + b$)

(c) $\int_{0}^{2} |2x-1| \, dx = \underbrace{5/2}_{2} = \sec \exp |\alpha + a| = \sin \theta$ on back

(d) $\int_{e}^{e^{4}} \frac{dx}{x\sqrt{\ln x}} = \underbrace{U = \ln x}_{4}$

(e) $\int (7x-7^{-x}) \, dx = \underbrace{\frac{7}{2} \times^{2} + 7^{-x} + C}_{2} = \underbrace{by \ 9ness-and-check}_{2}$

(f) $\int_{0}^{1} x(\sqrt[3]{x} + \sqrt[4]{x}) \, dx = \underbrace{\int_{0}^{1} \times^{4/2} + x^{5/4} \, dx}_{2} = \underbrace{\frac{3}{4}}_{7} \times \frac{7/3}{4} + \underbrace{\frac{4}{7}}_{7} \times \frac{9/4}{4} = \underbrace{\frac{55}{63}}_{63}$

(g) $\int \pi \, dt = \underbrace{(77 + C)}_{1} = \underbrace{(3 + C) + C}_{2} \times \frac{1}{4} + \underbrace{(77 + C)}_{2} = \underbrace{(3 + C) + C}_{2} \times \frac{1}{4} = \underbrace{(3 + C) + C}_{2}$

2. Complete the u-substitution, or any other work, for the integrals from problem **1**.

(a) =
$$\int e^{u}(-du) = -e^{u} + c = (-e^{\cos x} + c)$$

 $V = \cos x$ $du = -\sin x dx$ $-du = \sin x dx$

$$\frac{du}{du} = \int \frac{du}{du} = \frac{1}{a} \int \frac{du}{du} = \frac{1}{a} \ln |u| + C$$

$$= \frac{1}{a} \ln |ax + b| + C$$

U=ax+b du=adx dwa=dx

(c)
$$3\frac{1}{4}$$
 < total area = $\frac{1}{2} \cdot \frac{1}{2} \cdot 1 + \frac{1}{2} \cdot \frac{3}{2} \cdot 3 = \frac{10}{4} = \frac{5}{2}$

$$=\int_{1}^{4}\frac{du}{\sqrt{u}}=\int_{1}^{4}u^{-1/2}du$$

$$U = \ln x$$

$$du = \frac{1}{x} dx$$

$$U(e) = \ln e = 1$$

$$= 2u^{2}]^{4} = 2(\pi - \pi) = 6$$

$$U(e) = he = 1$$

 $U(e^4) = he^4 = 4$

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$$\int \int u^2 du = \frac{1}{3}u^3 + C$$

$$= \left(\frac{1}{3} \tan^3 0 + C\right)$$

$$(j) = \int \frac{du}{u} = \ln|u| + c$$

$$U = tan^{T}x$$

$$du = \frac{1}{1+x^{2}}dx$$