

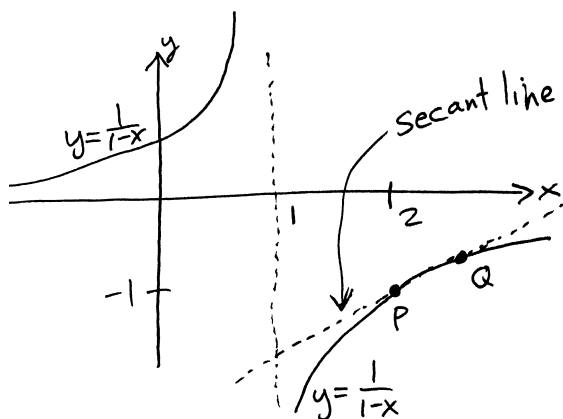
Solutions to Section 2.1 Worksheet

1. The first part has a single, precise answer. For the second and third parts I provide the best answers I can find. (A more thorough search might be required.) The fourth part is just a guess.

1. $m = (0.82 - 0.44)/(2018 - 1990) = +0.0136$ C/year
2. the ten-year period [1992, 2002]: $m = (0.62 - 0.22)/10 = +0.04$ C/year
3. the ten-year period [1998, 2008]: $m = (0.52 - 0.62)/10 = -0.01$ C/year
4. from a line through (2010, 0.70) that looks vaguely reasonable: $m = +0.0074$ C/year

Every function, even data which is really bumpy or rough, does have secant lines. However, for rough data such slopes don't mean much! Calculus is mostly about better-behaved functions like in the problems below.

2. a)



- b) In this part P is the fixed point (2, -1) while Q is the point given by the following x-values.

Let $f(x) = 1/(1-x)$. Then:

- (i) $m = (f(1.5) - f(2))/(1.5 - 2) = 2.0$
 - (ii) $m = (f(1.99) - f(2))/(1.99 - 2) = 1.01$
 - (iii) $m = (f(1.999) - f(2))/(1.999 - 2) = 1.001$
 - (iv) $m = (f(2.5) - f(2))/(2.5 - 2) = 0.6667$
 - (v) $m = (f(2.01) - f(2))/(2.01 - 2) = 0.9901$
 - (vi) $m = (f(2.001) - f(2))/(2.001 - 2) = 0.9990$
- c) Based on the above I would guess that the tangent line slope at $P(2, -1)$ is $m = 1$.
- d) We now have a point and a slope. Thus we get the equation of the line:

$$y - (-1) = 1(x - 2) \quad \text{or} \quad y = x - 3$$

3. If you plot the data (with a computer?) you see it is all close to one line. Here we first compute the four secant line slopes:

- a) $m = 68.8$ beats/min
- b) $m = 71.8$ beats/min
- c) $m = 72.5$ beats/min
- d) $m = 71.0$ beats/min

Now we can say, with some confidence, that the heart monitor should report a number between 68 and 73. My choice for best estimate averages the secant slopes from a) and b) and uses the difference for an estimate of uncertainty:

$$m = \frac{1}{2}(68.8 + 71.8) = 70.3 \pm 1.5 \text{ beats/min}$$

(Your answer will be different but it should follow the same, general idea.)