

Review

K -subsets: You can use almost the same idea as for the power set:

partition solution space into

$$\{H \subseteq S \mid x \in H\} \text{ and } \{H \subseteq S \mid x \notin H\}.$$

\parallel
 K_x

\parallel
 \bar{K}_x

$$\boxed{\text{ksub}(S, k) = K_x \cup \bar{K}_x}$$

How to compute \bar{K}_x ? Just make a recursive call:

$$\bar{K}_x = \text{ksub}(S \setminus \{x\}, k).$$

How to compute K_x ?

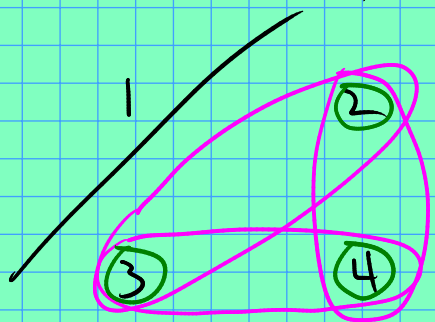
First compute $\text{ksub}(S \setminus \{x\}, \underline{k-1})$ and then add x to all of the resulting sets.

Base case? if $k > |S|$, return $\{\}$

if $k = 0$, return $\{\{\}\}$

Example:

say $k=2$. Let $x=1$.

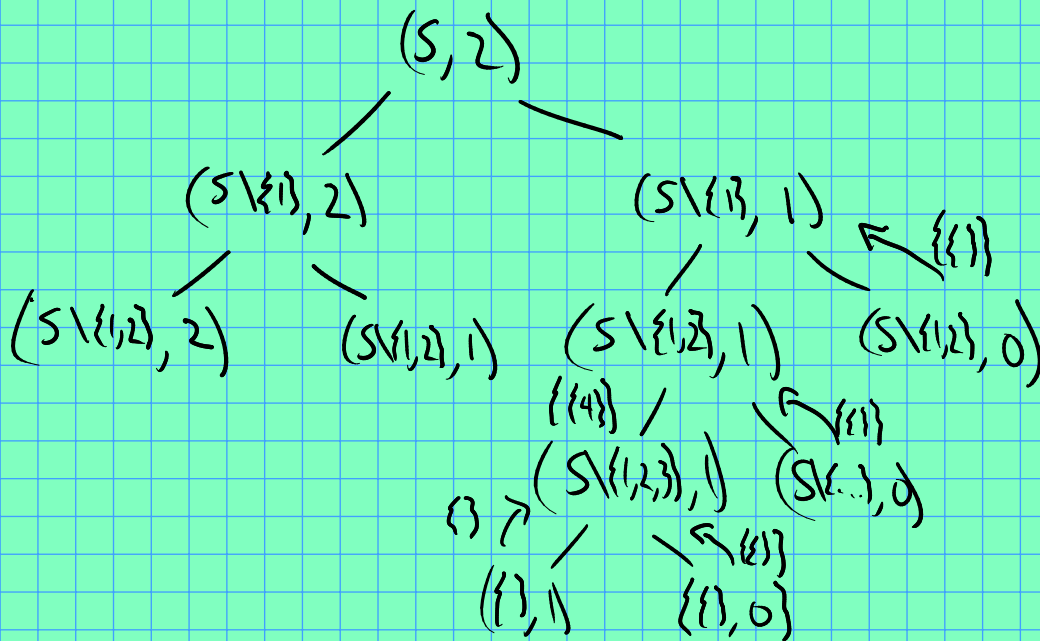


Final result:

$\{2,3\}, \{2,4\}, \{3,4\},$
 $\{1,2\}, \{1,3\}, \{1,4\}$

Recursion tree for the above:

$$S = \{1,2,3,4\}, k=2$$



It's getting a little messy. I'll leave the rest as an exercise.