

CS 353 Spring 2020

Homework 4

Due: 13 April, Monday till midnight

You will use the Moodle course page for submission of this assignment

Q.1 [18 pts, 2 pts each] Given the following instance of the relation R(A,B,C)

| | A | B | C |
|---------|----|----|----|
| Tuple 1 | a1 | b1 | c1 |
| Tuple 2 | a1 | b2 | c2 |
| Tuple 3 | a2 | b3 | c1 |
| Tuple 4 | a2 | b3 | c2 |

Which of the following dependencies may hold in relation R? If a dependency cannot hold, indicate which tuples cause the violation.

- (a) $B \rightarrow A$ (b) $C \rightarrow A$ (c) $A \rightarrow B$ (d) $C \rightarrow B$ (e) $A \rightarrow C$ (f) $B \rightarrow C$ (g) $BC \rightarrow A$
(h) $AC \rightarrow B$ (i) $AB \rightarrow C$

Q.2 [8 pts, 4 pts each] Given the following relations with functional dependencies:

Relations: P(A, B, C, D) and Q(A, B, C, D)

Functional Dependencies:

- For P: $A \rightarrow BCD$, $B \rightarrow ACD$

- For Q: $BC \rightarrow AD$, $D \rightarrow B$

- (a) Find all candidate keys in P
(b) Find all candidate keys in Q

Q.3 [20 pts] Given the following relation with functional dependencies:

Relation: S(A, B, C, D, E, F, G)

Functional Dependencies: $F = \{BCD \rightarrow A, BC \rightarrow E, A \rightarrow F, F \rightarrow G, C \rightarrow D, A \rightarrow G\}$

Decompose S into 3NF. The decomposition should be lossless-join and dependency preserving. Show all your work.

Q.4 [24 pts] Given the following relation with functional dependencies:

Relation: Q(A,B,C,D,E)

Functional Dependencies: $AB \rightarrow E$ and $D \rightarrow C$

- (a) [6 pts] Find all superkey(s) and candidate key(s)
(b) [18 pts] Decompose Q into BCNF. Show all your work.

Q.5 [18 pts, 6 pts each] Determine if the following decompositions are lossless-join or not. Show all your work.

- (a) Given the relational schema S(A, B, C, D, E), and the functional dependency set: $\{A \rightarrow C, BD \rightarrow A, D \rightarrow E\}$. S is decomposed into S1(B, C, D), S2(A, B, D) and S3(A, E)
(b) Given the relational schema S(A, B, C, D), and the functional dependency set: $\{A \rightarrow BCD, B \rightarrow C, CD \rightarrow A\}$. S is decomposed into S1(A, B, C) and S2(B, C, D)
(c) Given the relational schema S(A, B, C, D), and the functional dependency set: $\{A \rightarrow BCD, B \rightarrow C, CD \rightarrow A\}$. S is decomposed into S1(A, B, D) and S2(B, C)

Q.6 [12 pts] Given the relational schema S(A, B, C, D), and the functional dependency set:

$\{ A \rightarrow BCD, B \rightarrow C, CD \rightarrow A \}$. Determine if the decomposition of S into $S_1(A, B, C)$ and $S_2(B, C, D)$ is dependency preserving or not. Show all your work.