

- (a) How does Zeroth law of thermodynamics lead to concept of temperature?
 - (b) How does the first-order differ from the second-order phase transitions?
 - (c) Show that $\left(\frac{\partial U}{\partial V}\right)_T = 0$ for an ideal gas.
 - (d) Explain the need for the second law of thermodynamics when the energy conservation law exists.
 - (e) Can the change in entropy be a negative quantity? Support your answer.
 - (f) Calculate the root mean square speed of oxygen molecules at 300K. Take mass of oxygen molecule as 5.31×10^{-26} kg.
 - (g) Discuss the limitations of van der Waal's equation of state.
2. (a) What is Adiabatic Lapse Rate? Derive an expression for the rate of change of temperature with height during the adiabatic gas expansion. How does the presence of water vapour in air affect this process? (6)
- (b) One mole of an ideal gas ($\gamma = 1.4$) initially kept at 27°C is adiabatically compressed so that its pressure becomes 10 times its original value. Calculate its temperature after compression and work done on the gas. (6)
- (c) Show that the 100% efficiency of a reversible Carnot's heat engine violates laws of thermodynamics. (6)
3. (a) If two Carnot engines A and B are operated in series such that engine A absorbs heat at temperature T_1 and rejects heat to the sink at temperature

T_2 while engine B absorbs half of the heat rejected by engine A and rejects heat to the sink at temperature T_3 . If the work done in both cases is equal, show that $T_3 = 3T_2 - 2T_1$. (6)

(b) The heat capacity of a given crystal of mass m at very low temperature varies like T^3 . Calculate the entropy of the crystal as a function of temperature. (6)

(c) Show that transfer of heat from a body at higher temperature to a body at lower temperature or vice versa leads to increase of entropy of the interacting system. (6)

4. (a) Using Maxwell's equation to prove (any two) : (2*6)

(i) $C_p - C_v = \frac{T\alpha^2 v}{\beta_T}$

(ii) Ratio of isentropic to isochoric pressure coefficients of expansion is $\gamma/(\gamma-1)$

(iii) $T dS = C_p dT - T V \alpha dP$

Where, S stands for entropy, C_v and C_p specific heat at constant volume and pressure, respectively. α is the coefficient of volume expansion and β_T is the isothermal compressibility.

(b) Use the path-independent nature of thermodynamic potentials to obtain and derive corresponding Maxwell's thermodynamic relations. (6)

5. (a) Show using Clausius-Clapeyron's latent heat equation that substances which expands on melting have their melting point raised by the increasing pressure, whereas those that contract on melting get their melting points lowered by the increase of pressure. (6)

(b) Draw the pressure-volume isotherms obtained by Andrew's experiments on CO_2 . Discuss the deviations observed from expected ideal gas behavior. (6)

(c) How can van der Waals's equation of state can explain Andrew's experiment results ? (6)

6. (a) Obtain the coefficient of thermal conductivity (K) of a gas. Discuss the effect of temperature and molecular diameter on ? (7+5)

(b) Calculate the mean free path of the molecules of a gas of diameter 3 angstrom at STP. How does the mean free path change if the temperature is reduced to half of its original value and pressure is doubled. (6)

Some useful constants

Boltzmann constant 1.38×10^{-23} J/K, Gas constant 8.31 J/mole-K Avagadro's number 6.02×10^{23} mol⁻¹ or 6.02×10^{26} kmol⁻¹, $1 \text{ amu} = 1.67 \times 10^{-27}$ kg The symbols like U, V, T, p, γ stand for standard notations. (6)