

# **TUGAS 5 PRAKTIKUM ANALISIS ALGORITMA**



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**PROGRAM STUDI S-1 TEKNIK INFORMATIKA  
FAKULTAS MATEMATIKA DAN ILMU PENGETAHUAN ALAM  
UNIVERSITAS PADJADJARAN  
2020**

## Studi Kasus 5: Mencari Pasangan Titik Terdekat (Closest Pair of Points)

 Source Code

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```
/* Bunga Azizha N
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Program Program Closest Pair of Points */

#include <bits/stdc++.h>
#include <chrono>

using namespace std;
using namespace std::chrono;

class Point {
public:
    int x, y;
};

int compareX(const void* a, const void* b){
    Point *p1 = (Point *)a, *p2 = (Point *)b;
    return (p1->x - p2->x);
}

int compareY(const void* a, const void* b){
    Point *p1 = (Point *)a, *p2 = (Point *)b;
    return (p1->y - p2->y);
}

float dist(Point p1, Point p2){
    return sqrt( (p1.x - p2.x)*(p1.x - p2.x) + (p1.y - p2.y)*(p1.y - p2.y));
}

float bruteForce(Point P[], int n){
    float min = FLT_MAX;
    for (int i = 0; i < n; ++i)
        for (int j = i+1; j < n; ++j)
            if (dist(P[i], P[j]) < min)
                min = dist(P[i], P[j]);
    return min;
}

float min(float x, float y){
    return (x < y)? x : y;
}
```

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```

float stripClosest(Point strip[], int size, float d){
    float min = d;

    qsort(strip, size, sizeof(Point), compareY);

    for (int i = 0; i < size; ++i)
        for (int j = i+1; j < size && (strip[j].y - strip[i].y) < min; ++j)
            if (dist(strip[i], strip[j]) < min)
                min = dist(strip[i], strip[j]);

    return min;
}

float closestUtil(Point P[], int n){
    if (n <= 3)
        return bruteForce(P, n);

    int mid = n/2;
    Point midPoint = P[mid];

    float dl = closestUtil(P, mid);
    float dr = closestUtil(P + mid, n - mid);
    float d = min(dl, dr);

    Point strip[n];

    int j = 0;
    for (int i = 0; i < n; i++)
        if (abs(P[i].x - midPoint.x) < d)
            strip[j] = P[i], j++;

    return min(d, stripClosest(strip, j, d) );
}

float closest(Point P[], int n){
    qsort(P, n, sizeof(Point), compareX);

    return closestUtil(P, n);
}

int main(){
    high_resolution_clock::time_point t1 = high_resolution_clock::now();
    Point P[] = {{2, 3}, {12, 30}, {40, 50}, {5, 1}, {12, 10}, {3, 4}};
    int n = sizeof(P) / sizeof(P[0]);

```

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```

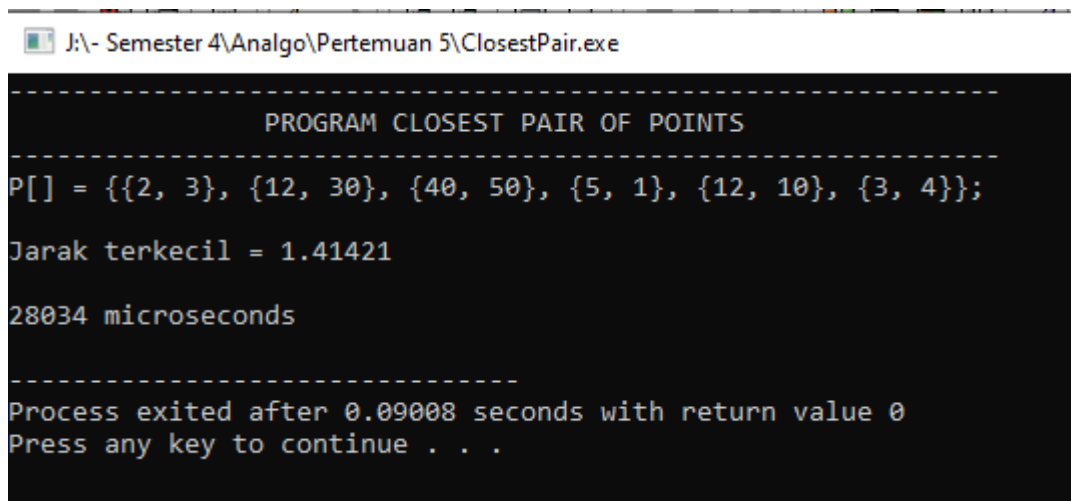
cout<<"-----"<<endl;
cout<<"\t\tPROGRAM CLOSEST PAIR OF POINTS"<<endl;
cout<<"-----"<<endl;
cout<<"P[] = {{2, 3}, {12, 30}, {40, 50}, {5, 1}, {12, 10}, {3, 4}};"<<endl<<endl;
cout<<"Jarak terkecil = "<<closest(P, n);

high_resolution_clock::time_point t2 = high_resolution_clock::now();
auto duration = duration_cast<microseconds>( t2 - t1).count();
cout<<endl<<endl<<duration<<" microseconds" <<endl;
}

```

---

#### Screenshoot Hasil Program



```

J:\- Semester 4\Analgo\Pertemuan 5\ClosestPair.exe

-----
PROGRAM CLOSEST PAIR OF POINTS
-----
P[] = {{2, 3}, {12, 30}, {40, 50}, {5, 1}, {12, 10}, {3, 4}};

Jarak terkecil = 1.41421

28034 microseconds

-----
Process exited after 0.09008 seconds with return value 0
Press any key to continue . . .

```

#### Rekurensi

$$T(n) = 2T(n/2) + O(n) + O(n * \log n) + O(n)$$

$$T(n) = 2T(n/2) + O(n * \log n)$$

$$T(n) = T(n * \log n * \log n)$$

## Studi Kasus 6: Algoritma Karatsuba untuk Perkalian Cepat

### Source Code

---

```
/* Bunga Azizha N
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Program Karatsuba */

#include<iostream>
#include<chrono>
#include<stdio.h>

using namespace std;
using namespace std::chrono;

int makeEqualLength(string &str1, string &str2){
    int len1 = str1.size();
    int len2 = str2.size();
    if (len1 < len2){
        for (int i = 0 ; i < len2 - len1 ; i++){
            str1 = '0' + str1;
        }
        return len2;
    }
    else if (len1 > len2){
        for (int i = 0 ; i < len1 - len2 ; i++){
            str2 = '0' + str2;
        }
        return len1;
    }
}

string addBitStrings( string first, string second ){
    string result;
    int length = makeEqualLength(first, second);
    int carry = 0;

    for (int i = length-1 ; i >= 0 ; i--){
        int firstBit = first.at(i) - '0';
        int secondBit = second.at(i) - '0';
        int sum = (firstBit ^ secondBit ^ carry)+'0';
        result = (char)sum + result;
        carry = (firstBit&secondBit) | (secondBit&carry) | (firstBit&carry);
    }
    if (carry) result = '1' + result;

    return result;
}
```

---

---

```

int multiplySingleBit(string a, string b){
    return (a[0] - '0')*(b[0] - '0');
}

long int multiply(string X, string Y){
    int n = makeEqualLength(X, Y);

    if (n == 0) return 0;
    if (n == 1) return multiplySingleBit(X, Y);

    int fh = n/2;
    int sh = (n-fh);

    string Xl = X.substr(0, fh);
    string Xr = X.substr(fh, sh);
    string Yl = Y.substr(0, fh);
    string Yr = Y.substr(fh, sh);

    long int P1 = multiply(Xl, Yl);
    long int P2 = multiply(Xr, Yr);
    long int P3 = multiply(addBitStrings(Xl, Xr), addBitStrings(Yl, Yr));

    return P1*(1<<(2*sh)) + (P3 - P1 - P2)*(1<<sh) + P2;
}

int main(){
    high_resolution_clock::time_point t1 = high_resolution_clock::now();

    cout<<"-----"<<endl;
    cout<<"\tPROGRAM KARATSUBA"<<endl;
    cout<<"-----"<<endl;
    cout<<"String 1: 1100, String 2: 1010"<<endl;
    cout<<"String 1: 11, String 2: 11"<<endl;
    cout<<"\nHasil kali: "<<multiply("1100", "1010");
    cout<<"\nHasil kali: "<<multiply("11", "11");

    high_resolution_clock::time_point t2 = high_resolution_clock::now();
    auto duration = duration_cast<microseconds>( t2 - t1 ).count();
    cout<<endl<<endl<<duration<<" microseconds" <<endl;
}

```

---

#### Screenshot Hasil Program

```

-----
PROGRAM KARATSUBA
-----
String 1: 1100, String 2: 1010
String 1: 11, String 2: 11

Hasil kali: 120
Hasil kali: 9

4003 microseconds
-----

```

## Rekurensi

- Let's try divide and conquer.
  - Divide each number into two halves.
    - $x = x_H r^{n/2} + x_L$
    - $y = y_H r^{n/2} + y_L$
  - Then:
$$xy = (x_H r^{n/2} + x_L) y_H r^{n/2} + y_L$$
$$= x_H y_H r^n + (x_H y_L + x_L y_H) r^{n/2} + x_L y_L$$
  - Runtime?
    - $T(n) = 4 T(n/2) + O(n)$
    - $T(n) = O(n^2)$
- Instead of 4 subproblems, we only need 3 (with the help of clever insight).
- Three subproblems:
  - $a = x_H y_H$
  - $d = x_L y_L$
  - $e = (x_H + x_L) (y_H + y_L) - a - d$
- Then  $xy = a r^n + e r^{n/2} + d$
- $T(n) = 3 T(n/2) + O(n)$
- $T(n) = O(n^{\log_2 3}) = O(n^{1.584...})$

## Studi Kasus 7: Permasalahan Tata Letak Keramik Lantai (Tiling Problem)

### Source Code

---

```
/* Bunga Azizha N
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Program Tiling */

#include <iostream>
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
using namespace std;

int board[1000][1000];
int no = 0;
int quadrant = 0;

void trominoTile(int xBoard,
                 int yBoard,
                 int x_hole,
                 int y_hole,
                 int boardSize);

void trominoTile(int xBoard, int yBoard, int x_hole, int y_hole, int boardSize){
```

---

---

```

int halfSize = boardSize / 2,
    xCenter = 0,
    yCenter = 0;

xCenter = xBoard + halfSize - 1;
yCenter = yBoard + halfSize - 1;

if (boardSize == 2){
    if (board[xBoard][yBoard + 1] == 0 && board[xBoard + 1][yBoard] == 0 &&
board[xBoard + 1][yBoard + 1] == 0){
        no++;
        board[xBoard][yBoard + 1] = no;
        board[xBoard + 1][yBoard] = no;
        board[xBoard + 1][yBoard + 1] = no;
    }

    if (board[xBoard][yBoard] == 0 && board[xBoard + 1][yBoard] == 0 &&
board[xBoard + 1][yBoard + 1] == 0){
        no++;
        board[xBoard][yBoard] = no;
        board[xBoard + 1][yBoard] = no;
        board[xBoard + 1][yBoard + 1] = no;
    }

    if (board[xBoard][yBoard + 1] == 0 && board[xBoard][yBoard] == 0 &&
board[xBoard + 1][yBoard + 1] == 0){
        no++;
        board[xBoard + 1][yBoard + 1] = no;
        board[xBoard][yBoard + 1] = no;
        board[xBoard][yBoard] = no;
    }

    if (board[xBoard][yBoard + 1] == 0 && board[xBoard + 1][yBoard] == 0 &&
board[xBoard][yBoard] == 0){
        no++;
        board[xBoard][yBoard] = no;
        board[xBoard][yBoard + 1] = no;
        board[xBoard + 1][yBoard] = no;
    }

    return;
}

if (x_hole <= xCenter){
    if (y_hole <= yCenter){

```

---



---

```
        if (board[xCenter][yCenter + 1] == 0 && board[xCenter + 1][yCenter] == 0 &&
board[xCenter + 1][yCenter + 1] == 0){
            no++;
            board[xCenter][yCenter + 1] = no;
            board[xCenter + 1][yCenter] = no;
            board[xCenter + 1][yCenter + 1] = no;
            quadrant = 1;
        }
    }
    else{
        if (board[xCenter][yCenter] == 0 && board[xCenter + 1][yCenter] == 0 &&
board[xCenter + 1][yCenter + 1] == 0){
            no++;
            board[xCenter][yCenter] = no;
            board[xCenter + 1][yCenter + 1] = no;
            board[xCenter + 1][yCenter] = no;
            quadrant = 2;
        }
    }
}
else{
    if (y_hole <= yCenter){
        if (board[xCenter][yCenter + 1] == 0 && board[xCenter][yCenter] == 0 &&
board[xCenter + 1][yCenter + 1] == 0){
            no++;
            board[xCenter][yCenter] = no;
            board[xCenter][yCenter + 1] = no;
            board[xCenter + 1][yCenter + 1] = no;
            quadrant = 3;
        }
    }
    else{
        if (board[xCenter + 1][yCenter] == 0 && board[xCenter][yCenter] == 0 &&
board[xCenter][yCenter + 1] == 0){
            no++;
            board[xCenter][yCenter] = no;
            board[xCenter][yCenter + 1] = no;
            board[xCenter + 1][yCenter] = no;
            quadrant = 4;
        }
    }
}
}

if (quadrant == 1){
```

---

---

```
trominoTile(xBoard, yBoard, x_hole, y_hole, halfSize);
trominoTile(xBoard, yCenter + 1, xCenter, yCenter + 1, halfSize);
trominoTile(xCenter + 1, yBoard, xCenter + 1, yCenter, halfSize);
trominoTile(xCenter + 1, yCenter + 1, xCenter + 1, yCenter + 1,
            halfSize);
}

if (quadrant == 2){
    trominoTile(xBoard, yBoard, xCenter, yCenter, halfSize);
    trominoTile(xBoard, yCenter + 1, x_hole, y_hole, halfSize);
    trominoTile(xCenter + 1, yBoard, xCenter + 1, yCenter, halfSize);
    trominoTile(xCenter + 1, yCenter + 1, xCenter + 1, yCenter + 1,
                halfSize);
}

if (quadrant == 3){
    trominoTile(xBoard, yBoard, xCenter, yCenter, halfSize);
    trominoTile(xBoard, yCenter + 1, xCenter, yCenter + 1, halfSize);
    trominoTile(xCenter + 1, yBoard, x_hole, y_hole, halfSize);
    trominoTile(xCenter + 1, yCenter + 1, xCenter + 1, yCenter + 1,
                halfSize);
}

if (quadrant == 4){
    trominoTile(xBoard, yBoard, xCenter, yCenter, halfSize);
    trominoTile(xBoard, yCenter + 1, xCenter, yCenter + 1, halfSize);
    trominoTile(xCenter + 1, yBoard, xCenter + 1, yCenter, halfSize);
    trominoTile(xCenter + 1, yCenter + 1, x_hole, y_hole, halfSize);
}
}

int main(){
    int boardSize, x_hole, y_hole;
    do{
        printf("\n-----");
        printf("\nEnter size of board (0 to quit): ");
        scanf("%d", &boardSize);
        if (boardSize){
            printf("\nEnter coordinates of missing hole: ");
            scanf("%d%d", &x_hole, &y_hole);
            for (int i = 1; i <= pow(2, boardSize); i++){
                for (int j = 1; j <= pow(2, boardSize); j++){
                    board[i][j] = 0;
                }
            }
        }
    }
```

---

---

```

    board[x_hole][y_hole] = -1;

    trominoTile(1, 1, x_hole, y_hole, pow(2, boardSize));

    for (int i = 1; i <= pow(2, boardSize); i++){
        for (int j = 1; j <= pow(2, boardSize); j++){
            if (i == x_hole && j == y_hole){
                board[i][j] == -1;
                printf("%4s", "X");
            }
            else{
                printf("%4d", board[i][j]);
            }
        }cout << endl;
    }
    }no = 0;
}

while (boardSize);

return EXIT_SUCCESS;
}

```

---

## Rekurensi

Relasi perulangan untuk algoritma rekursif di atas dapat ditulis seperti di bawah ini. C adalah konstanta.

$$T(n) = 4T(n/2) + C$$

Rekursi di atas dapat diselesaikan dengan menggunakan Metode Master dan kompleksitas waktu adalah  $O(n^2)$

$$T(n) = 4T(n/2) + C$$

$$a = 4, b = 2, f(n) = 1$$

$$n \log_b a = n \log_2 4 = n^2$$

$$f(n) = 1 = O(n \log_2 4 - \epsilon) \text{ untuk } \epsilon = 1$$

Case 1 applies

Maka, solusinya adalah

$$T(n) = O(n \log_b a) = O(n \log_2 4) = O(n^2)$$