COMPARISON OF MATLAB, OCTAVE, AND PYLAB

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On the next page are two algorithms each in MATLAB/OCTAVE form (left column) and PYLAB form (right column). To download these examples, go to my page bueler.github.io. To get gaussint.m below, for example, go to bueler.github.io/gaussint.m.

A bit of background is useful. MATLAB (www.mathworks.com) was designed by Cleve Moler around 1980 for teaching numerical linear algebra without needing FORTRAN. It has since become a powerful programming language and engineering tool. More than half of UAF 600-level math/science/engineering students are already familiar with it. It is available in most labs and graduate student offices at UAF.

But I like free, open source software. There are several free alternatives to MATLAB, and two of these work well for this course. First, OCTAVE is a MATLAB clone. The ".m" examples on the next page work in an identical way in MATLAB and in OCTAVE. I will mostly use OCTAVE myself for teaching, but I'll test examples in both OCTAVE and MATLAB. To download OCTAVE, go to www.gnu.org/software/octave.

Second, the SCIPY (www.scipy.org) and MATPLOTLIB (matplotlib.org) libraries give the general-purpose interpreted language Python (python.org) all of MATLAB functionality plus quite a bit more. This combination is called Pylab. Using it with the IPYTHON interactive shell (ipython.org) gives the most MATLAB-like experience. The examples on the next page hint at the computer language differences and the different modes of thought between MATLAB/OCTAVE and PYTHON. Students who already use Python will like this option.

Here are some brief "how-to" comments for the MATLAB/OCTAVE examples: gaussint.m is a script. A script is run by starting MATLAB/OCTAVE, usually in the directory containing the script you want to run. Then type the name of the script at the prompt, without the ".m":

>> gaussint

Typing

>> help gaussint

shows the block of comments as documentation.

The second algorithm bis.m is a function which needs inputs. At the prompt enter

>>
$$f = @(x) cos(x) - x$$

>> $bis(0,1,f)$

for example. We have given bis.m three arguments; the last is an "anonymous function."

For the PYTHON versions: Type run gaussint.py at the IPYTHON prompt or python gaussint.py at a shell prompt. For the function bis.py, run PYTHON or IPYTHON and do: from bis import bis. In IPYTHON you can type bis? to get documentation for that function, and run the example as shown in the docstring.

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gaussint.m

```
% plot the integrand and approximate
% the integral
% / 1
  exp(-x^2/pi) dx
용 / 0
% by left-hand, right-hand, and
% trapezoid rules
N = 1000;
dx = (1 - 0) / N;
x = linspace(0,1,N+1);
y = \exp(-x.^2 / pi);
plot(x,v)
axis([0 1 0 1]), grid
format long
lhand = dx * sum(y(1:end-1))
rhand = dx * sum(y(2:end))
trap = (dx/2) * sum(y(1:end-1)+y(2:end))
exact = (pi/2) * erf(1/sqrt(pi))
```

bis.m

```
function c = bis(a,b,f)
% BIS Apply the bisection method to solve
% f(x) = 0
% with initial bracket [a,b].
% example:
  >> f = @(x) cos(x) - x
                                % define fcn
  >> r = bis(0,1,f)
                                % find root
  >> f(r)
                                % confirm
if (feval(f,a)) * (feval(f,b)) > 0
 error('not a bracket!'), end
for k = 1:100
 c = (a+b)/2;
 r = feval(f,c);
 if abs(r) < 1e-12
   return % we are done
 elseif feval(f, a) * r >= 0.0
   a = c;
 else
   b = c;
 end
end
error('no convergence')
```

gaussint.py

```
#!/usr/bin/env python
# plot the integrand and approximate
# the integral
   / 1
   -
          exp(-x^2/pi) dx
     / 0
# by left-hand, right-hand, and
# trapezoid rules
from pylab import plot,axis,linspace,sum, \
                  pi,sqrt,exp,show,grid
from scipy.special import erf
N = 1000
dx = (1.0 - 0.0) / N
x = linspace(0.0, 1.0, N+1)
y = \exp(-x \star \star 2 / pi)
plot(x, y)
axis([0.0,1.0,0.0,1.0]); grid(True)
lhand = dx * sum(y[:-1])
print "lhand = %.15f" % lhand
rhand = dx * sum(y[1:])
print "rhand = %.15f" % rhand
trap = (dx/2) * sum(y[:-1]+y[1:])
print "trap = %.15f" % trap
exact = (pi/2) * erf(1/sqrt(pi))
print "exact = %.15f" % exact
show() # allow user to close figure
```

bis.py

```
def bis(a,b,f):
  """ BIS Apply the bisection method to solve
   f(x) = 0
 with initial bracket [a,b].
 example (after "from bis import bis"):
    def f(x):
       from math import cos
        return cos(x) - x
    r = bis(0.0, 1.0, f)
                                  11 11 11
    print(f(r))
 if f(a) * f(b) > 0.0:
    print "not a bracket!"; return
  for k in range(100):
   c = (a+b)/2
    r = f(c)
   if abs(r) < 1e-12:
     return c # we are done
    elif f(a) * r >= 0.0:
     a = c
    else:
     b = c
 print "no convergence"; return
```