BLG 336E - ANALYSIS OF ALGORITHMS II

Project 1

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Introduction

We are wanted to implement **DFS** and **BFS** algorithms for solving sliding blocks problem.

Environment

Project implemented in an Ubuntu 16 machine with C++.

Structures

Node: Represents current state. Contains block information in a vector and a hash value for cycle detection.

- Node::fill(bool ar[][MAXN]): Fills ar according to block information.
- Node::print(): Prints blocks in right format
- Node::getHash(): Calculates hash value of node. If it is calculated before(if it is not -1) returns that value. Hash function gives a number transformed from 107(prime number) base modulo 1000000007(prime also).

Block: Represents blocks. It just stores block information.

Code

In the code there are some explanations (comments).

BFS

Breadth First Search is an algorithm that uses a **queue** in order to reach nodes by their distances to start node(when wights of edges are 1 like in this project). Pseudo-code of BFS:

```
Queue.push(start)
while there is at least one element in queue:
      current ← next element in queue
      if current is target node:
            cnt \leftarrow 0 // This will be path length
            write ← create stack
            cur ← current.getHash()
            while until finish the solution path:
                  cnt++
                  write.push(visited[cur]) // next node, found by hash value
            print( all elemets of write stack )
      for each block in current:
            if block is vertical:
                  if neighbouring upper cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited: // Cycle control
                              queue.push(new_state)
                              make → new_state_getHash() visited
                  if neighbouring down cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited: // Cycle control
                              queue.push(new_state)
                              make → new_state_getHash() visited
            else:
                  if neighbouring right cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited: // Cycle control
                              queue.push(new_state)
                              make → new_state_getHash() visited
                  if neighbouring left cell is empty:
                        create → new state
                        if new_state.getHash() is not visited: // Cycle control
                              queue.push(new_state)
                              make → new_state_getHash() visited
```

DFS

Depth First Search is an algorithm that uses a **stack(in my code function calls represents stack)** in order to reach nodes. It doesn't always give the shortest distance like BFS. Pseudo-code of BFS:

```
dfs(node):
     S.push(node) // S is a stack that holds current path
     visited_dfs.insert(node.getHash()) // To avoid cycles
     if node is target node:
           length ← size of S // This is path length
           write ← create stack
           while until finish the solution path:
                  write.push(S.top()) // parent node of last removed node
                 write.pop()
           print( all elemets of write stack )
     for each block in node:
           if block is vertical:
                  if neighbouring upper cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited // Cycle control
                           and dfs(new_state):
                              return true // We found a way
                  if neighbouring down cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited // Cycle control
                           and dfs(new_state):
                              return true // We found a way
           else:
                  if neighbouring right cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited // Cycle control
                           and dfs(new_state):
                              return true // We found a way
                  if neighbouring left cell is empty:
                        create → new_state
                        if new_state.getHash() is not visited // Cycle control
                           and dfs(new_state):
                              return true // We found a way
     S.pop() // removing current node in order to keep the correctly
```

return false // We tried everythong and couldn't find a way

Analysis

For the sake of simplicity, let N be the number of nodes(a state of table) and M be the number of edges(state transitions).

BFS: Time complexity of BFS is O(N+MlgM), because every node goes into queue at most once(O(N)). And every edge is to be tried by program in order to create a new state(O(M)). In addition, cycle detection costs O(lgM) (find function of STL set). So total complexity is O(N+M). According to pseudo-code time complexity of while loop is O(N) and in the while loop there are state transition operations. Sum of every state transition operations is O(M). So we have O(N+M) again.

DFS: Time complexity of DFS is O(N+M), because every node calls with dfs(node) function at most once(O(N)). And every edge is to be tried by program in order to create a new state(O(M)). In addition, cycle detection costs O(lgM) (find function of STL set) So total complexity is O(N+MlgM). According to pseudo-code, time complexity of dfs(node) calls are O(N) and in the function there are state transition operations. Sum of every state transition operations is O(MlgM). So we have O(N+MlgM) again.

Cycle Searches: Checking hash values in visited set costs **O(lgM)** time(STL set). There is no need to go on a node that visited before.

Adjacency List Representation: Complexity of this case depends on implementation. Trying to find every valid node and querying every pair if they have edge between them will be $O(N^2)$ because of calculation of all node pairs. But picking every node individually and finding its' neighbours is O(N+M), it is like the situation above. We are trying transition operations to every node. There are N nodes and M edges(transitions). Plus there will be complexity of DFS-BFS.