SOLUTIONS

1. Differentiate the function.

$$F(r) = \frac{5}{r^3}$$

$$F(r) = 5 r^{-3}$$

$$F(r) = -15 r^{-4}$$

$$y = 3e^{x} + \frac{4}{\sqrt[3]{x}}$$

$$y = 3e^{x} + 4x^{-1/3}$$

$$\frac{dy}{dx} = 3e^{x} - \frac{4}{3}x^{-4/3}$$

$$G(q) = (1+q^{-1})^{2}$$

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$$G(q) = (1+q^{-1})^{2} + q^{-2} = (1+2q^{-1}+q^{-2})^{2}$$

$$G'(q) = -2q^{-2} - 2q^{-3}$$

2. Find equations of the tangent line and normal line to the curve at the given point: $y = x^2 + 2e^x$, (0,2)

$$\frac{dy}{dx} = 2x + 2e^{x}$$

$$\frac{m}{dx} = \frac{dy}{dx}\Big|_{x=0} = 0 + 2e^{0} = 2, \quad m_{normal} = \frac{-1}{2}$$

$$\frac{\tan y}{dx}\Big|_{x=0} = 0 + 2e^{0} = 2, \quad m_{normal} = \frac{-1}{2}$$

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- **3.** The equation of motion of a particle is $s = t^4 2t^3 + t^2 t$, where s is in meters and t is in seconds.
 - (a) Find the velocity and acceleration as functions of t.

$$V = S' = \dot{S} = 4t^3 - 6t^2 + 2t - 1$$

$$Q = V' = S'' = \dot{S} = 12t^2 - 12t + 2$$

(b) Find the acceleration after 1 s.

$$a(1) = 12 - 12 + 2 = 2 \frac{m}{5^2}$$

4. Find an equation of a tangent line to the curve $y = x^4 + 1$ which is parallel to the line 32x - y = 15.

line
$$32x - y = 15$$
.
I Me $y = 32x - 15$ has $m = 32$
and $\frac{dy}{dx} = 4x^3 + 0 = 4x^3$ \Rightarrow 501 $y = 2$ $y - 17 = 32(x - 2)$ \Rightarrow 50 $y = 2$ $y + 1 = 17$

5. Find the first and second derivatives of the function.

$$G(r) = \sqrt{r} - \sqrt[3]{r}$$

$$G(r) = r^{2} - r^{2}$$

$$G(r) = \frac{1}{2}r^{-1/2} - \frac{1}{3}r^{-3/3}$$

$$G''(r) = -\frac{1}{4}r^{-3/2} + \frac{2}{9}r^{-5/3}$$