



Decoupled Neural Interfaces using Synthetic Gradients

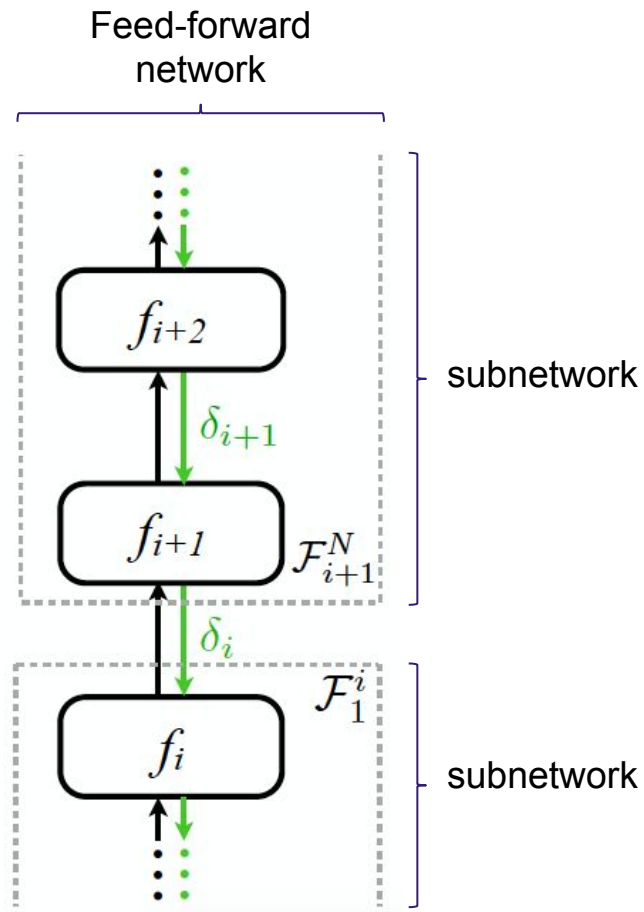
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Locking

- **Locking** - Wait for all dependent computations before parameter update at current module
- **Forward Locking** - Wait for entire forward pass
- **Update Locking** - Wait for forward pass and compute cost function
- **Backwards Locking** - Wait for forward pass and dependent backwards pass



Backpropagation Expanded

$$\frac{\partial L}{\partial \theta_i} = f_{BProp}((h_i, x_i, y_i, \theta_i), (h_{i+1}, x_{i+1}, y_{i+1}, \theta_{i+1}), \dots) \frac{\partial h_i}{\partial \theta_i} \simeq \hat{f}_{BProp}(h_i) \frac{\partial h_i}{\partial \theta_i}$$

- **Goal:** Remove **all locking**
- **Main contribution:** Backward unlocking for infinite time with RNNs
- Expanding BP exposes dependencies
- **Approximate gradient of activations** w.r.t. parameters of **adjacent layers**
(modules depending on how you divide up the computation graph)
- Update **Synthetic Gradient Model** with True Gradients

Synthetic Gradient Model

$$\hat{\delta}_A = M_B(h_A, s_B, c)$$

 $\hat{\delta}_A$

Synthetic gradient **for previous layer/module**

 s_B

Activation of **next layer/module**, which we refer to as module B

 M_B

Synthetic Gradient Model

 c

Context information - additional information such as label information if it's available

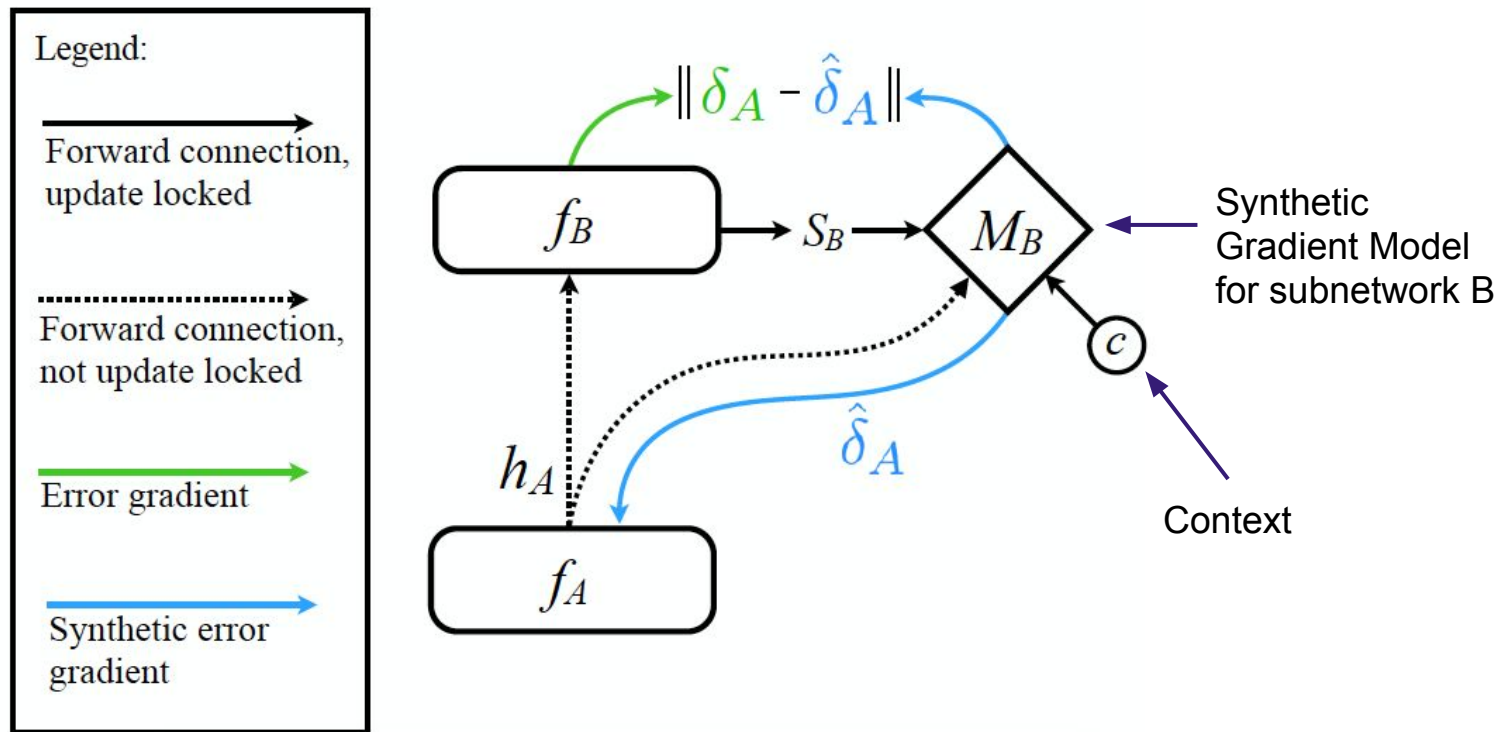
 h_A

Activation of **previous layer/module**, which we refer to as module A

 δ_A

True gradient from backpropagation

Decoupled Neural Interface (DNI)



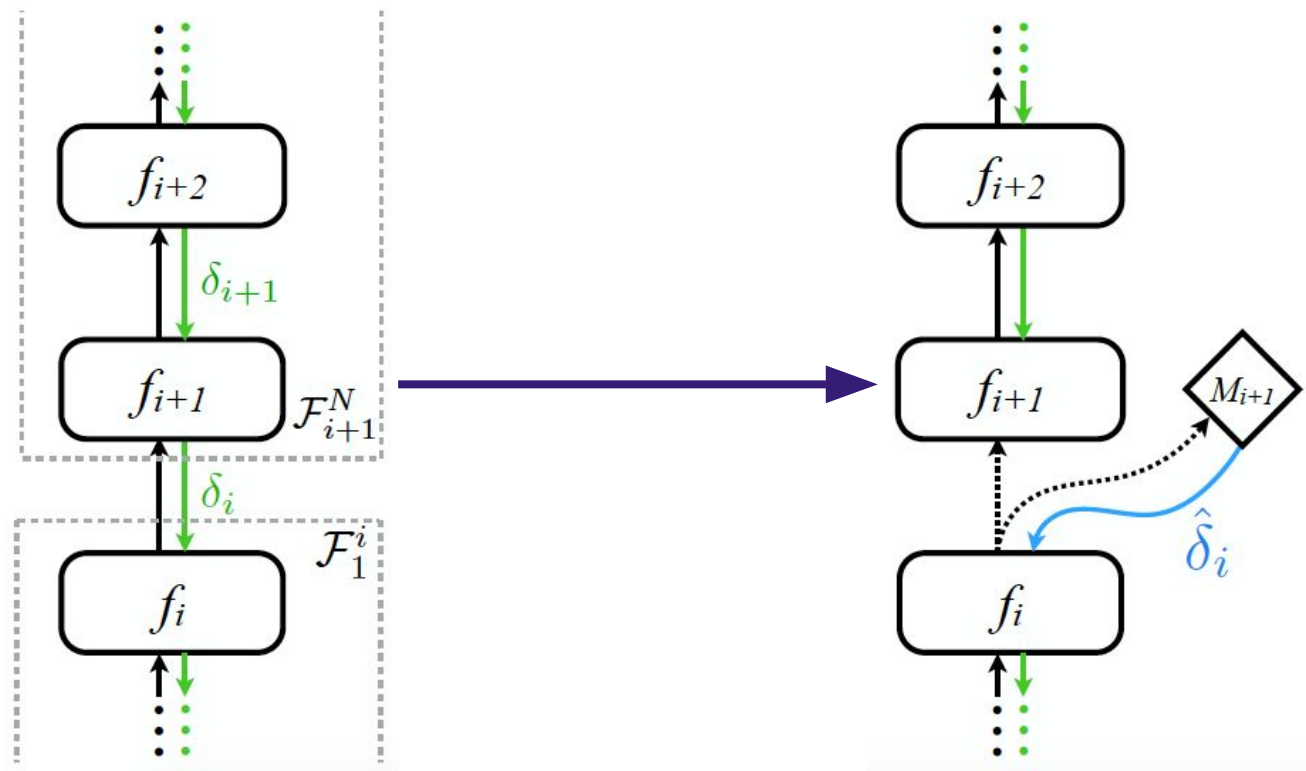
Updating DNI

- DNI are update locked
- Trained to minimize L_2
- Can incorporate context information if available

$$L_{\delta_i} = d(\hat{\delta}_i, \delta_i)$$

$$\hat{\delta}_i = M_{i+1}(h_i, c)$$

Unlocked Subnetworks



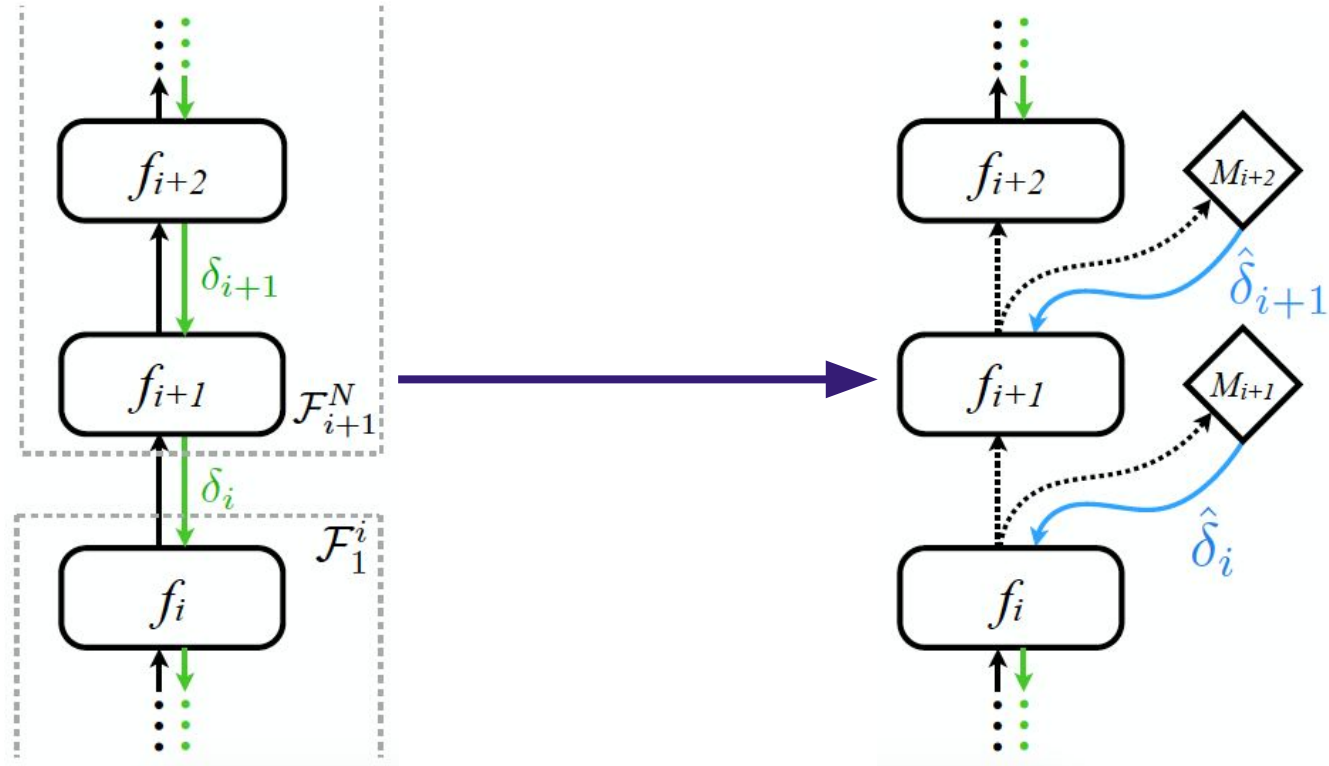
Expanding Backpropagation

$$\theta_i \leftarrow \theta_i - \alpha \delta_i \frac{\partial h_i}{\partial \theta_i}; \delta_i = \frac{\partial L}{\partial h_i}$$

Parameters Learning Rate Local Gradient True Gradient

The diagram illustrates the components of the backpropagation equation. Four purple arrows point from labels below to specific terms in the equation above. The first arrow points from 'Parameters' to the first θ_i . The second arrow points from 'Learning Rate' to α . The third arrow points from 'Local Gradient' to $\frac{\partial h_i}{\partial \theta_i}$. The fourth arrow points from 'True Gradient' to $\frac{\partial L}{\partial h_i}$.

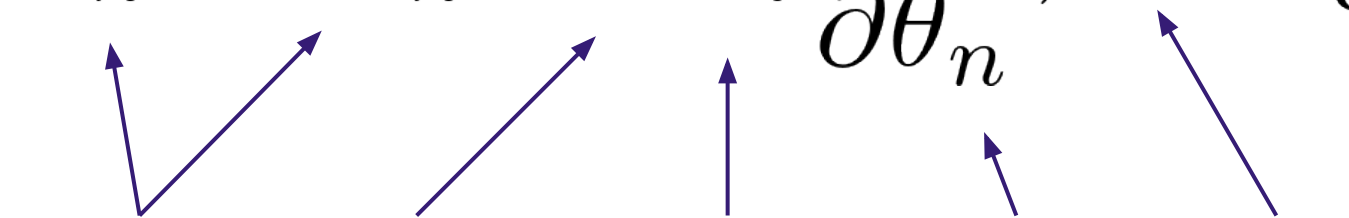
Multiple DNI Feedforward Network



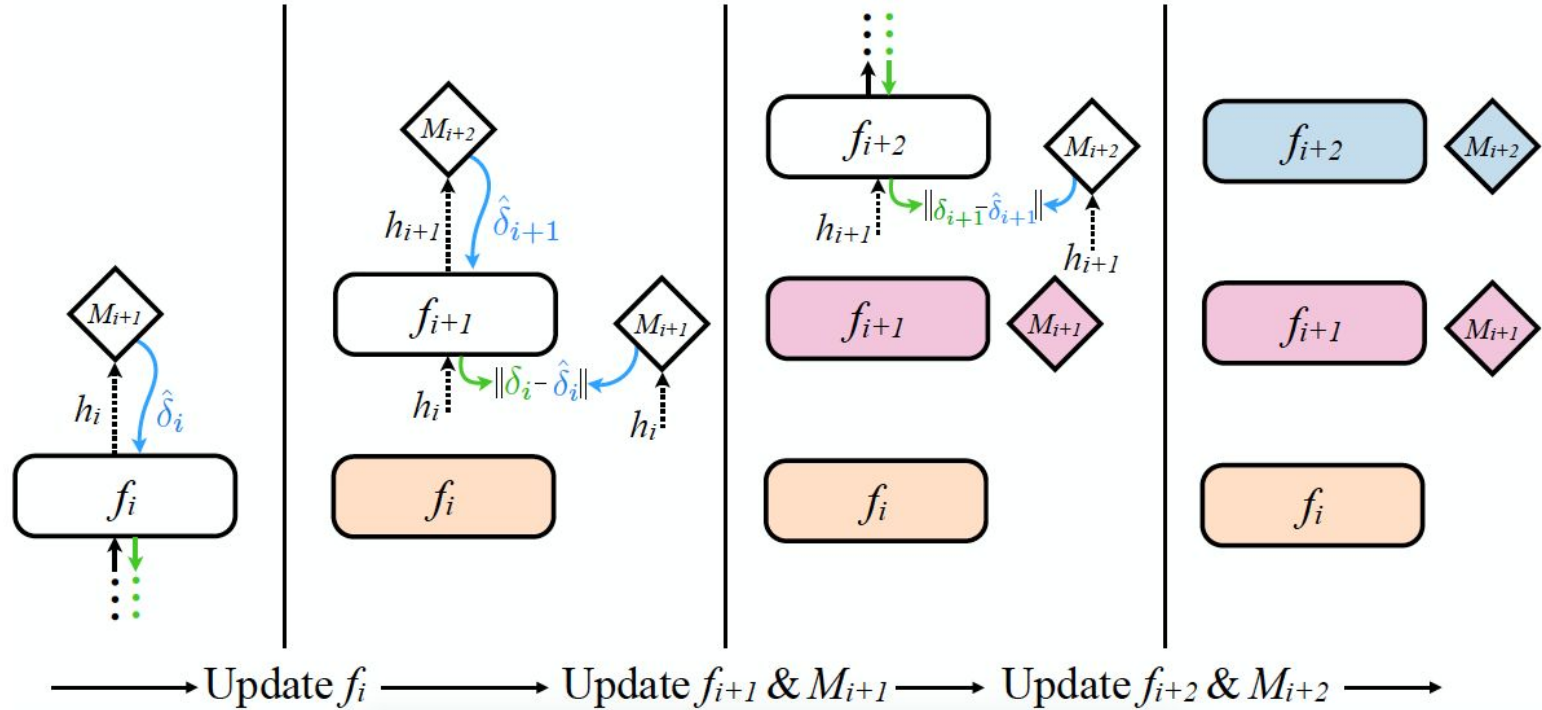
Multiple DNI Update Rule

$$\theta_n \leftarrow \theta_n - \alpha \hat{\delta}_i \frac{\partial h_i}{\partial \theta_n}, n \in \{1, \dots, i\}$$

Parameters Learning Rate Synthetic Gradient Local Gradient Layers



Updating Multiple DNI Feedforward Networks



Expanding BP for RNN

$$\theta - \alpha \sum_{\tau=t}^{\infty} \frac{\partial L_{\tau}}{\partial \theta}$$

Parameters

Learning Rate

Sum over infinite timesteps

Gradient at timestep τ

Expanding BP for RNN

$$= \theta - \alpha \left(\underbrace{\sum_{\tau=t}^{t+T} \frac{\partial L_{\tau}}{\partial \theta}}_{\text{Unroll for only T timesteps}} + \underbrace{\left(\sum_{\tau=T+1}^{\infty} \frac{\partial L_{\tau}}{\partial h_T} \right) \frac{\partial h_T}{\partial \theta}}_{\text{Timesteps after T (future timesteps)}} \right)$$

Expanding BP for RNN

$$= \theta - \alpha \left(\sum_{\tau=t}^{t+T} \frac{\partial L_{\tau}}{\partial \theta} + \underbrace{\delta_T \frac{\partial h_T}{\partial \theta}} \right)$$

- Calculating infinite timesteps is intractable
- Typically ignore timesteps after T by multiplying future gradients by 0

Summation of true gradients over infinite timesteps after timestep T

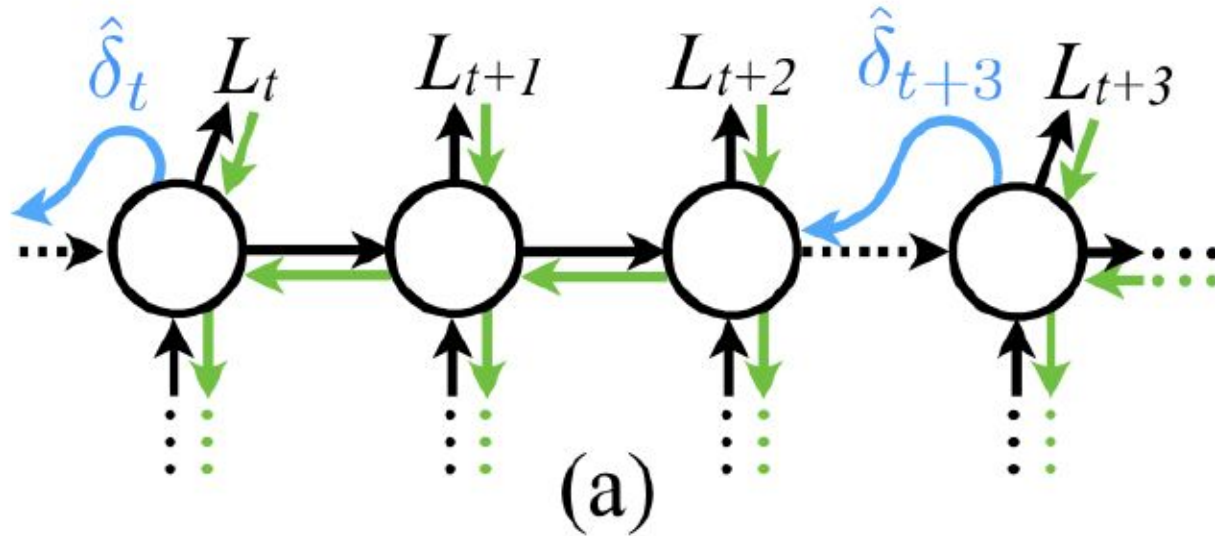
Breaking RNN Time Boundaries

$$\theta \leftarrow \alpha \left(\sum_{\tau=t}^{t+T} \frac{\partial L_{\tau}}{\partial \theta} + \underbrace{\hat{\delta}_T \frac{\partial h_T}{\partial \theta}} \right)$$

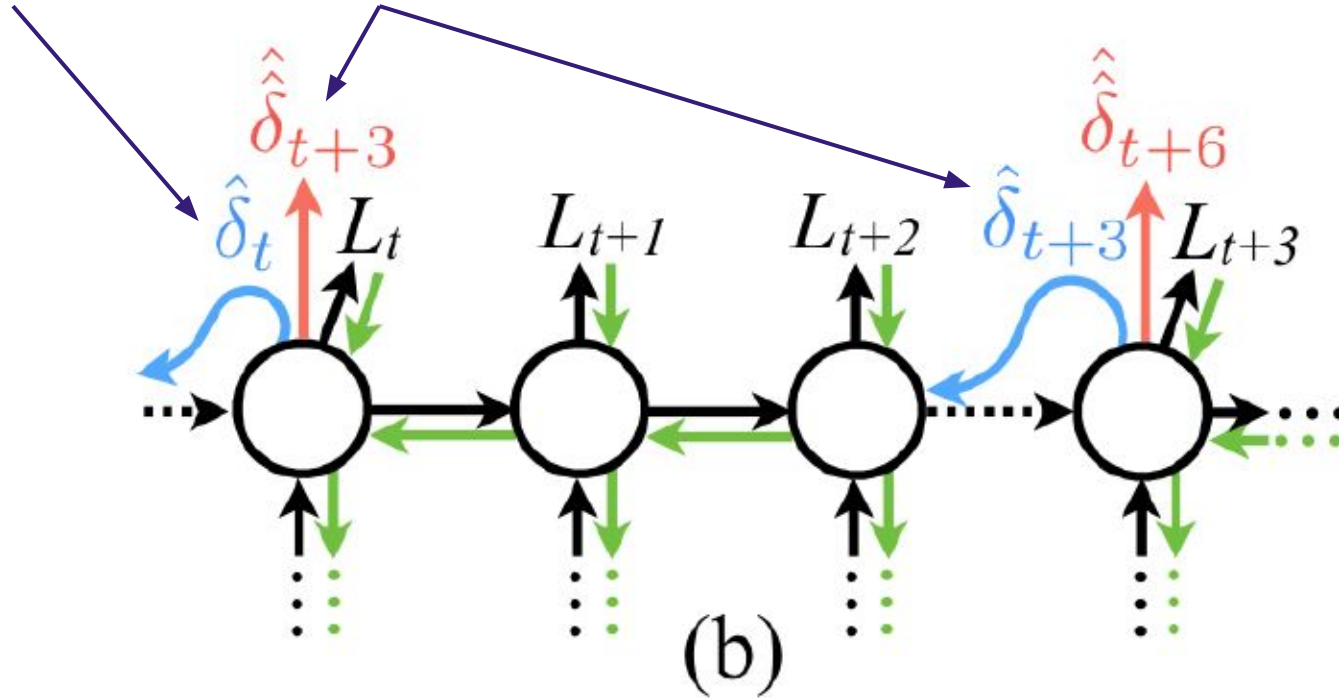
- Equivalent to unrolling for infinite timesteps with infinite subnetworks
- DNI allows RNN to asynchronously communicate with future self

Approximate with DNI

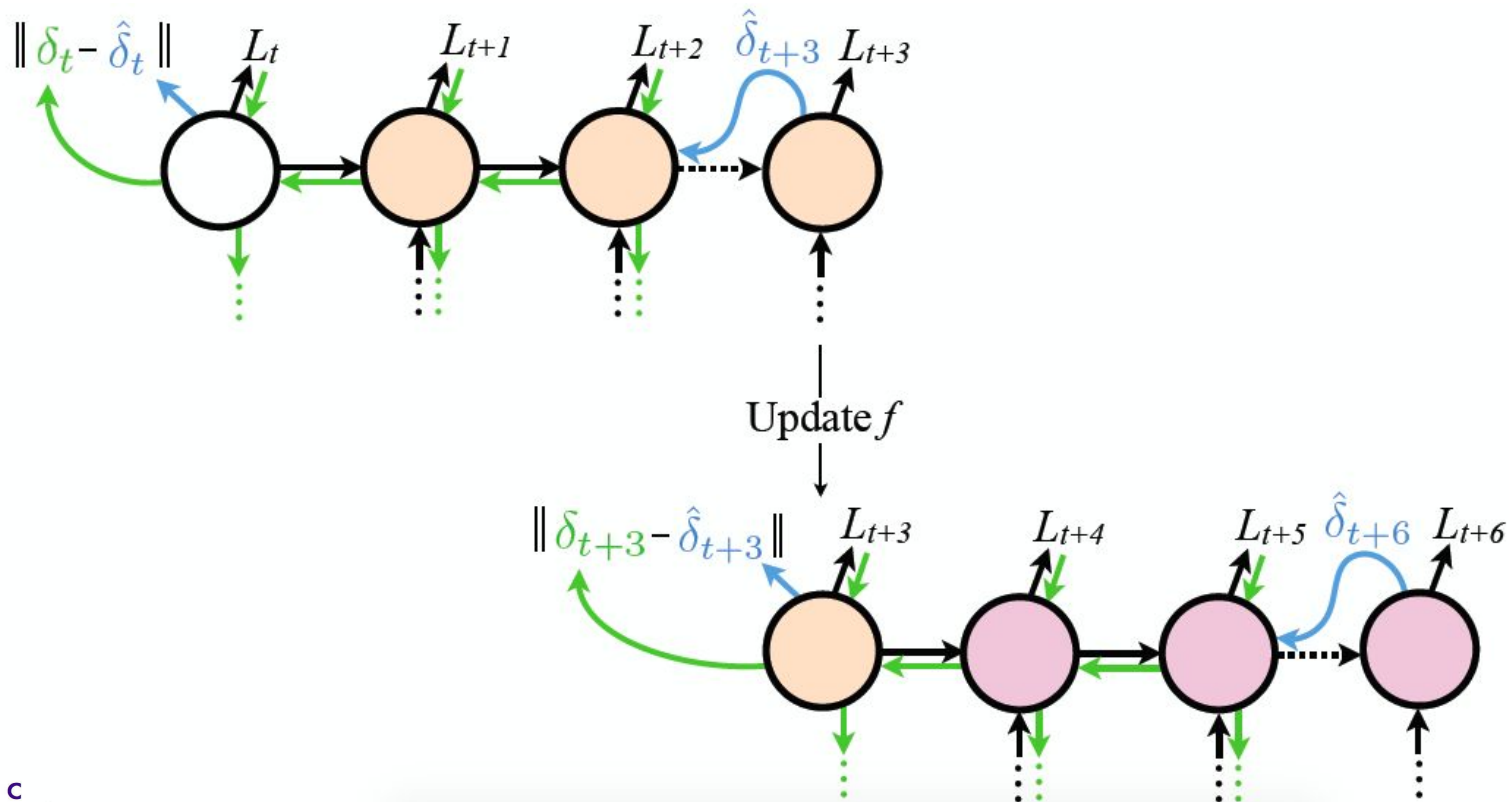
Breaking RNN Time Boundaries



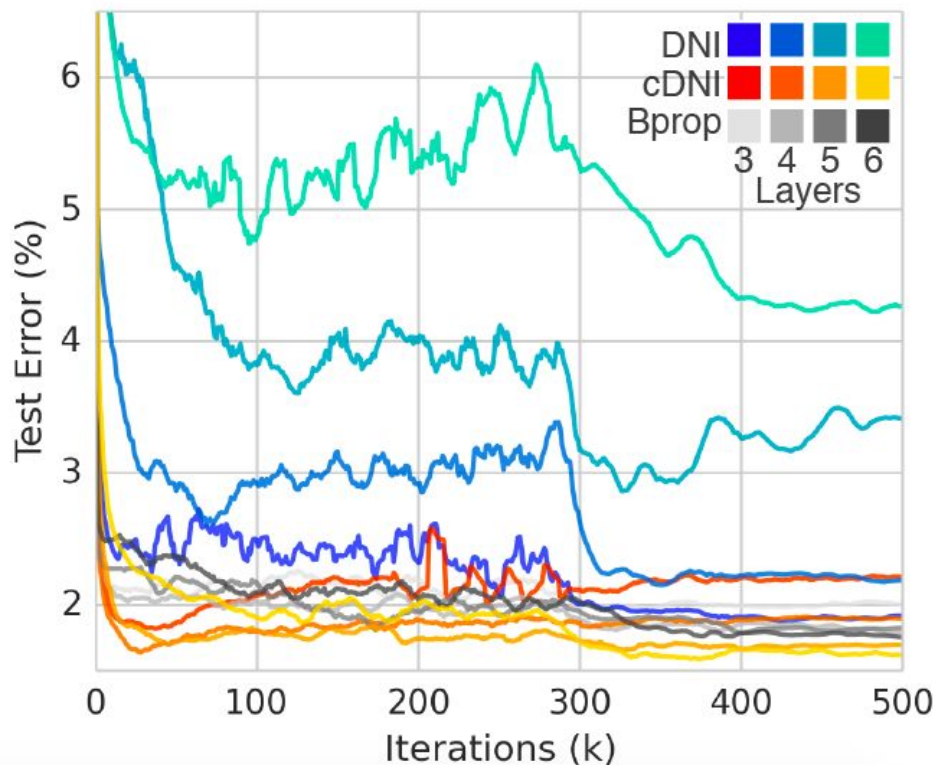
Short-term & Long-term Synthetic Gradients



Updating Multiple DNI Recurrent Networks



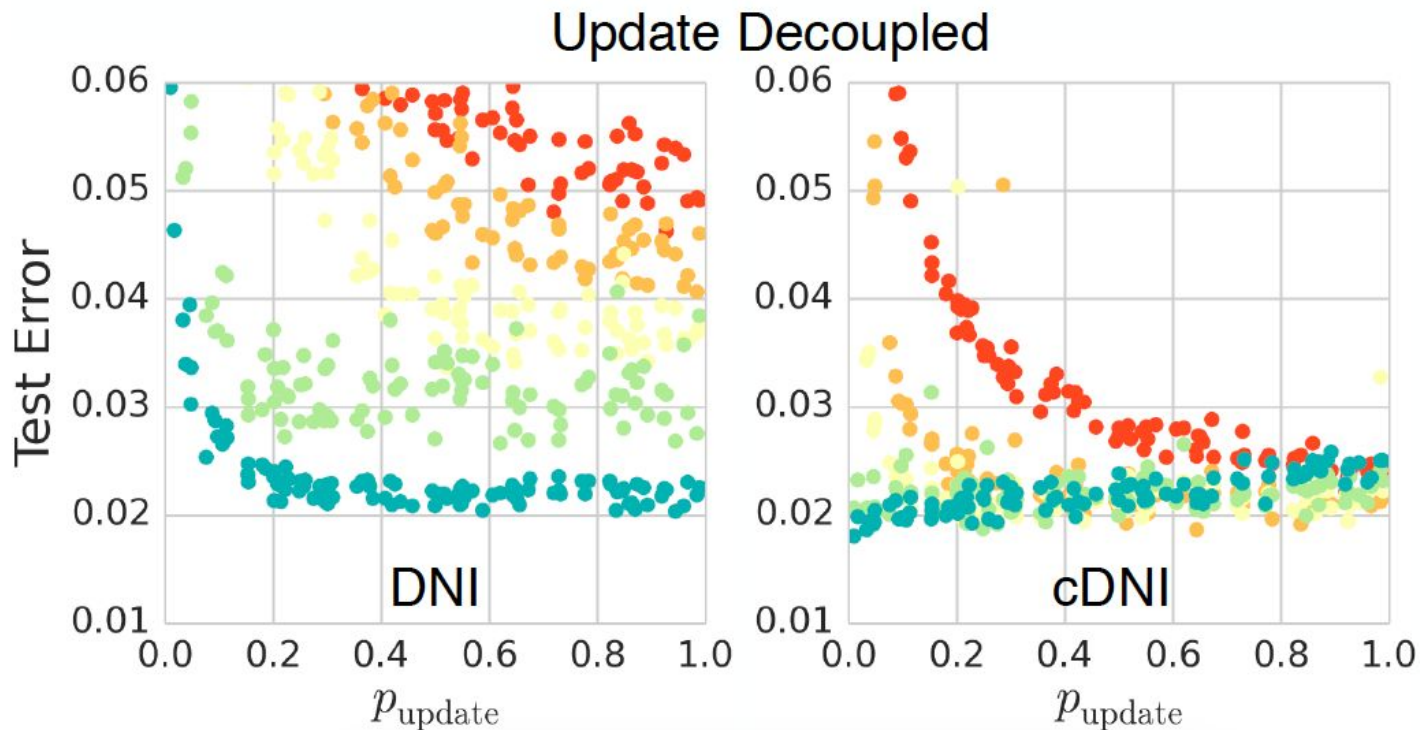
DNI between every layer in FCN



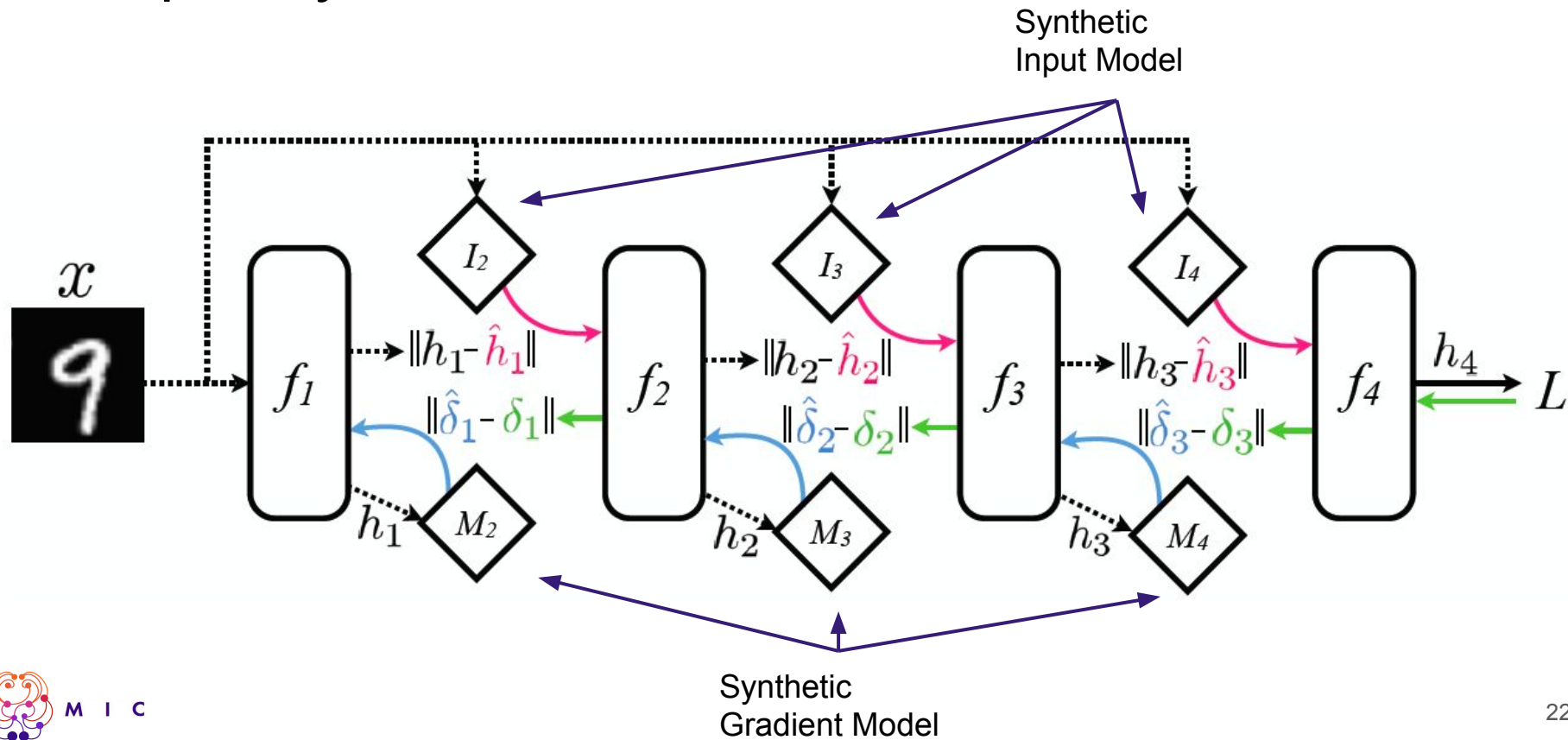
DNI between every layer in FCN and CNN

Layers		MNIST (% Error)				CIFAR-10 (% Error)			
		No Bprop	Bprop	DNI	cDNI	No Bprop	Bprop	DNI	cDNI
FCN	3	9.3	2.0	1.9	2.2	54.9	43.5	42.5	48.5
	4	12.6	1.8	2.2	1.9	57.2	43.0	45.0	45.1
	5	16.2	1.8	3.4	1.7	59.6	41.7	46.9	43.5
	6	21.4	1.8	4.3	1.6	61.9	42.0	49.7	46.8
CNN	3	0.9	0.8	0.9	1.0	28.7	17.9	19.5	19.0
	4	2.8	0.6	0.7	0.8	38.1	15.7	19.5	16.4

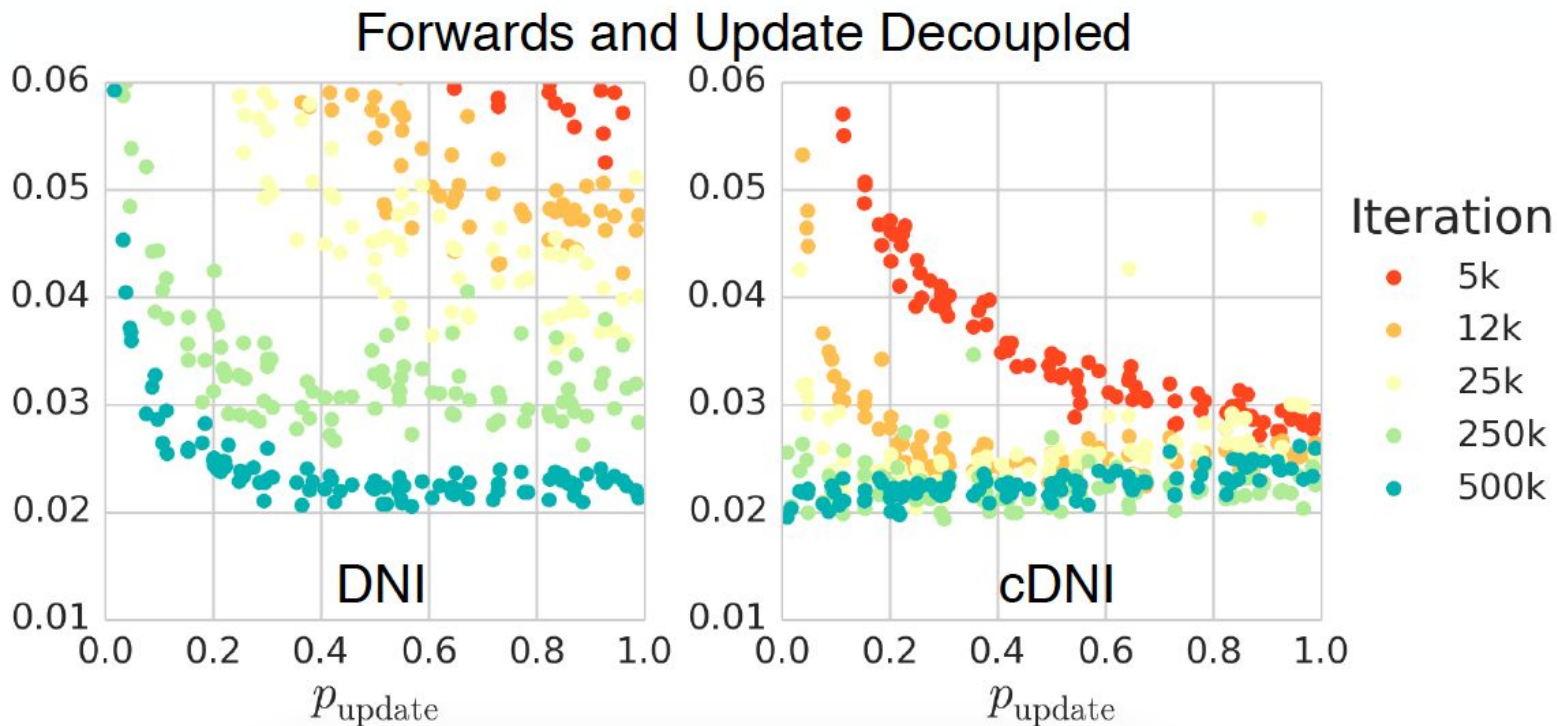
20% Chance Backwards Unlocking



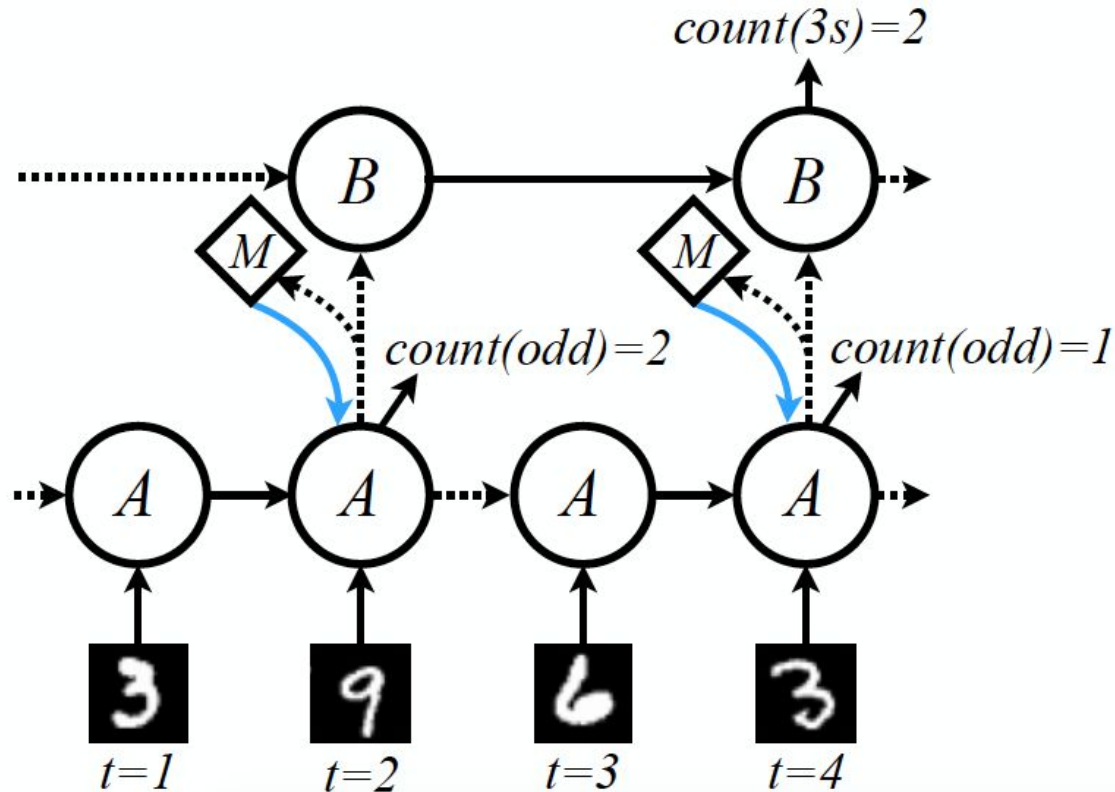
Completely Unlocked Network



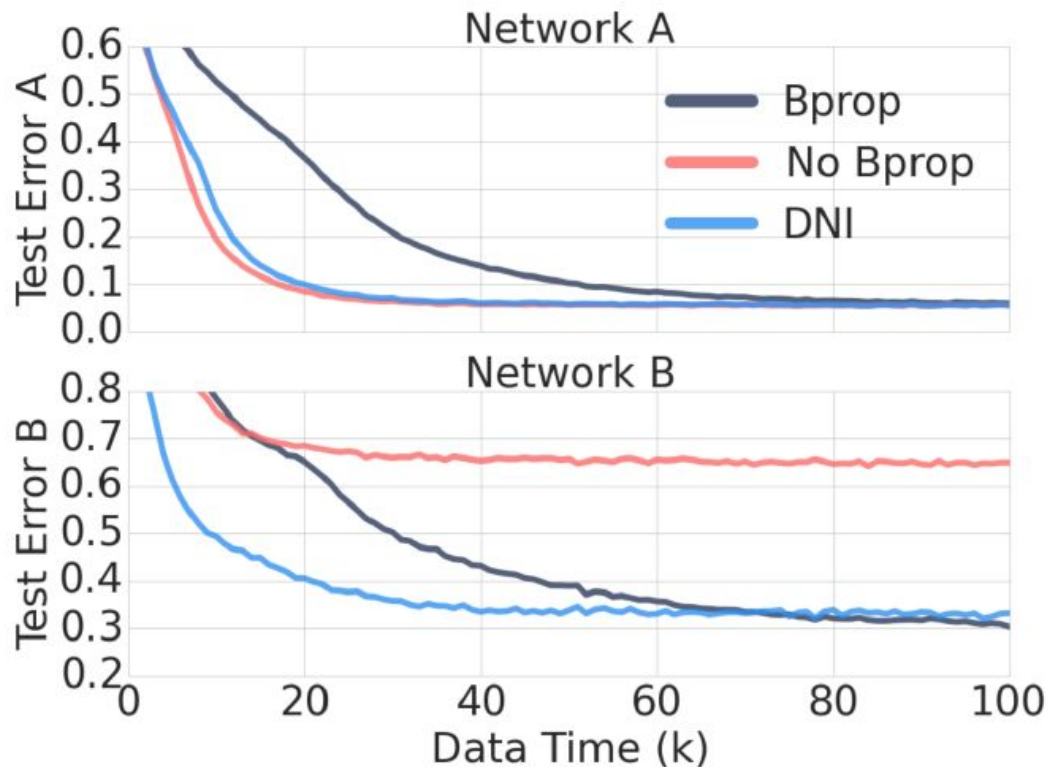
Forwards Unlocking



Dynamic Computation Graphs and Ensembles



Two RNNs communicating with DNI



- One RNN trained to count number of 3s seen
- Second RNN trained to count number odd numbers seen

References and Further Reading

1. Jaderberg, Max, et al. "**Decoupled neural interfaces using synthetic gradients.**" arXiv preprint arXiv:1608.05343 (2016).
2. Czarnecki, Wojciech Marian, et al. "**Understanding Synthetic Gradients and Decoupled Neural Interfaces.**" arXiv preprint arXiv:1703.00522 (2017).
3. Miyato, Takeru, et al. "**Synthetic Gradient Methods with Virtual Forward-Backward Networks.**" (2017).
4. Czarnecki, Wojciech Marian, et al. "**Sobolev Training for Neural Networks.**" arXiv preprint arXiv:1706.04859 (2017).