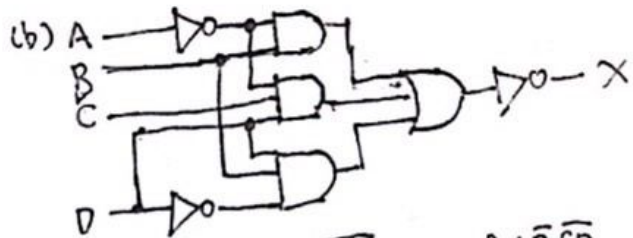


$$X = \bar{A} + \bar{A}B + AC$$

$$= \bar{A} + AC$$

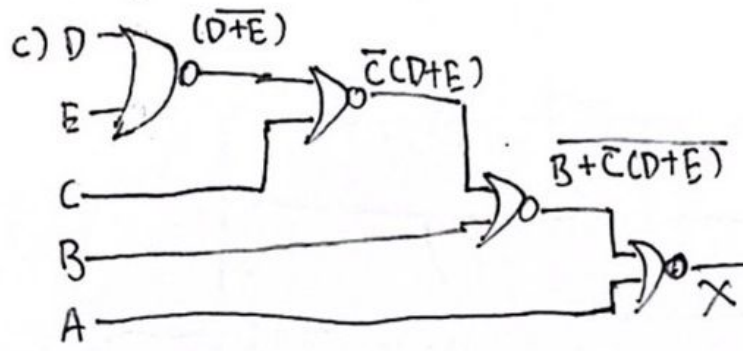
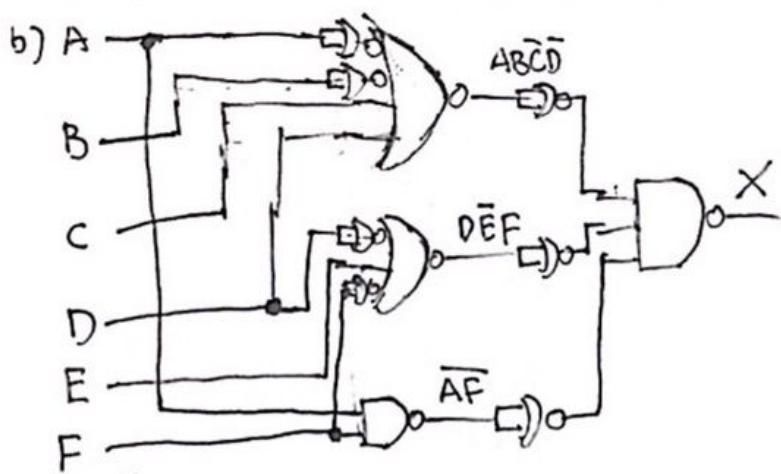
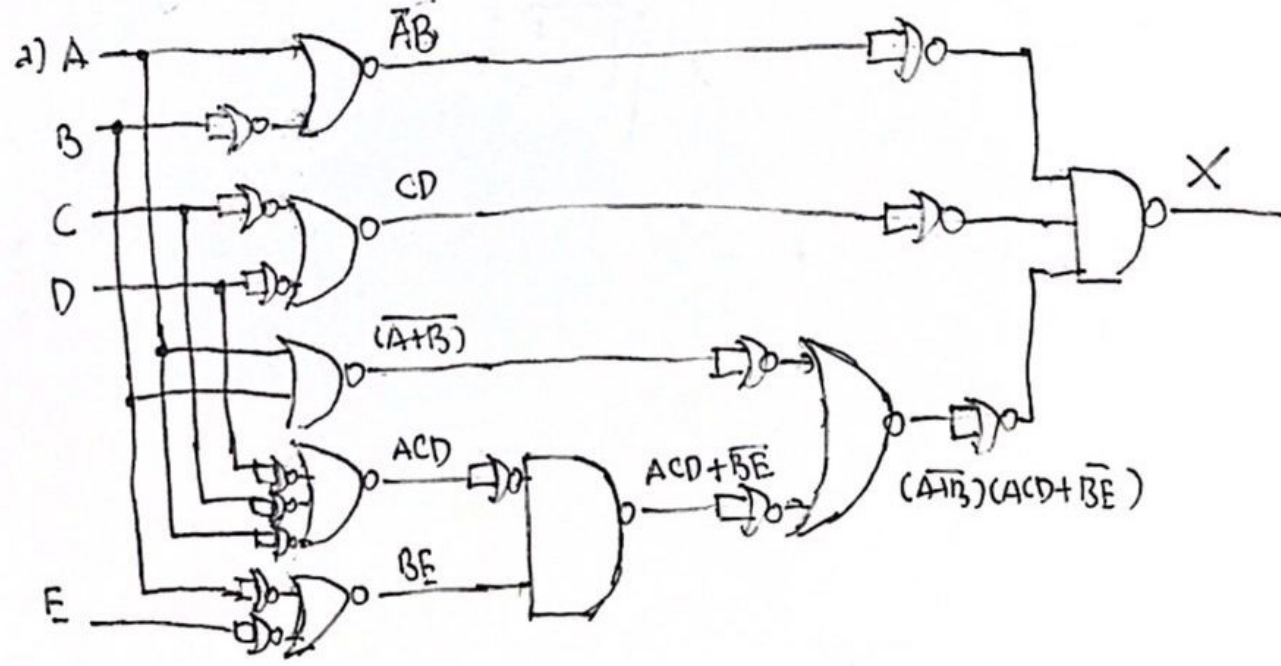
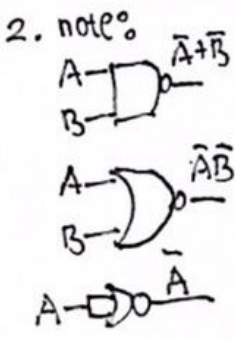


$$X = \bar{A}B + \bar{A}C\bar{D} + B\bar{D}$$

$$= \bar{A}(B + C\bar{D})$$

$$= \bar{A}(B + C\bar{D})$$

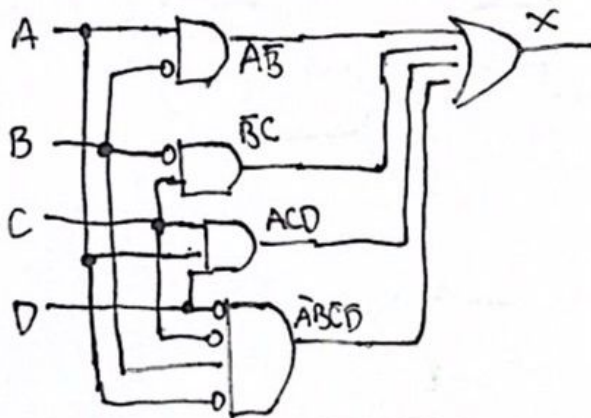
$$= A + \bar{B}\bar{C} + \bar{B}\bar{D}$$



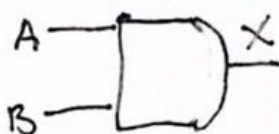
3. K-map,

	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$			1	1
$\bar{A}B$	1			
AB			1	
$A\bar{B}$	1	1	1	1

$$X = \bar{A}\bar{B} + \bar{B}\bar{C} + ACD + \bar{A}BC\bar{D}$$



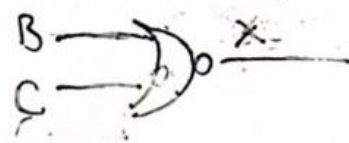
4a) $X = AB + ABC$
 $= AB(1 + C)$
 $= AB$



A	B	C	AB	ABC	AB + ABC
0	0	0	0	0	0
0	0	1	0	0	0
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	0	0	0
1	0	1	0	0	0
1	1	0	1	0	1
1	1	1	1	1	1

identical

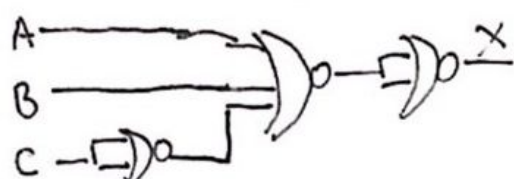
b) $X = (\overline{(AB)(B+C)}) + C$
 $= (\bar{A}\bar{B})(\bar{B} + \bar{C})\bar{C}$
 $= (\bar{A} + \bar{B})(\bar{B}\bar{C})\bar{C}$
 $= \bar{A}\bar{B}\bar{C} + \bar{B}\bar{B}\bar{C}$
 $= \bar{B}\bar{C}$



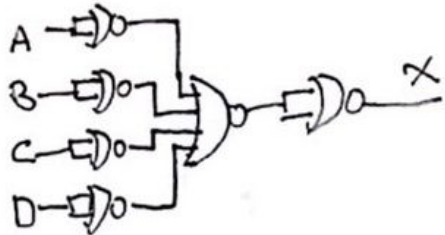
A	B	C	AB	$\bar{B}\bar{C}$	B+C	$(\overline{(AB)(B+C)}) + C$
0	0	0	0	1	0	1
0	0	1	0	0	1	0
0	1	0	0	0	1	0
0	1	1	0	0	1	0
1	0	0	0	1	0	1
1	0	1	0	0	1	0
1	1	0	1	0	1	0
1	1	1	1	0	1	0

identical

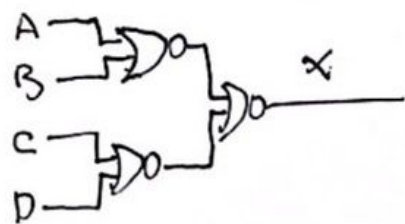
5(d) $X = A + B + \bar{C} = \overline{(\bar{A}\bar{B}\bar{C})}$



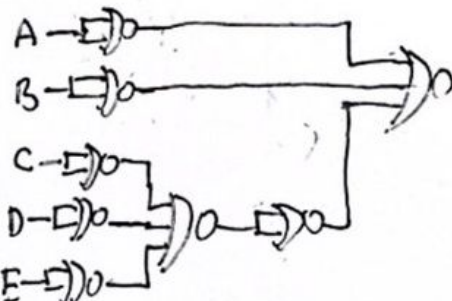
6c) $X = \bar{A}\bar{B} + \bar{C}\bar{D} = \overline{(\bar{A} + \bar{B})(\bar{C} + \bar{D})}$



cf) $X = (A + B)(C + D) = \overline{(\bar{A}\bar{B})(\bar{C}\bar{D})}$



cg) $X = AB[C(\bar{D}\bar{E} + \bar{A}\bar{B}) + \bar{B}\bar{C}\bar{E}]$
 $= \bar{A}\bar{B} + (C(\bar{D}\bar{E} + \bar{A}\bar{B})(\bar{B} + \bar{C} + \bar{E}))$
 $= \bar{A}\bar{B} + (\bar{A} + \bar{B} + \bar{C} + \bar{D} + \bar{E})$
 $= \bar{A} + \bar{B} + (\bar{C} + \bar{D} + \bar{E})$



G. K-map, \bar{C} C

$\bar{A}\bar{B}$

$\bar{A}B$

AB

AB



$$X = AC + A\bar{B} = A(\bar{B} + C)$$

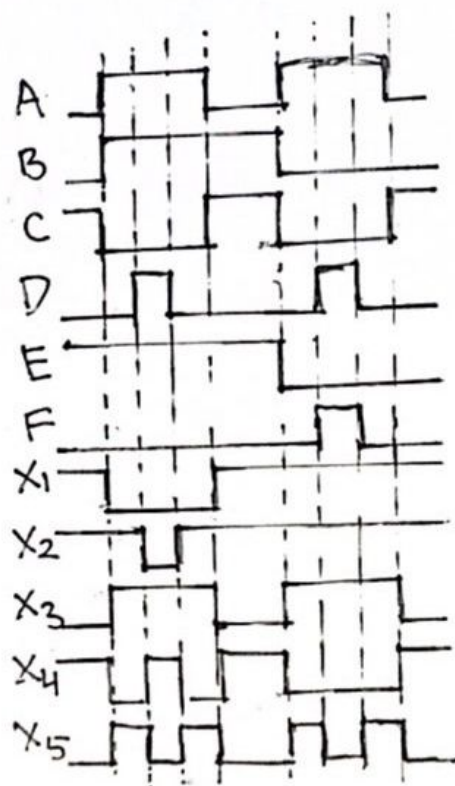
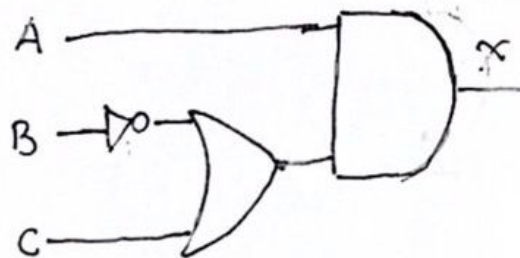
$$7. X_1 = \bar{A} + \bar{B} = \overline{AB}$$

$$X_2 = \bar{D} + \bar{E} = \overline{DE}$$

$$X_3 = \overline{X_1 \cdot C}$$

$$X_4 = \overline{X_3 + X_2} = \overline{X_2 \cdot X_3}$$

$$X_5 = \overline{X_4 + F}$$

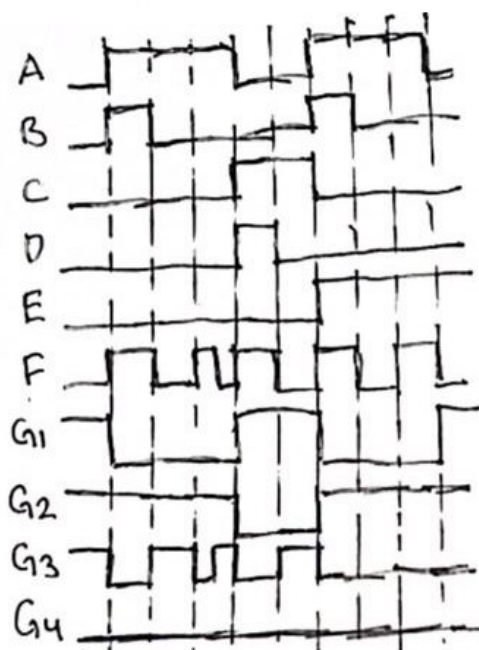


$$9. G_1 = \bar{A}\bar{B} = \overline{(A+B)}$$

$$G_2 = \bar{C}\bar{D} = \overline{(C+D)}$$

$$G_3 = \bar{E}\bar{F} = \overline{(E+F)}$$

$$G_4 = \overline{G_1 + G_2 + G_3}$$



G_4 doesn't match the observed output. By focusing on the intermediate output, it can be found that G_2 is faulty. We can make G_2 gate Low so that when output is high, gate will give faulty output, undershorted.