

PIC 10A 2B

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Today...

- Random Numbers
 - Applications to Loop Exercises
- Functions
- More Loop Exercises
 - Collatz Conjecture

Random Numbers

Syntax, Libraries, and Usage

rand()

<stdlib.h>

- `rand()` generates a (pseudo-) random integer,
 - Between 0 and `RAND_MAX`
 - `RAND_MAX` depends on the library
 - But at least $0x7fff = 2^{15} - 1 = 32767$ on any standard library implementation
 - Using a “seed”
- Using the same seed, `rand()` will generate the same sequence of random numbers
 - More on this later

Using `rand()` – Floating Point numbers

- Since it generates an `int` between 0 and `RAND_MAX`, you can generate a random number between 0 and `X` (inclusive) by

- `rand_num = (rand()*1./RAND_MAX)*X;`

Type
Conversion

Normalized to
0 ~ 1

- Or,

- `rand_num = (static_cast<double>(rand())/RAND_MAX)*X;`

which is preferable

Using `rand()` – Floating Point numbers

- If you want a real number between **A** and **B**,
 - The size of interval = (**B** - **A**)
 - Starts from **A**
- `rand_num = ((rand()*1./RAND_MAX)*(B-A) + A;`



Between 0 and (B-A)

Using `rand()` – Integers

- For integers, we can use the % (mod/remainder) operator
- Random int between 0 and N (inclusive):
 - `n = rand()%(N+1)`
 - The remainder is always between 0 and N
 - Note that, there are **N+1** different integers in [0,N]
- Random int between A and B:
 - = A + (random int between 0 and (B-A))
 - `n = A + rand() % (B-A+1)`

A Seed for `rand()`

- The function `rand()` generates a sequence of random numbers using a seed
- The seed can be set by `srand(some_number);`
- Ex) `some_number == 1` \rightarrow `rand()` gives
 - 41
 - 18467
 - 6334
 - 26500
 - 19169
 - 15724 ...
- Exercise: Use `rand()` several times without `srand()` commands, and verify that you get the sequence above

Seed for `rand()`

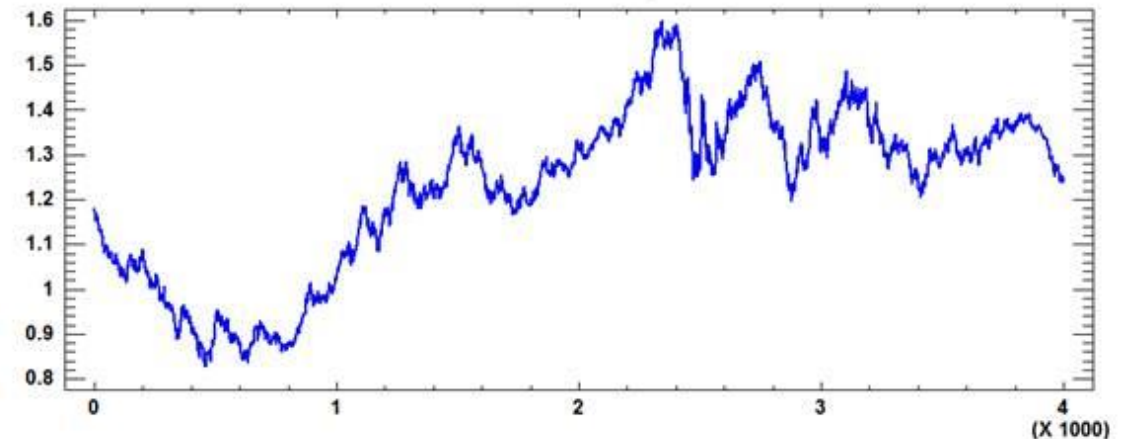
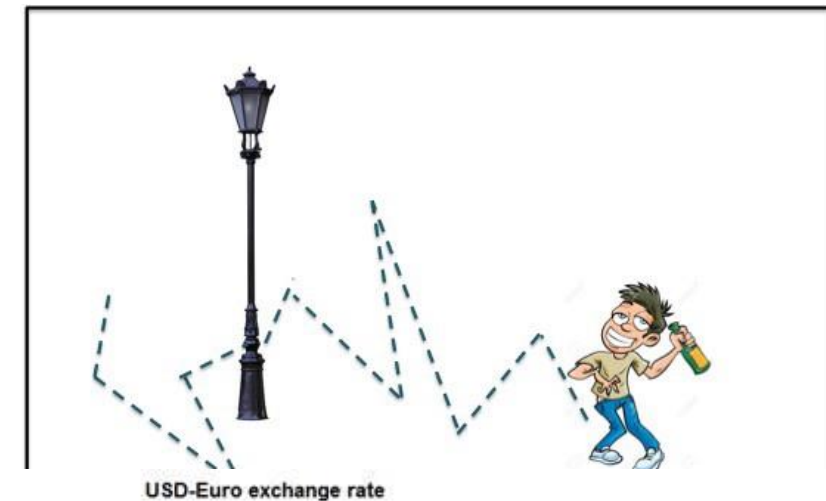
- With the same seed, you'll have the same sequence of random numbers
- So, to get a random-like numbers (pseudo-random numbers), use different seed every time you run the code
- Commonly used trick: use a **current time** as a seed
 - `time(nullptr)` in `<ctime>` library returns the current time in **seconds**, since *00:00, Jan 1 1970 UTC*
 - Ex) `time(nullptr) == 1666067370` when this slide was created

Summary

- `#include <cstdlib>` for `rand()` and `srand()`
- `#include <ctime>` for `time()`
- Use `time(nullptr)` to generate a seed:
 - `srand(time(nullptr));`
 - And then use `rand()`
- Intervals:
 - `r_double = (rand()*1./RAND_MAX)*(B-A) + A;`
 - `r_int = A + rand()%(B-A+1);`

Exercise – Random Walk Simulator

- Suppose someone walks in a constant speed, but chooses the direction randomly in each step
- The path (to be more precise, this *stochastic process*) is called a random walk
- We will simulate a 1-D random walk:
 - An object can only move forward or backward at each step
 - When the object hits the wall (upper/lower bounds), it stops walking
 - The time that it hits the wall is called the “stopping time”
 - Important in mathematical finance



Functions

Basic Syntax and Terminology

Functions

- Functions can be
 - Declared and then defined later
 - If you declare the function first (not define it right now) then need ;
 - Defined when it is declared (so both are done at the same time)
- The declaration determines a “signature” of the function
 - [Return Type] [Function Name] [Input Parameters] (and other options later)



The diagram consists of four colored arrows pointing from the text in the list above to the code snippet below. A red arrow points from '[Return Type]' to 'double'. A blue arrow points from '[Function Name]' to 'find_max'. Two green arrows point from '[Input Parameters]' to 'double a,' and 'double b' respectively.

```
double find_max(double a, double b);
```

Functions

- The declaration determines a “signature” of the function
 - [Return Type] [Function Name] [Input Parameters] (and other options later)

```
double find_max(double a, double b);
```

- Return Type

- The type of the expression returned by the function
- If the function returns nothing, can be `void`

- Function Name

- Name of the function; cannot be a reserved word, the same naming rule applies with variables

- Input Parameters

- The objects passed to the function
- Number of arguments can be 0, 1, or more
- Still need parentheses () even when the function gets zero parameters

Functions – Examples

- A function returning the maximum of two numbers

```
double find_max(double a, double b) {  
    return (a > b) ? a : b;  
}
```

Recall: The ternary operator

A ? **B** : **C**

is (almost) equivalent to

if (**A**) { **B**; }

else { **C**; }

- A **procedure** is a function returning **void**
 - Which means, it doesn't return anything
 - Example: a function printing the max to the console

```
void print_max(double a, double b) {  
    cout << "The max of " << a << " and " << b  
        << " is " << find_max(a, b);  
}
```

Possible if find_max is **declared**
before this expression

Q: [true or false?]

Using “return” keyword in a **procedure** results in a syntax error.

Functions – Examples

- A function that inputs several different types of arguments

```
void func(unsigned int i, string str) {  
    cout << str[i];  
}
```

Here `i` cannot be negative

- A ***predicate*** function is a function returning `bool`
 - The following function checks whether the first letter of the string is capitalized or not

```
bool isCapitalized(string str) {  
    if ('A' <= str[0] && str[0] <= 'Z') {  
        return true;  
    } else {  
        return false;  
    }  
}
```

True if `str[0]` is between 'A' and 'Z' (otherwise it is not a capital letter)

More Loop Exercises

Collatz Conjecture

Exercise – Collatz Conjecture

- Given a positive integer, perform the following operation each step:
 - If the number is even, divide it by two $x \leftarrow x/2$
 - If the number is odd, triple it and add one $x \leftarrow 3x + 1$
- The Collatz conjecture states that you will always reach 1.
- Write a function that computes how many steps it takes to reach 1 starting from a positive integer. The input and output should be:

```
Starting from X.  
Step 1: X  
Step 2: X  
...  
Step X: X  
Starting from X, it took X steps.
```

- Hints
 - Again, the `while` loop will be useful
 - This function is a **procedure**, i.e., it will return `void`




Output example starting from 6

```
Starting from 6  
Step 1: 3  
Step 2: 10  
Step 3: 5  
Step 4: 16  
Step 5: 8  
Step 6: 4  
Step 7: 2  
Step 8: 1  
Starting from 6, it took 8 Steps.
```

Your Feedback is welcome

- Don't hesitate to give a feedback on the discussion
- Use the link on my Github repo, or the link below:
 - <https://forms.gle/erZj1iSgHNrHQuXk6>

My Github repo on the web looks like:

| | |
|---|------------------|
|  code | Week2 Tu |
|  LICENSE | Initial commit |
|  README.md | Update README.md |

README.md

PIC10A

PIC10A discussion 2B, UCLA for Fall 2022

Google form link for feedbacks: <https://forms.gle/erZj1iSgHNrHQuXk6>

 Click this link