

Random Forest for Classification Problems

Raphael, Arkadiusz and Burak

Uni Bonn

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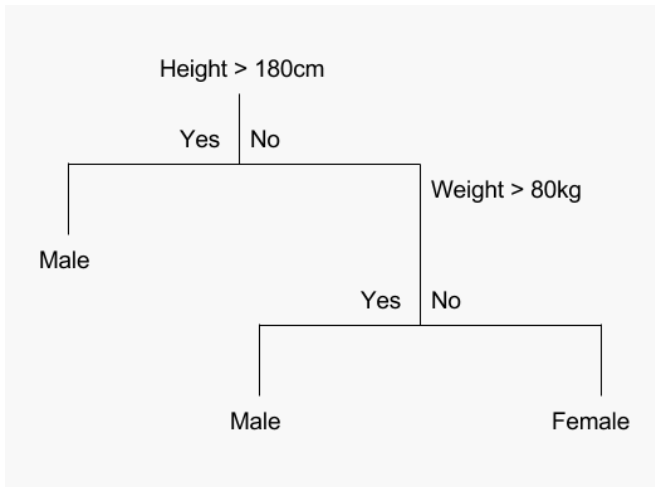
Overview

- 1 Intro
- 2 Decision Tree
- 3 Bias Variance
- 4 Bagging
- 5 Random Forest
- 6 Bias Variance
- 7 Simulation Study
- 8 Real Data
- 9 Conclusion
- 10 References

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Decision Tree: Example



Decision Tree: Tree Building Process

A tree is grown starting from the root node by repeatedly using the following steps on each node (also called binary splitting):

- (i) **Find best split s for each feature X_m :** For each feature X_m , there exist $K - 1$ -many potential splits whereas K is the number of different values for the respective feature. Evaluate each value $X_{m,i}$ at the current node t as a candidate split point (for $x \in X_m$, if $x \leq X_{m,i} = s$, then x goes to left child node t_L else to right child node t_R). The best split point is the one that maximizes the splitting criterion $\Delta i(s, t)$ the most when the node is split according to it. The different splitting criteria will be covered in the next chapter.
- (ii) **Find the node's best split:** Among the best splits for each feature from Step (i) find the one s^* , which maximizes the splitting criterion $\Delta i(s, t)$.
- (iii) **Satisfy stopping criterion:** Split the node t using best node split s^* from Step (ii) and repeat from Step (i) until stopping criterion is satisfied.

Decision Tree: Purity Measures

Gini Measure

$$i(t) = \sum_{c \in C} p(c|t)(1 - p(c|t)) = 1 - \sum_{c \in C} p_c^2 \quad (1)$$

Information Entropy

$$i(t) = \sum_{c \in C} p(c|t) \log(p(c|t)) \quad (2)$$

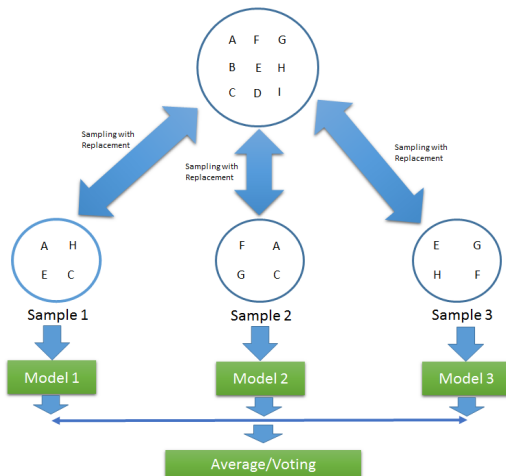
Heading

- 1 Statement
- 2 Explanation
- 3 Example

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Bagging

- 1 created for methods with high variance
- 2 reduces variance and gives better predictions
- 3 improvement of bagging: Random Forest



Random Forest

An ensemble of randomly trained decision trees, so in other words random forest was defined by L. Breiman:

Theorem

A random forest is a classifier consisting of a collection of tree-structured classifiers $\hat{T}_{\theta_b}(\mathbf{x})$, $b = 1, \dots, B$ where the θ_b are independent identically distributed random vectors and each tree casts a unit vote for the most popular class at input \mathbf{x} .

Random Forest is an extension and improvement over bagging:

- 1 Like in bagging, multiple decision trees are built
- 2 Improvement: an injection of randomness is made

Random Forest: randomness in the model

Two key concepts that makes decision forest "random" are:

- 1 Random sampling of training data points when building trees
- 2 Random subsets of features considered when splitting nodes.

Recommended number of variables:

- a For classification: $\lfloor \sqrt{n} \rfloor$
- b For regression: $\lfloor \frac{n}{3} \rfloor$

Algorithm 1: Random Forest for Regression or Classification

- 1 For $b = 1$ to B :
 - a Draw a bootstrap sample θ_b of size N from the training data.
 - b Grow the Random Forest tree T_{θ_b} to the bootstrapped data, by recursively repeating the following steps for each terminal node of the tree, until the minimum node size n_{min} is reached:
 - i Select m variables at random from the n variables
 - ii Pick the best variable/split-point among the m
 - iii Split the node into two daughter nodes
 - 2 Output the ensemble of trees $\{T_{\theta_b}\}_1^B$
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Example (Theorem Slide Code)

```
\begin{frame}  
\frametitle{Theorem}  
\begin{theorem}[Mass--energy equivalence]  
$E = mc^2$  
\end{theorem}  
\end{frame}
```

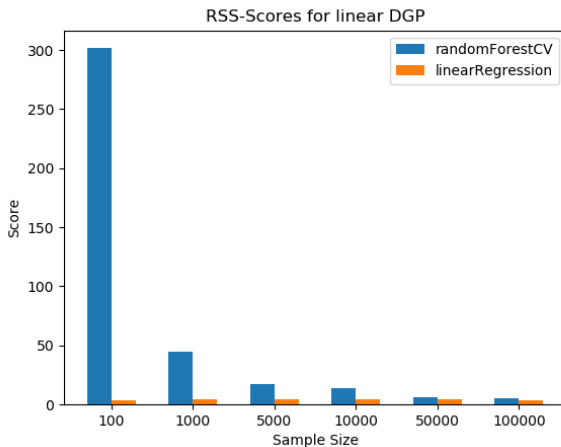
Simulation Study: Linear DGP

The linear DGP generates the data tuples (y, x_1, x_2, x_3) as follows:

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \epsilon, \quad (3)$$

whereas $(\beta_0, \beta_1, \beta_2, \beta_3) = (0.3, 5, 10, 15)$, $x_1, x_2, x_3 \sim \mathcal{N}(0, 3)$, and $\epsilon \sim \mathcal{N}(0, 1)$.

Decision Tree: Linear DGP Results



Simulation Study: Non-Linear DGP

The non-linear DGP generates the data tuples (y, x_1, x_2) as follows:

$$y = \beta_0 + \beta_1 \mathbb{1}(x_1 \geq 0, x_2 \geq 0) + \beta_2 \mathbb{1}(x_1 \geq 0, x_2 < 0) + \beta_3 \mathbb{1}(x_1 < 0) + \epsilon, \quad (4)$$

whereas $(\beta_0, \beta_1, \beta_2, \beta_3)$, x_1, x_2 and ϵ are the same as in the previous DGP.

Simulation Study: Non-Linear DGP Results



An example of the `\cite` command to cite within the presentation:

This statement requires citation [**breiman1984classification**].

The End

References