

Yohandi - assignment 9

14. $\omega_t^2 = \omega_0^2 + 2\theta\alpha$

$(15 \text{ rev/s})^2 = (10 \text{ rev/s})^2 + 2 \cdot 60 \text{ rev} \cdot \alpha$

a) $\alpha = 1.0417 \text{ rev/s}^2$

b) $\omega_t = \omega_0 + \alpha t$

$t = \frac{\omega_t - \omega_0}{\alpha} = \frac{15 - 10}{1.0417} \text{ s} = 4.800 \text{ s}$

c) $t = \frac{\omega_t - \omega_0}{\alpha} = \frac{10 - 0}{1.0417} \text{ s} = 9.600 \text{ s}$

d) $\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$

$\theta = (0 + 0 + \frac{1}{2} \cdot 1.0417 \cdot 9.6^2) \text{ rev}$

$= 48 \text{ rev}$

28. $V_A = V_C$

$\omega_A R_A = \omega_C R_C$

$\omega_C = \frac{\omega_A R_A}{R_C} = \frac{(\omega_A t) R_A}{R_C}$

$\Rightarrow t = \frac{\omega_C R_C}{\omega_A R_A} = \frac{100 \cdot 2\pi \cdot 0.25}{60 \cdot 2\pi \cdot 0.10} \text{ s}$

$= \frac{250\pi}{60} \text{ s}$

$= \frac{25}{6} \pi \text{ s} = 13 \text{ s}$

e) $I = \frac{L}{\alpha} = \frac{(T_2 - T_1) R}{\alpha} = 0.0139 \text{ kg} \cdot \text{m}^2$

53. $\omega_t = \omega_0 + \alpha t$

$250 = 0 + \alpha \cdot (1.25 - 0)$

$\alpha = 200 \text{ rad/s}^2 (\curvearrowright)$

$\tau = I \alpha$

$(F_2 - F_1) R = I \alpha$

$(F_2 - F_1) R = \frac{1}{2} M R^2 \alpha$

$F_2 = F_1 + \frac{1}{2} M R \alpha$

$= (0.100 + \frac{1}{2} \cdot 0.02 \cdot 0.02 \cdot 200) \text{ N}$

$= 0.140 \text{ N}$

56. $I_f = m L_1^2 + m L_2^2 = m (L_1^2 + L_2^2)$

$\tau = I \alpha$

$m g L_2 - m g L_1 = m (L_1^2 + L_2^2) \alpha$

$g (L_2 - L_1) = (L_1^2 + L_2^2) \alpha$

$\alpha = 8.647 \text{ rad/s}^2 (\curvearrowright)$

a) $a_1 = \alpha R_1 = \alpha L_1 = 1.73 \text{ m/s}^2 (\uparrow)$

b) $a_2 = \alpha R_2 = \alpha L_2 = 6.92 \text{ m/s}^2 (\downarrow)$

41. a) $I = (\frac{1}{12} M d^2 + M (\frac{d}{2})^2) + (m d^2) + (\frac{1}{12} M d^2 + M (\frac{3d}{2})^2) + (m (2d)^2)$

$= \frac{8}{3} M d^2 + 5 m d^2$

$= 0.02336 \text{ kg} \cdot \text{m}^2$

b) $K = \frac{1}{2} I \omega^2 = 0.00105 \text{ J}$

51. $m_2 g - T_2 = m_2 a \dots (1)$

$\tau = I \alpha$

$(T_2 - T_1) R = \frac{1}{2} M R^2 \cdot \frac{a}{R}$

$T_2 - T_1 = \frac{1}{2} M a \dots (2)$

$\Rightarrow T_1 - m_1 g = m_1 a \dots (2)$

a) $h_0 = h + v_0 t - \frac{1}{2} a t^2$

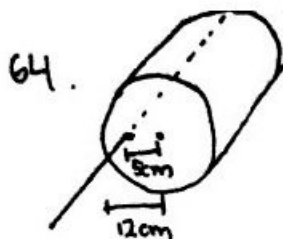
$-0.75 = 0 + 0 - \frac{1}{2} \cdot a \cdot 5.00^2$

$a = 0.06 \text{ m/s}^2 (\downarrow)$

b) $T_2 = m_2 (g - a) = 4.87 \text{ N}$

c) $T_1 = m_1 (g + a) = 4.5356 \text{ N}$

d) $\alpha = \frac{a}{R} = 1.2 \text{ rad/s}^2 (\curvearrowright)$



64. a. $I = I_{\text{cm}} + M d^2$

$= \frac{1}{2} M R^2 + M (\frac{5}{12} R)^2$

$= \frac{97}{144} M R^2$

$= 0.2425 \text{ kg} \cdot \text{m}^2$

b. $\Delta K + \Delta U = 0$

$\frac{1}{2} I \omega^2 - m g h = 0$

$\omega = \sqrt{\frac{2 m g h}{I}}$

$= \sqrt{\frac{2 \cdot (2.5 \times 9.8) \cdot (0.05)}{0.2425}} \text{ rad/s}$

$= 10.05 \text{ rad/s}$