

### Mathematical Analyzation:

The program is a sequence containing light and dark disks that moves in an alternating pattern, where there cannot be a repeating light or dark disk. Building upon and deleting some parts from the linked list algorithm displays a time complexity of  $O(N)$  because there is a one-to-one cardinality between the actions. However, time complexity is different under the core part of the algorithm, which is the recursiveSort function. Each call from the recursive function has a time complexity of  $O(1)$  because there is a constant number of comparisons and possible swaps from the left and right. The worst-case scenario for the program in terms of time complexity would result in a maximum of  $O(n^2)$ , which is dependent on the depth and the distance of travel it needs. Through induction,

Assume that for any list of Size  $k$ , the algorithm sorts itself in  $O(k^2)$  time, where the base case immediately returns to  $O(1)$  through a single node.

The inductive step is  $(n = k + 1)$  where the work would be:  $T(k+1) = O(k) + O(k^2) = O((k+1)^2)$

Thus, by induction, the algorithm runs in quadratic time.