```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
      [] => []
      | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

Optional: Java/C# Arrays

Picking on Java (and C#)

Arrays should work just like records in terms of depth subtyping

- But in Java, if t1 <: t2, then t1[] <: t2[]</p>
- So this code type-checks, surprisingly

```
class Point { ... }
class ColorPoint extends Point { ... }
void m1 (Point[] pt arr) {
 pt arr[0] = new Point(3,4);
String m2 (int x) {
  ColorPoint[] cpt arr = new ColorPoint[x];
  for (int i=0; i < x; i++)
     cpt arr[i] = new ColorPoint(0,0,"green");
 m1(cpt arr); //!
  return cpt arr[0].color; // !
```

Why did they do this?

- More flexible type system allows more programs but prevents fewer errors
 - Seemed especially important before Java/C# had generics
- Good news: despite this "inappropriate" depth subtyping
 - e.color will never fail due to there being no color field
 - Array reads e1[e2] always return a (subtype of) t if e1 is a t[]
- Bad news: to get the good news
 - e1[e2]=e3 can fail even if e1 has type t[] and e3 has type t
 - Array stores check the run-time class of e1's elements and do not allow storing a supertype
 - No type-system help to avoid such bugs / performance cost

So what happens

- Causes code in m1 to throw an ArrayStoreException
 - Even though logical error is in m2
 - At least run-time checks occur only on array stores, not on field accesses like c.color

null

- Array stores probably the most surprising choice for flexibility over static checking
- But **null** is the most *common* one in practice
 - null is not an object; it has no fields or methods
 - But Java and C# let it have any object type (backwards, huh?!)
 - So, in fact, we do not have the static guarantee that evaluating
 e in e.f or e.m(...) produces an object that has an f or m
 - The "or null" caveat leads to run-time checks and errors, as you have surely noticed
- Sometimes null is convenient (like ML's option types)
 - But also having "cannot be null" types would be nice