

## [0 pts] The most valuable tree

In graph theory, a Tree is an undirected graph in which any two vertices are connected by exactly one path. Trees have some nice mathematical properties, e.g, if  $n$  is the number of vertices of a Tree, then there are exactly  $n-1$  edges in the graph.

In this question you will be provided with a Tree, let's call it  $\mathbf{T}$ , which has  $\mathbf{n}$  vertices, numbered from 1 to  $n$ . The vertex 1 is the root of  $\mathbf{T}$ . Furthermore, each vertex has a correspondence value, to be more specific, the node  $i$  has the value of  $v_i$  (The value could be positive or negative). The value of a  $\mathbf{T}$  is defined as the sum of the value of its vertices. However, we are not satisfied with the value of  $\mathbf{T}$ , and we want to cut some sub-trees so that the value of our Tree increase. One constraint about this problem is that we are only allowed to cut  $\mathbf{k}$  sub-trees.

### Input

The first line contains two integers  $\mathbf{n}$  and  $\mathbf{k}$  ( $2 \leq n \leq 10^5, 1 \leq k \leq 200$ ) – where  $\mathbf{n}$  is the number of vertices of the tree and  $\mathbf{k}$  is the maximum number of cut from the Tree (you even can have a zero cut).

The second line contains  $n$  integers describing the value of each node. To be more precise, the  $i$ -th integer is the value of  $i$ -th node ( $-10^9 \leq V_i \leq 10^9$ )

Each of the next  $\mathbf{n-1}$  lines consist of two integer  $\mathbf{v}$  and  $\mathbf{u}$ . It indicates that there is a edge between node  $\mathbf{v}$  and node  $\mathbf{u}$ .

### Output

Print a single integer denoting the value of the final Tree.

#### Example 1

##### Input

```
5 2
1 1 -1 -1 -1
1 2
2 3
4 1
4 5
```

##### Output

```
2
```

### Explanation

We use both two cuts: we remove the sub-trees rooted at node 3 and 4.

## Deliveries

You are suppose to find efficient algorithm that can solve the question in  $O(nk)$ . Finding a better asymptotic complexity has bonus. You also need to make a document that clearly explain your approach and your reasoning for asymptotic complexity. You also need to manually write 10 test cases (both input and output) to check correctness of your program. Your test cases should be such that it consider a variety of possibilities.