

$$2. (a) 100001_{(2)} = 1 \cdot 2^5 + 0 + 0 + 0 + 0 + 1 \cdot 2^0_{(10)}$$

$$= 33_{(10)}$$

$$(b) 100111_{(2)} = 1 \cdot 2^5 + 0 + 0 + 1 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0$$

$$= 39_{(10)}$$

$$(c) 101010_2 = 1 \cdot 2^5 + 0 + 1 \cdot 2^3 + 0 + 1 \cdot 2^1 + 0$$
$$= 42_{(10)}$$

$$(d) 111001_{(2)} = 1 \cdot 2^5 + 1 \cdot 2^4 + 1 \cdot 2^3 + 0 + 0 + 1 \cdot 2^0$$

3. (e) $65_{(10)} = 2^6 + 2^0_{(10)} = 1000001_{(2)}$

(f) $97_{(10)} = 2^6 + 2^5 + 2^0_{(10)} = 1100001_{(2)}$

(g) $127_{(10)} = 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0_{(10)} = 111111_{(2)}$

(h) $190_{(10)} = 2^7 + 2^6 + 2^2 + 2^1_{(10)} = 11000110_{(2)}$

$$4. (27) 0.26_{(10)} = 2^{-2} + 2^{-7} + 2^{-9} + \epsilon_{(10)} = 0.010000101 \dots_{(2)}$$

$$(b) 0.762_{(10)} = 2^{-1} + 2^{-2} + 2^{-7} + 2^{-8} + \epsilon_{(10)} = 0.110000110_{(2)}$$

(c) $0.0975_{(10)} = 2^{-4} + 2^{-5} + 2^{-9} + \epsilon_{(10)} = 0.000110001..._{(2)}$

5. (2) $\underbrace{101010}_{\text{invert}} \xrightarrow{\text{convert 2's complement}} 010110$

(f) $\underbrace{11001}_{\text{invert}} \xrightarrow[\text{2's complement}]{\text{convert}} 00111$

eg) 11001100 $\xrightarrow{\text{convert 2's complement}}$ 00110100

(ch) $\underbrace{11000111}_{\text{invert}} \xrightarrow{\text{convert } 2^{\text{'s}} \text{ complement}}} 00111001$

$$6.(2). 10011001_{(2)} = -2^7 + 2^4 + 2^3 + 2^0_{(10)} = -103_{(10)}$$

(b) $01110100_{(2)} = 2^6 + 2^5 + 2^4 + 2^2 = 116_{(10)}$

$$(c) \ 10111111_{(2)} = -2^7 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0_{(10)} = -65$$

$$\begin{array}{r} 7.(2) \quad 00010110_{(2)} \\ \quad \quad 00110011_{(2)} \\ \hline 01001001_{(2)} \end{array}$$

$$\begin{array}{r} (b) \quad 01110000_2 \\ \quad \quad 10101111_2 \\ \hline \quad \quad 10001111_2 = 00011111_2 \\ \text{(ignored)} \end{array}$$

8. (a) $00110011 - \underbrace{00010000}_{\text{invert}}_{(2)} = \begin{array}{r} 00110011_{(2)} \\ 11100000_{(2)} \\ \hline 10010011_{(2)} \end{array}$
 ignored
 $= 00100011_{(2)}$

(b) $01100101 - \underbrace{11101000}_{\text{invert}} (2) : \begin{array}{r} 01100101 (2) \\ 00011000 (2) \\ \hline 01111101 (2) \end{array}$

$$9.10001000_{(2)} \div 00100010_{(2)}$$

$$\begin{array}{r} 10001000 \text{ (2)} \\ 11011110 \text{ (2)} \\ \hline \end{array} + \quad \text{Add 1 to quotient}$$

$$\begin{array}{r} 101100110 \text{ (2)} \\ 11011110 \text{ (2)} \\ \hline \end{array} + \quad \text{Add 1 to quotient}$$

$$\begin{array}{r} 1010001100 \text{ (2)} \\ 11011110 \text{ (2)} \\ \hline \end{array} + \quad \text{Add 1 to quotient}$$

$$\begin{array}{r} 100100010 \text{ (2)} \\ 11011110 \text{ (2)} \\ \hline \end{array} + \quad \text{Add 1 to quotient}$$

$$\begin{array}{r} 100000000 \text{ (2)} \\ \hline \end{array}$$

quotient = $-4_{(10)} = 1111100 \text{ (2)}$

$$10_{(2)} 1111_{(2)} = F_{16}$$

$$(b) 1011(2) = B_{16}$$

(c) $\underbrace{0001}_{1} \underbrace{1111}_{15} (2) = 1F_{16}$

$$\begin{array}{r}
 11(a) \quad 60_{(16)} \\
 \underline{39_{(16)}} \\
 27_{(16)}
 \end{array}
 \quad
 \begin{array}{r}
 (b) \quad A5_{(16)} \\
 \underline{9\theta_{(16)}} \\
 D_{(16)}
 \end{array}$$

$$\begin{array}{r}
 (c) \quad F1_{(16)} \\
 \underline{A6_{(16)}} \\
 4B_{(16)}
 \end{array}
 \quad
 \begin{array}{r}
 (d) \quad AC_{(16)} \\
 \underline{10_{(16)}} \\
 9C_{(16)}
 \end{array}$$

$$\begin{aligned}
 12(a) \quad 0010_{(BCD)} + 0001_{(BCD)} &= 2_{(10)} + 1_{(10)} = 0011_{(BCD)} \\
 (b) \quad 0101_{(BCD)} + 0011_{(BCD)} &= 5_{(10)} + 3_{(10)} = 1000_{(BCD)} \\
 (c) \quad 0111_{(BCD)} + 0010_{(BCD)} &= 7_{(10)} + 2_{(10)} = 1001_{(BCD)} \\
 (d) \quad 1000_{(BCD)} + 0001_{(BCD)} &= 8_{(10)} + 1_{(10)} = 1001_{(BCD)}
 \end{aligned}$$

13. 30 INPUT A, B

51 48 32 73 78 80 85 84 032 065 044 032 066

00110011 00110000 00100000 01001001 01001110 01010000 01010101
 01010100 00100000 01000001 00101100 00100000 01000010

$$\begin{aligned}
 14(a) \quad 11110110 &\rightarrow (1+1+1+1+0+1+1+0) \bmod 2 = 0 \\
 &\quad \text{(ERROR)} \\
 (b) \quad 00110001 &\rightarrow (0+0+1+1+0+0+0+1) \bmod 2 = 1 \\
 &\quad \text{(NO ERROR)}
 \end{aligned}$$

$$(c) \quad 01010101010101010 \rightarrow (0+1+0+1+0+1+0+1+0+1+0+1+0+1+0) \bmod 2 = 0 \quad \text{(ERROR)}$$

$$15. \quad 10110010 \rightarrow 10110010 \oplus 0000$$

$$\begin{array}{r}
 101100100000 \\
 \underline{1010} \oplus \\
 1001 \\
 \underline{1010} \oplus \\
 1100 \\
 \underline{1010} \oplus \\
 1100 \\
 \underline{1010} \oplus \\
 1100 \\
 \underline{1010} \oplus \\
 1100 \\
 \underline{1010} \oplus \\
 1100 \\
 \underline{1010} \oplus \\
 110
 \end{array}$$

\Rightarrow Transmitted value is 10110010110