

Question-1:

Firstly, I will calculate the support counts for all individual items.

$$\Rightarrow M = \{\text{Beef: } 3/7 \approx 43\%, \text{ Boots: } 1/7 \approx 14\%, \text{ Cheese: } 3/7 \approx 43\%, \text{ Clothes: } 3/7 \approx 43\%, \\ \text{Shoes: } 1/7 \approx 14\%, \text{ Milk: } 3/7 \approx 43\%, \text{ Bread: } 6/7 \approx 86\%\}$$

So, 'Boots' and 'Shoes' will not go to L because they do not satisfy MIS value of first item.

$$\Rightarrow L = \{\text{Beef, Cheese, Clothes, Milk, Bread}\}$$

Now, I must check satisfying own MIS values of items in L for going to set of F_1 . All items satisfy own MIS values except 'Milk', because MIS value of Milk is 50% but support count of Milk is 43%.

$$\Rightarrow F_1 = \{\text{Beef, Cheese, Clothes, Bread}\} \quad // \text{ The information about } F_1 \text{ is given in the question} \\ \text{but I must know itemset which is called 'L' to find the set 'C}_2\text{'}$$

To find set of C_2 .

Statements of for-loop are satisfying based on 4th line in Algorithm MS-Apriori with ' $k = 2$ ' and ' $F_1 \neq \emptyset$ '. Then, if-statement is satisfied in 5th line with ' $k = 2$ ', too. So, I must go to Function level2-candidate-gen. I am creating an empty set which is called ' C_2 '. Then, I am taking the first item in L - Beef- and check satisfying own MIS value. It satisfies and I am taking the item that is after 'Beef', it is 'Cheese'. I check satisfying MIS value of 'Beef' and Bingo! This pair of items fulfil the all conditions and deserve being incorporated into ' C_2 '. I will check all situations about deserving being incorporated into ' C_2 ' for all pairs and I will calculate the itemset ' C_2 '. So,

$$C_2 = \{\{\text{Beef, Cheese}\}, \{\text{Beef, Clothes}\}, \{\text{Beef, Milk}\}, \{\text{Beef, Bread}\}, \{\text{Cheese, Clothes}\}, \{\text{Cheese, Milk}\}, \{\text{Cheese, Bread}\}, \{\text{Clothes, Milk}\}, \{\text{Clothes, Bread}\}\}$$

To find set of F_2 .

I am going back to 9th line of Algorithm MS-Apriori and now, I am taking the first transaction -Beef, Bread-. According to for-loop in 10th line, I am taking the first candidate in C_2 -Beef, Cheese- and I am checking this candidate is contained in this transaction. If the answer is yes, I will add to support count of this candidate. This process is going on for all candidates in C_2 . When all candidates are checked, I will go back to first for-loop and I will take the second transaction. Then, I will check all candidates until all transactions are checked.

$$C_2 = \{\{\text{Beef, Cheese}\}: 2/7 \approx 29\%, \{\text{Beef, Clothes}\}: 0/7 = 0\%, \{\text{Beef, Milk}\}: 1/7 \approx 14\%, \\ \{\text{Beef, Bread}\}: 3/7 \approx 43\%, \{\text{Cheese, Clothes}\}: 0/7 = 0\%, \{\text{Cheese, Milk}\}: 1/7 \approx 14\%, \\ \{\text{Cheese, Bread}\}: 2/7 \approx 29\%, \{\text{Clothes, Milk}\}: 2/7 \approx 29\%, \{\text{Clothes, Bread}\}: 3/7 \approx 43\%\}$$

Finally, a candidate which satisfies MIS value of first item of this candidate is adding to itemset ' F_2 '. So,

$$F_2 = \{\{\text{Beef, Cheese}\}, \{\text{Beef, Bread}\}, \{\text{Cheese, Bread}\}, \{\text{Clothes, Milk}\}, \{\text{Clothes, Bread}\}\}$$

To find set of C_3 .

I am going back to 4th line in Algorithm MS-Apriori. Statements of for-loop are satisfying with ' $k = 3$ ' and ' $F_2 \neq \emptyset$ '. Then, , if-statement is not satisfied in 5th line and I am going to 7th line which defines the C_3 using Function MSCandidate-gen. So, I am going to MSCandidate-gen function. First of all, I am creating the candidate itemset which is called ' C_3 '. Now, I am searching for f_1 and f_2 which are same except last item of them. Also, last item of f_2 must be greater than last item of f_1 according to MIS value and if MIS values are equal, I must check lexicographic order. So, I found two pair.

1. The first of these pairs,

- **f_1 : Beef, Bread**
- **f_2 : Beef, Cheese**

I am identifying a candidate which is named ' c ' and so, **$c = \{\text{Beef, Bread, Cheese}\}$** . I am adding this ' c ' to the C_3 and **$C_3 = \{\{\text{Beef, Bread, Cheese}\}\}$** for now. In 8th and 9th lines, these if-statements are for removing c from C_3 . For each all 2-subsets which is named ' s_1, s_2 and s_3 '.

1. **s_1 : Beef, Bread**

First if-statement is true, because first item of c is in s_1 . Second if-statement is not true because s_1 is in F_2 . So, it will not be deleted for now.

2. **s_2 : Beef, Cheese**

First if-statement is true, because first item of c is in s_2 . Second if-statement is not true because s_2 is in F_2 . So, it will not be deleted for now.

3. **s_3 : Bread, Cheese**

First if-statement is not true, because first item of c is not in s_3 OR MIS values of Bread and Cheese are not equal. So, c is not deleted from C_3 .

2. The second of these pairs,

- **f_1 : Clothes, Bread**
- **f_2 : Clothes, Milk**

I am identifying a candidate which is named ' c ' and so, **$c = \{\text{Clothes, Bread, Milk}\}$** . I am adding this ' c ' to the C_3 and **$C_3 = \{\{\text{Beef, Bread, Cheese}\}, \{\text{Clothes, Bread, Milk}\}\}$** for now. In 8th and 9th lines, these if-statements are for removing c from C_3 . For each all 2-subsets which is named ' s_1, s_2 and s_3 '.

1. **s_1 : Clothes, Bread**

First if-statement is true, because first item of c is in s_1 . Second if-statement is not true because s_1 is in F_2 . So, it will not be deleted for now.

2. **s_2 : Clothes, Milk**

First if-statement is true, because first item of c is in s_2 . Second if-statement is not true because s_2 is in F_2 . So, it will not be deleted for now.

3. **s_3 : Bread, Milk**

First if-statement is not true, because first item of c is not in s_3 OR MIS values of Bread and Cheese are not equal. So, c is not deleted from C_3 .

Finally, I found the C_3 and it is,

$C_3 = \{\{\text{Beef, Bread, Cheese}\}, \{\text{Clothes, Bread, Milk}\}\}$

To find set of F_3 ,

I am going back to 9th line of Algorithm MS-Apriori and now, I am taking the first transaction -Beef, Bread-. According to for-loop in 10th line, I am taking the first candidate in C_3 -Beef, Bread, Cheese- and I am checking this candidate is contained in this transaction. If the answer is yes, I will add to support count of this candidate. This process is going on for all candidates in C_3 . When all candidates are checked, I will go back to first for-loop and I will take the second transaction. Then, I will check all candidates until all transactions are checked.

$C_3 = \{\{\text{Beef, Bread, Cheese}\}; 2/7 \approx 29\%, \{\text{Clothes, Bread, Milk}\}; 2/7 \approx 29\%\}$

Finally, a candidate which satisfies MIS value of first item of this candidate is added to itemset ' F_3 '.
So,

$F_3 = \{\{\text{Beef, Bread, Cheese}\}, \{\text{Clothes, Bread, Milk}\}\}$

Question-2:

I am calculating the values of probability of Class is T and Class is F.

$\Pr(Class = T) = \frac{5}{10} = \frac{1}{2}$	$\Pr(Class = F) = \frac{5}{10} = \frac{1}{2}$
---	---

I am calculating the values of probability about variables of 'Attr1' when Class is T, and Class is F.

$\Pr(Attr1 = x1 Class = T) = \frac{2}{5}$	$\Pr(Attr1 = x1 Class = F) = \frac{1}{5}$
$\Pr(Attr1 = x2 Class = T) = \frac{2}{5}$	$\Pr(Attr1 = x2 Class = F) = \frac{2}{5}$
$\Pr(Attr1 = x3 Class = T) = \frac{1}{5}$	$\Pr(Attr1 = x3 Class = F) = \frac{2}{5}$

I am calculating the values of probability about variables of 'Attr2' when Class is T, and Class is F.

$\Pr(Attr2 = x4 Class = T) = \frac{1}{5}$	$\Pr(Attr2 = x4 Class = F) = \frac{2}{5}$
$\Pr(Attr2 = x5 Class = T) = \frac{2}{5}$	$\Pr(Attr2 = x5 Class = F) = \frac{1}{5}$
$\Pr(Attr2 = x6 Class = T) = \frac{2}{5}$	$\Pr(Attr2 = x6 Class = F) = \frac{2}{5}$

1. Attr1 = x1 and Attr2 = x6, so Class = ?

$$\Pr(Class = T) \times \Pr(Attr1 = x1 | Class = T) \times \Pr(Attr2 = x6 | Class = T) = \frac{1}{2} \times \frac{2}{5} \times \frac{2}{5} = \frac{4}{50}$$

$$\Pr(Class = F) \times \Pr(Attr1 = x1 | Class = F) \times \Pr(Attr2 = x6 | Class = F) = \frac{1}{2} \times \frac{1}{5} \times \frac{2}{5} = \frac{2}{50}$$

So,

probability of Class is T is greater than probability of Class is F. Consequently, **Class must be T.**

2. Attr1 = x2 and Attr2 = x4, so Class = ?

$$\Pr(Class = T) \times \Pr(Attr1 = x2 | Class = T) \times \Pr(Attr2 = x4 | Class = T) = \frac{1}{2} \times \frac{2}{5} \times \frac{1}{5} = \frac{2}{50}$$

$$\Pr(Class = F) \times \Pr(Attr1 = x2 | Class = F) \times \Pr(Attr2 = x4 | Class = F) = \frac{1}{2} \times \frac{2}{5} \times \frac{2}{5} = \frac{4}{50}$$

So,

probability of Class is F is greater than probability of Class is T. Consequently, **Class must be F.**