```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
      [] => []
      | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman 2013

Subtyping for OOP

Now...

Use what we learned about subtyping for records and functions to understand subtyping for class-based OOP

Like in Java/C#

Recall:

- Class names are also types
- Subclasses are also subtypes
- Substitution principle: Instance of subclass should usable in place of instance of superclass

An object is...

- Objects: mostly records holding fields and methods
 - Fields are mutable
 - Methods are immutable functions that also have access to self
- So could design a type system using types very much like record types
 - Subtypes could have extra fields and methods
 - Overriding methods could have contravariant arguments and covariant results compared to method overridden
 - Sound only because method "slots" are immutable!

Actual Java/C#...

Compare/contrast to what our "theory" allows:

- 1. Types are class names and subtyping are explicit subclasses
- 2. A subclass can add fields and methods
- 3. A subclass can override a method with a covariant return type
 - (No contravariant arguments; instead makes it a nonoverriding method of the same name)
- (1) Is a subset of what is sound (so also sound)
- (3) Is a subset of what is sound and a different choice (adding method instead of overriding)

Classes vs. Types

- A class defines an object's behavior
 - Subclassing inherits behavior and changes it via extension and overriding
- A type describes an object's methods' argument/result types
 - A subtype is substitutable in terms of its field/method types
- These are separate concepts: try to use the terms correctly
 - Java/C# confuse them by requiring subclasses to be subtypes
 - A class name is both a class and a type
 - This confusion is convenient in practice

Optional: More details

Java and C# are sound: They do not allow subtypes to do things that would lead to "method missing" or accessing a field at the wrong type

Confusing (?) Java example:

- Subclass can declare field name already declared by superclass
- Two classes can use any two types for the field name
- Instance of subclass have two fields with same name
- "Which field is in scope" depends on which class defined the method

Optional: self/this is special

- Recall our Racket encoding of OOP-style
 - "Objects" have a list of fields and a list of functions that take
 self as an explicit extra argument
- So if **self/this** is a function argument, is it contravariant?
 - No, it is covariant: a method in a subclass can use fields and methods only available in the subclass: essential for OOP

```
class A {
  int m() { return 0; }
}
class B extends A {
  int x;
  int m() { return x; }
}
```

- Sound because calls always use the "whole object" for self
- This is why coding up your own objects manually works much less well in a statically typed languages