

$$\Sigma_1 = (A \oplus B) \oplus C_{in} = (1 \oplus 0) \oplus 0 = 1$$

$$\Rightarrow C_{out} = AB + BC + AC = 1 \cdot 0 + 0 \cdot 0 + 1 \cdot 0 = 0$$

$$\Sigma_2 = (A \oplus B) \oplus C_{in} = (1 \oplus 1) \oplus 0 = 0$$

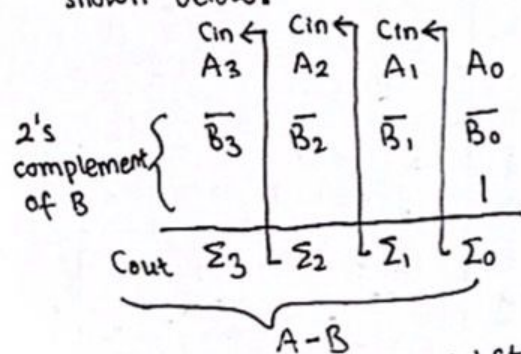
$$\Rightarrow C_{out} = AB + BC + AC = 1 \cdot 1 + 1 \cdot 0 + 1 \cdot 0 = 1$$

$$\Sigma_3 = (A \oplus B) \oplus C_{in} = (1 \oplus 0) \oplus 1 = 0$$

$$\Rightarrow \Sigma_4 = AB + BC + AC = 1 \cdot 0 + 0 \cdot 1 + 1 \cdot 1 = 1$$

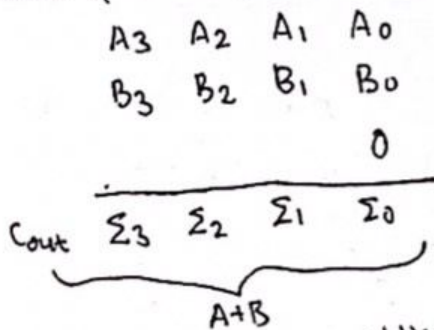
$$\Sigma_4 \Sigma_3 \Sigma_2 \Sigma_1 = 1001$$

2. When add/sub is high, the XOR gate produces complements of their inputs, so full adder addition function is as shown below:

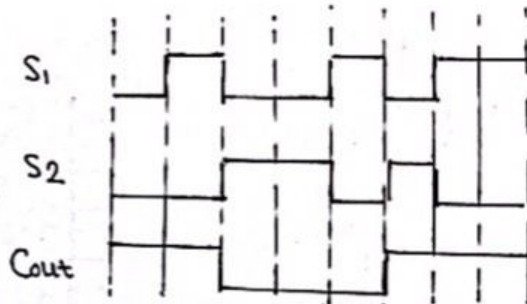
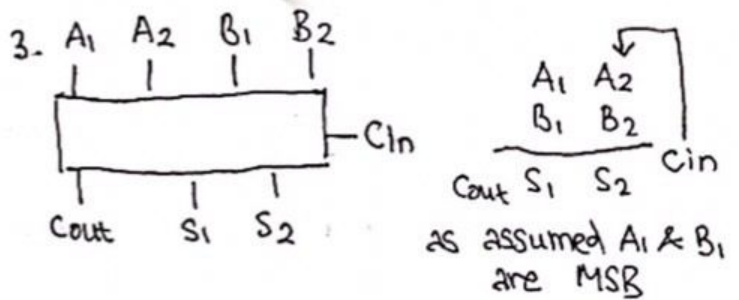


the operation performs subtraction

When add/sub is low, the XOR gate produces the outputs whereas similar with the inputs, so full adder function is as show below:



the operation performs addition



derived truth table is:

$A_1$	$A_2$	$B_1$	$B_2$	$C_{in}$	$S_1$	$S_2$	$C_{out}$
1	0	1	0	0	0	0	1
1	1	1	1	0	1	0	1
0	1	0	0	0	0	1	0
0	0	0	1	0	0	1	0
0	1	0	0	1	1	0	0
1	1	0	1	1	0	1	1
1	1	1	0	1	1	0	1
1	0	1	1	1	1	0	1

4. first clock pulse:

$$A = A_3 A_2 A_1 A_0 = 1001$$

$$B = B_3 B_2 B_1 B_0 = 0100$$

since the binary sequence of A is larger than B,  $A > B$  is high

second clock pulse:

$$A = A_3 A_2 A_1 A_0 = 1111$$

$$B = B_3 B_2 B_1 B_0 = 1111$$

since the binary sequence of A is equal to B,  $A = B$  is high

third clock pulse:

$$A = A_3 A_2 A_1 A_0 = 1110$$

$$B = B_3 B_2 B_1 B_0 = 0010$$

since the binary sequence of A is larger than B,  $A > B$  is high

fourth clock pulse:

$$A = A_3 A_2 A_1 A_0 = 1100$$

$$B = B_3 B_2 B_1 B_0 = 0011$$

since the binary sequence of A is larger than B,  $A > B$  is high

fifth clock pulse:

$$A = A_3 A_2 A_1 A_0 = 0101$$

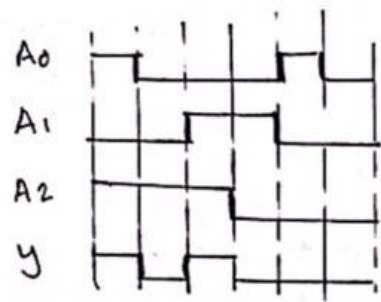
$$B = B_3 B_2 B_1 B_0 = 1100$$

since the binary sequence of A is smaller than B,  $A < B$  is high

COMP	1	2	3	4	5
$A > B$	1	0	1	1	0
$A = B$	0	1	0	0	0
$A < B$	0	0	0	0	1



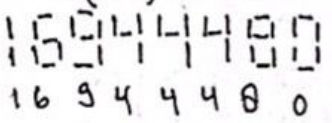
5.  $y = \bar{A}_0 A_1 A_2 + A_0 \bar{A}_1 A_2 + \bar{A}_0 A_1 \bar{A}_2$   
 $= A_0 \bar{A}_1 A_2 + \bar{A}_0 A_1$



6.

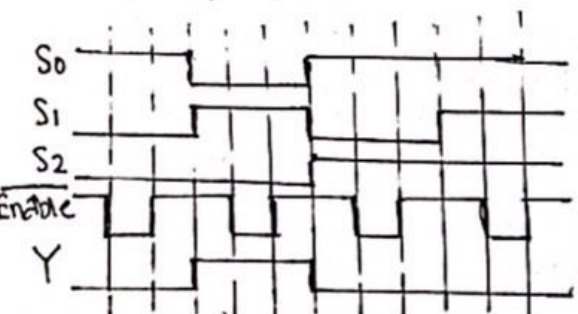
	A <sub>3</sub>	A <sub>2</sub>	A <sub>1</sub>	A <sub>0</sub>	waveform sequence
0	0	0	0	0	8
1	0	0	0	1	1
2	0	0	1	0	
3	0	0	1	1	
4	0	1	0	0	4,5,6
5	0	1	0	1	
6	0	1	1	0	2
7	0	1	1	1	
8	1	0	0	0	7
9	1	0	0	1	3

waveform sequence is read from timing diagram, reading taken from bottom to top, therefore, it will display:



7.

	S <sub>2</sub>	S <sub>1</sub>	S <sub>0</sub>	Y
	0	0	0	D <sub>0</sub>
	0	0	1	D <sub>1</sub>
	0	1	0	D <sub>2</sub>
	0	1	1	D <sub>3</sub>
	1	0	0	D <sub>4</sub>
	1	0	1	D <sub>5</sub>
	1	1	0	D <sub>6</sub>
	1	1	1	D <sub>7</sub>



$\overline{\text{Enable}} = 0$  implies the output depends on the inputs  
 $\overline{\text{Enable}} = 1$  implies the output doesn't depend on the input

8. (a) The A<sub>1</sub> input is open (top adder)

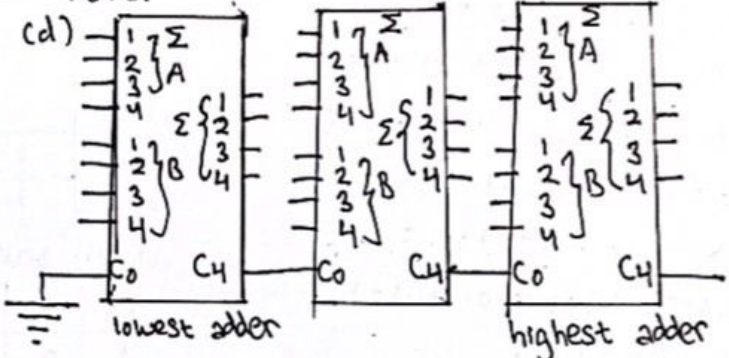
$\Sigma = 1$  Cout = 1

(b) The Cout is open (top adder)

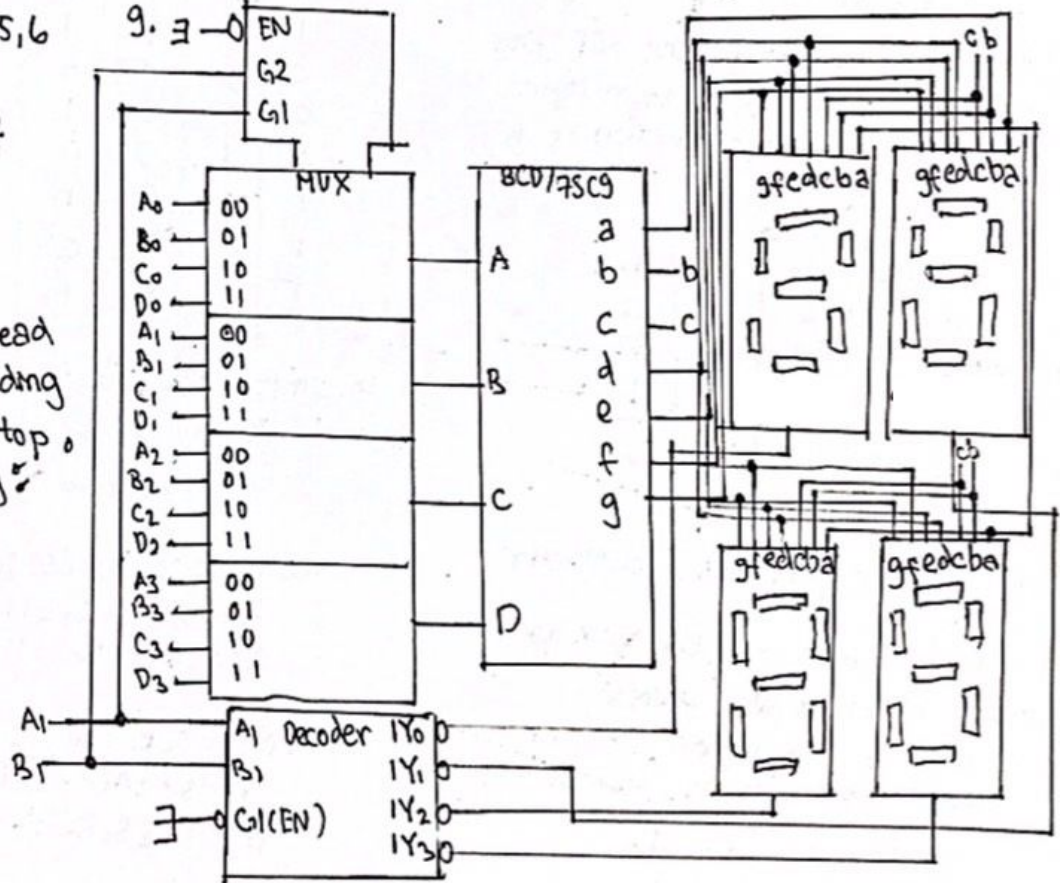
$\Sigma_1 = 0 \quad \Sigma_2 = 0 \quad \Sigma_3 = 1 \quad \Sigma_4 = 1$

(c) The  $\Sigma_4$  output is shorted to ground (top adder)

1011  
 1010  
 10101



9.  $\Sigma$



10. A<sub>3</sub> A<sub>2</sub> A<sub>1</sub> A<sub>0</sub> output(Y) the circuit coin looks like,

0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

