

Module E: Motion Planning

Part 1. Introduction to Motion Planning

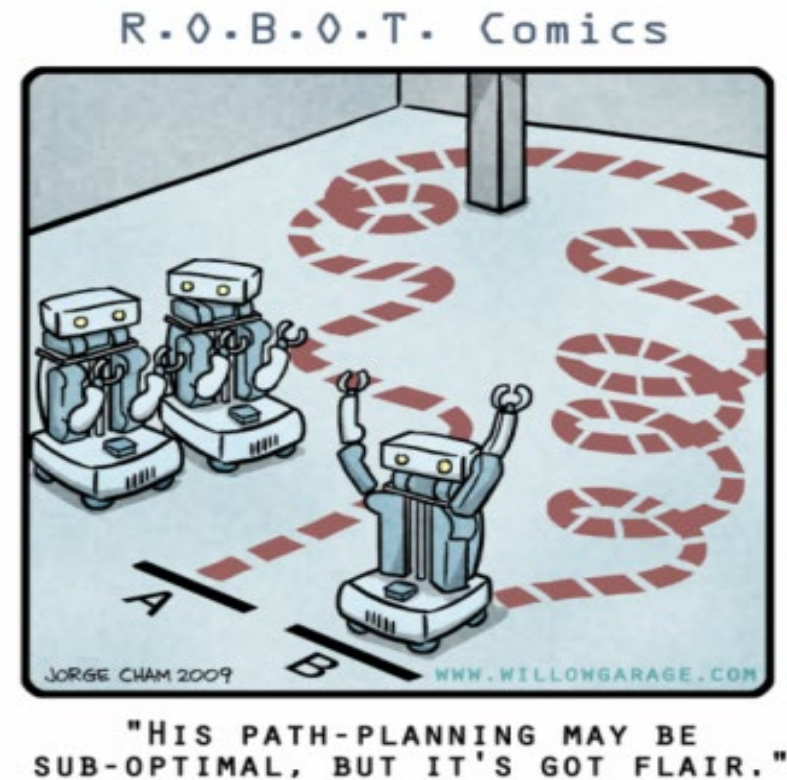
Part 2: Dijkstra and A* algorithm

Part 3. RRT and RRT*

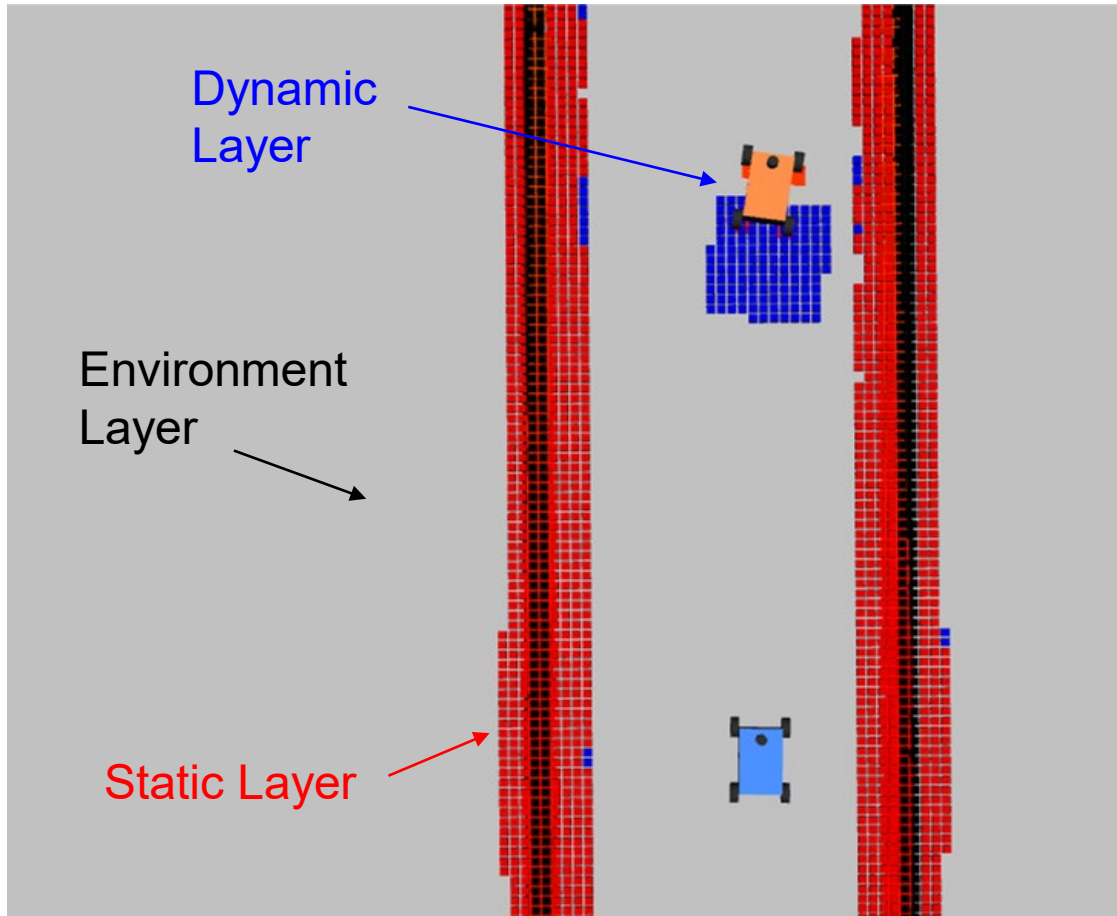
References:

<https://f1tenth.org> and UPenn ESE 680 Slides

<http://www.willowgarage.com/pages/research/motion-planning>



The Motion Planning Problem



From Upenn ESE 680 Slides

□ Path planning:

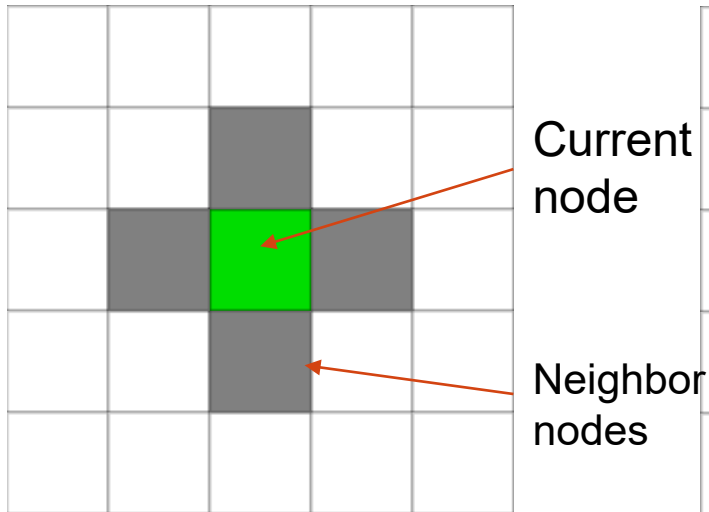
- ❖ Find a path to go from a starting point to a destination and avoid obstacles;
- ❖ May need to set a goal dynamically in race if multiple cars are on the race track;
- ❖ If possible, minimize the cost of the path
- ❖ Can be divided into local or global path planning

□ Performance metrics:

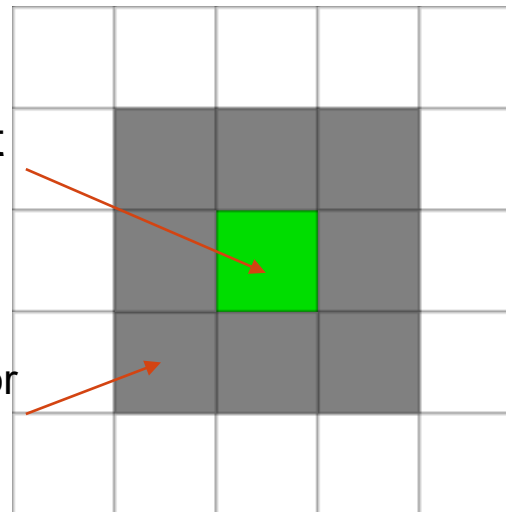
- ❖ Completeness: the algo terminates in finite time; returns a solution when one exists and failure otherwise;
- ❖ Optimality: returns the minimum cost solution when a solution exists.
- ❖ Complexity: time and memory space

Occupancy Grid or Graph

4-Connected



8-Connected

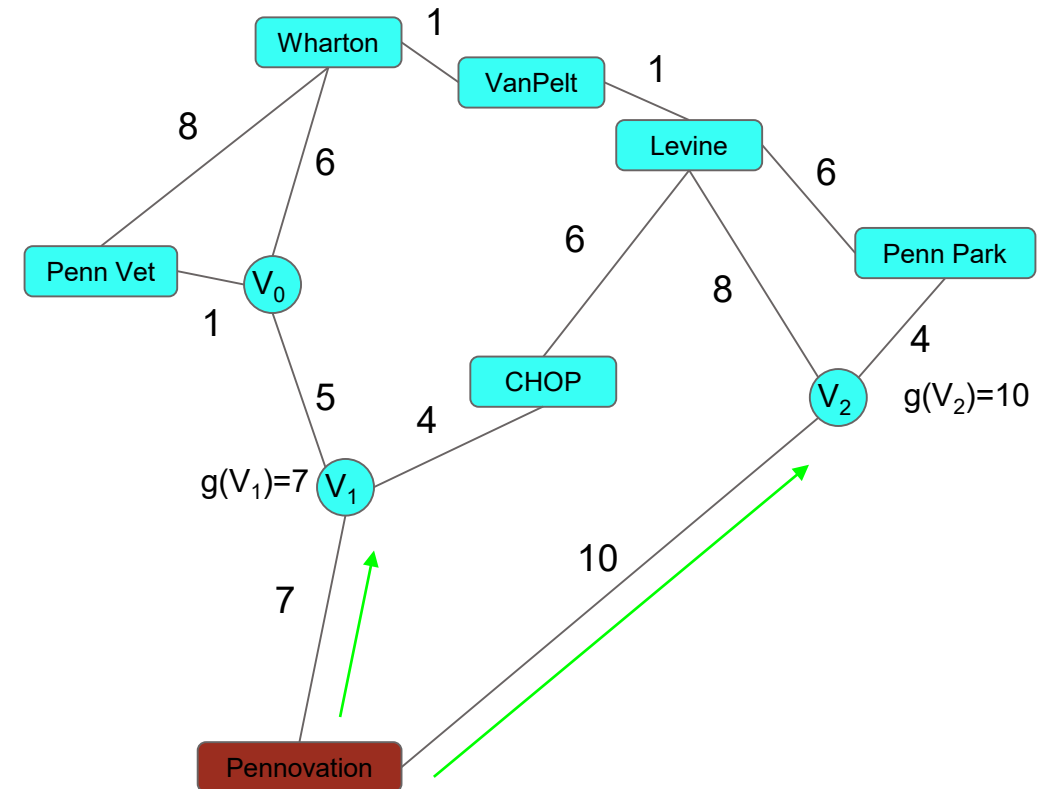


❖ Blind Search algorithm:

- ❖ Breadth First Search (BFS)
- ❖ Depth First Search (DFS)

❖ Informed Search algorithm:

- ❖ Heuristic Search: Dijkstra, D*, A*;
- ❖ Sampling based search: PRM, RRT, RRT*



A* Search Algorithms

| | | | | | | | |
|-------|----|----|----|----|----|----|------|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | GOAL |
| 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 |
| 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 |
| 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 |
| START | 41 | 42 | 43 | 44 | 45 | 46 | 47 |

❖ The cost of a node v :

$$f(v) = g(v) + h(v)$$

$h(v)$ is a heuristic that underestimates the cost to reach the goal from v

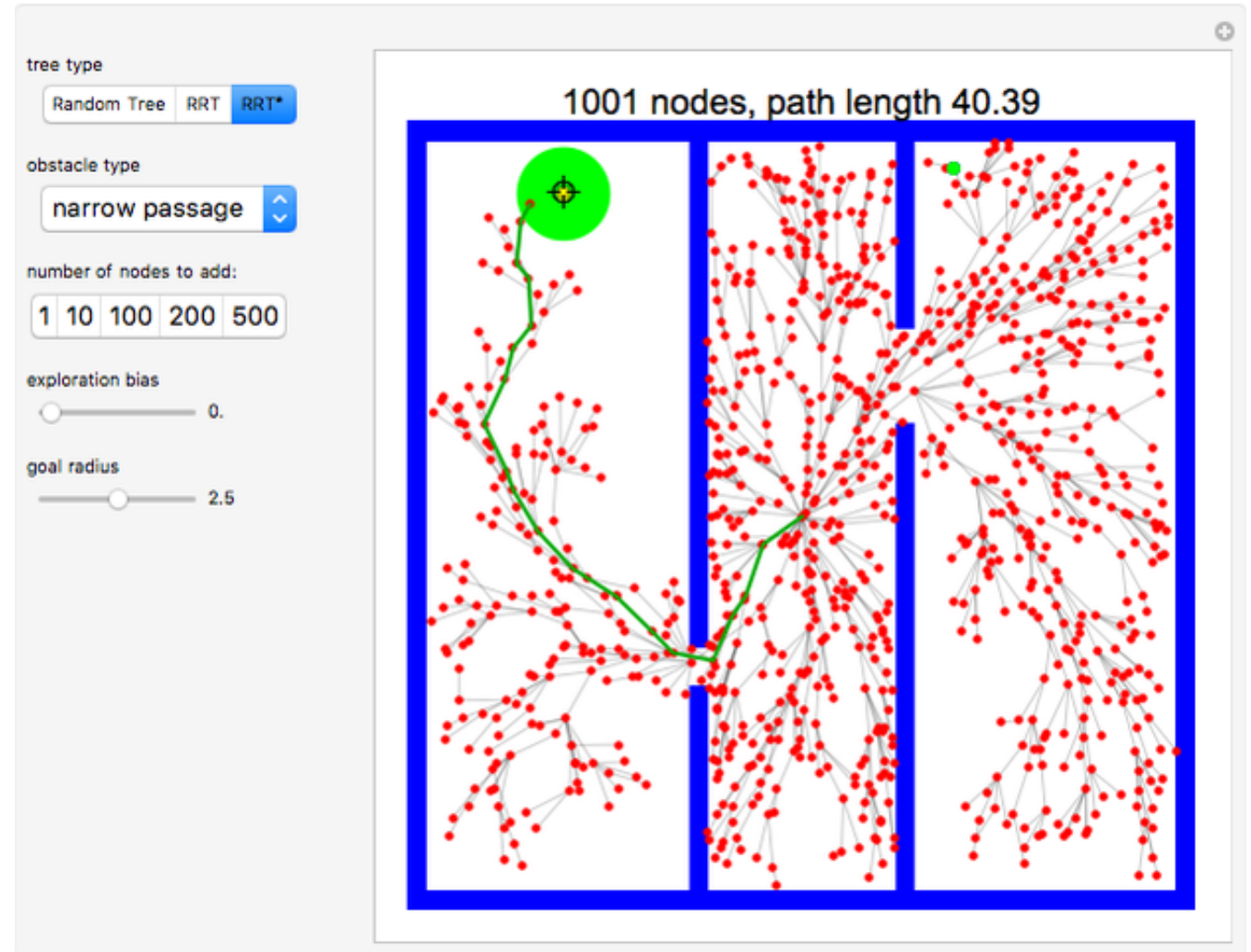
$g(v)$ is the sum cost of operation from start to v

A* algorithm is proven to be complete.

❖ Reference: lots of YouTube videos, e.g.:
<https://www.youtube.com/watch?v=-L-WgKMFuHE>

Random Graph, RRT and RRT*

- Aaron Becker of Houston University: RRT, RRT* & Random Trees:
<https://demonstrations.wolfram.com/RapidlyExploringRandomTreeRRTAndRRT/>
- Multi-robot RRT:
https://github.com/hasauino/rrt_exploration
- Python Robotics Library by Dr. Atsushi Sakai of UC Berkeley
<https://github.com/AtsushiSakai/PythonRobotics#path-planning>



- <https://www.youtube.com/watch?v=Ob3BIJkQJEw>