Ch 10.3: Convolutional Neural Nets

Lecture 32 - CMSE 381

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Dept of Computational Mathematics, Science & Engineering

Weds, Dec 6, 2022

Announcements

Last time:

- Multilayer
- pyTorch

This lecture:

CNNs

Announcements:

Project due Friday

Section 1

Last time: Neural Nets

MNIST

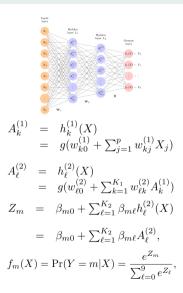
0123456789 0123456789 0123456789





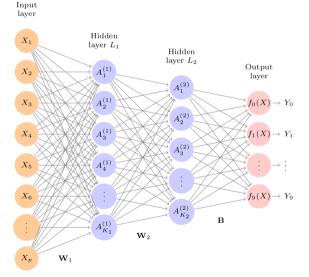


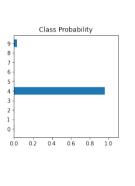
Neural network architecture for MNIST



MNIST learning







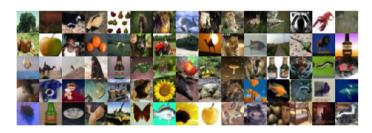
Section 2

Convolutional Neural Network

Last time: Flattening the image

$$\begin{pmatrix} 1 & 1 & 0 \\ 4 & 2 & 1 \\ 0 & 2 & 1 \end{pmatrix} \longrightarrow \begin{pmatrix} 1 \\ 1 \\ 0 \\ 4 \\ 2 \\ 1 \\ 0 \\ 2 \\ 1 \end{pmatrix}$$

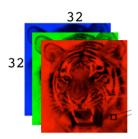
Example data set: CIFAR100 Data



- 60,000 images: 50K training, 10K test
- Labels with 20 super classes (e.g. aquatic mammals)
- 5 classes per super class (beaver, dolphin, otter, seal, whale)
- Images are 32x32

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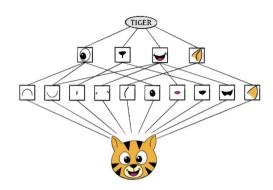
Image channel data



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Convolution layer

Convolution Filter

Original Image:

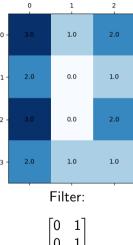
Convolution filter:

$$\begin{bmatrix} \alpha & \beta \\ \gamma & \delta \end{bmatrix}$$

Convolved Image

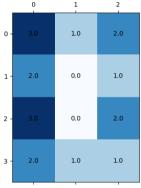
$$\begin{bmatrix} a\alpha + b\beta + d\gamma + e\delta & b\alpha + c\beta + e\gamma + f\delta \\ d\alpha + e\beta + g\gamma + h\delta & e\alpha + f\beta + h\gamma + i\delta \\ g\alpha + h\beta + j\gamma + k\delta & h\alpha + i\beta + k\gamma + l\delta \end{bmatrix}$$

Convolution Filter Example



Same example, different filter

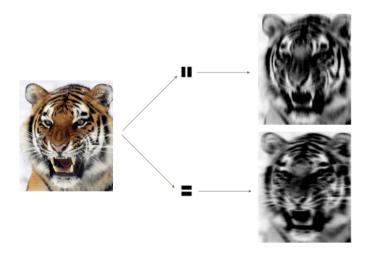
What is the convolved image?



Filter:

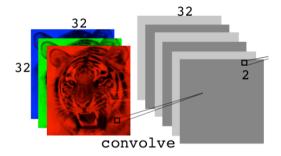
 $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$

Convolution filter: Bigger example



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Convolution layer



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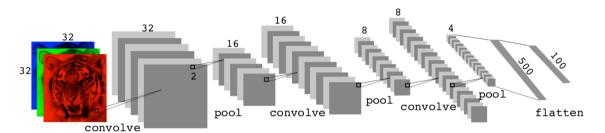
More notes on convolution

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Pooling layers

Max pool
$$\begin{bmatrix} 1 & 2 & 5 & 3 \\ 3 & 0 & 1 & 2 \\ 2 & 1 & 3 & 4 \\ 1 & 1 & 2 & 0 \end{bmatrix} \rightarrow \begin{bmatrix} 3 & 5 \\ 2 & 4 \end{bmatrix}$$

Putting it together to make a CNN



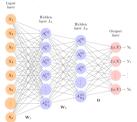
https://poloclub.github.io/cnn-explainer/

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Coding

TL;DR

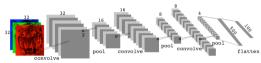
Feed Forward Neural Net



$$A_k = h_k(X) = g(w_{k0} + \sum_{j=1}^p w_{kj}X_j),$$

- Combines input data using learned weights
- Linear combo of those to get output
- Sometimes softmax to get probability of classification

CNN



- Specialized NN
- Gets next layer via
 - Convolution layer
 - Pooling Layer
 - Fully connected layer

Next time

| Lec# | Date | | | Reading | Homeworks |
|------|------|--------|------------------------------------|------------|-------------|
| | Wed | Nov 29 | Midterm #3 | | |
| 32 | Fri | Dec 1 | Multi Layer NN | 10.2 | |
| 33 | Mon | Dec 4 | CNN | 10.3 | |
| 34 | Wed | Dec 6 | Unsupervised Learning & Clustering | 12.1, 12.4 | |
| 35 | Fri | Dec 8 | Virtual: Project office hours | | Project due |