

Practical Exercise 5 | Statistics for CSAI II

Burcu_Ibicioglu, u986202

The goals of this exercise are to (a) to use R to run multiple linear regression models that include polynomials, b) running mixed models, and c) growth curve models.

Tasks indicate things that you need to complete in R/R Studio.

Task 1. Load the winequality-red.csv data file.

```
data<-read.csv('/Users/burcuibicioglu/Downloads/Practical Exercise 5-2/Practical Exercise 5/Wine.csv', ,
```

Task 2. Inspect the data by looking at the first few entries and the last few entries in the dataset as well as the variable types. In particular, we are interested in predicting the “quality” of the red wine, by knowing the “total.sulfur.dioxide” content of the wine.

```
head(data)
```

```
##    fixed.acidity volatile.acidity citric.acid residual.sugar chlorides
## 1             7.4             0.70         0.00             1.9      0.076
## 2             7.8             0.88         0.00             2.6      0.098
## 3             7.8             0.76         0.04             2.3      0.092
## 4            11.2             0.28         0.56             1.9      0.075
## 5             7.4             0.70         0.00             1.9      0.076
## 6             7.4             0.66         0.00             1.8      0.075
##    free.sulfur.dioxide total.sulfur.dioxide density    pH sulphates alcohol
## 1                   11                   34 0.9978 3.51     0.56     9.4
## 2                   25                   67 0.9968 3.20     0.68     9.8
## 3                   15                   54 0.9970 3.26     0.65     9.8
## 4                   17                   60 0.9980 3.16     0.58     9.8
## 5                   11                   34 0.9978 3.51     0.56     9.4
## 6                   13                   40 0.9978 3.51     0.56     9.4
##    quality
## 1         5
## 2         5
## 3         5
## 4         6
## 5         5
## 6         5
```

```
tail(data)
```

```
##    fixed.acidity volatile.acidity citric.acid residual.sugar chlorides
## 1594           6.8             0.620         0.08             1.9      0.068
## 1595           6.2             0.600         0.08             2.0      0.090
## 1596           5.9             0.550         0.10             2.2      0.062
## 1597           6.3             0.510         0.13             2.3      0.076
```

```
## 1598          5.9          0.645          0.12          2.0          0.075
## 1599          6.0          0.310          0.47          3.6          0.067
##      free.sulfur.dioxide total.sulfur.dioxide density    pH sulphates alcohol
## 1594          28          38 0.99651 3.42      0.82      9.5
## 1595          32          44 0.99490 3.45      0.58     10.5
## 1596          39          51 0.99512 3.52      0.76     11.2
## 1597          29          40 0.99574 3.42      0.75     11.0
## 1598          32          44 0.99547 3.57      0.71     10.2
## 1599          18          42 0.99549 3.39      0.66     11.0
##      quality
## 1594          6
## 1595          5
## 1596          6
## 1597          6
## 1598          5
## 1599          6
```

```
summary(data$total.sulfur.dioxide)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      6.00  22.00  38.00  46.47  62.00 289.00
```

```
summary(data$quality)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      3.000  5.000  6.000  5.636  6.000  8.000
```

a. Generate descriptive statistics. Evaluate these descriptives and print them here.

```
install.packages("psych")
```

```
## Error in contrib.url(repos, "source"): trying to use CRAN without setting a mirror
```

```
library(psych)
```

```
## Warning: package 'psych' was built under R version 4.3.3
```

```
describe.by(data)
```

```
## Warning: describe.by is deprecated. Please use the describeBy function
```

```
## Warning in describeBy(x = x, group = group, mat = mat, type = type, ...): no
## grouping variable requested
```

```
##      vars      n mean    sd median trimmed   mad  min   max
## fixed.acidity    1 1599  8.32  1.74   7.90    8.15 1.48 4.60 15.90
## volatile.acidity  2 1599  0.53  0.18   0.52    0.52 0.18 0.12  1.58
## citric.acid       3 1599  0.27  0.19   0.26    0.26 0.25 0.00  1.00
## residual.sugar    4 1599  2.54  1.41   2.20    2.26 0.44 0.90 15.50
## chlorides         5 1599  0.09  0.05   0.08    0.08 0.01 0.01  0.61
## free.sulfur.dioxide 6 1599 15.87 10.46 14.00   14.58 10.38 1.00 72.00
## total.sulfur.dioxide 7 1599 46.47 32.90 38.00   41.84 26.69 6.00 289.00
## density           8 1599  1.00  0.00   1.00    1.00 0.00 0.99  1.00
## pH                9 1599  3.31  0.15   3.31    3.31 0.15 2.74  4.01
## sulphates        10 1599  0.66  0.17   0.62    0.64 0.12 0.33  2.00
## alcohol          11 1599 10.42  1.07  10.20   10.31 1.04 8.40 14.90
## quality          12 1599  5.64  0.81   6.00    5.59 1.48 3.00  8.00
##
##      range skew kurtosis    se
## fixed.acidity 11.30 0.98    1.12 0.04
```

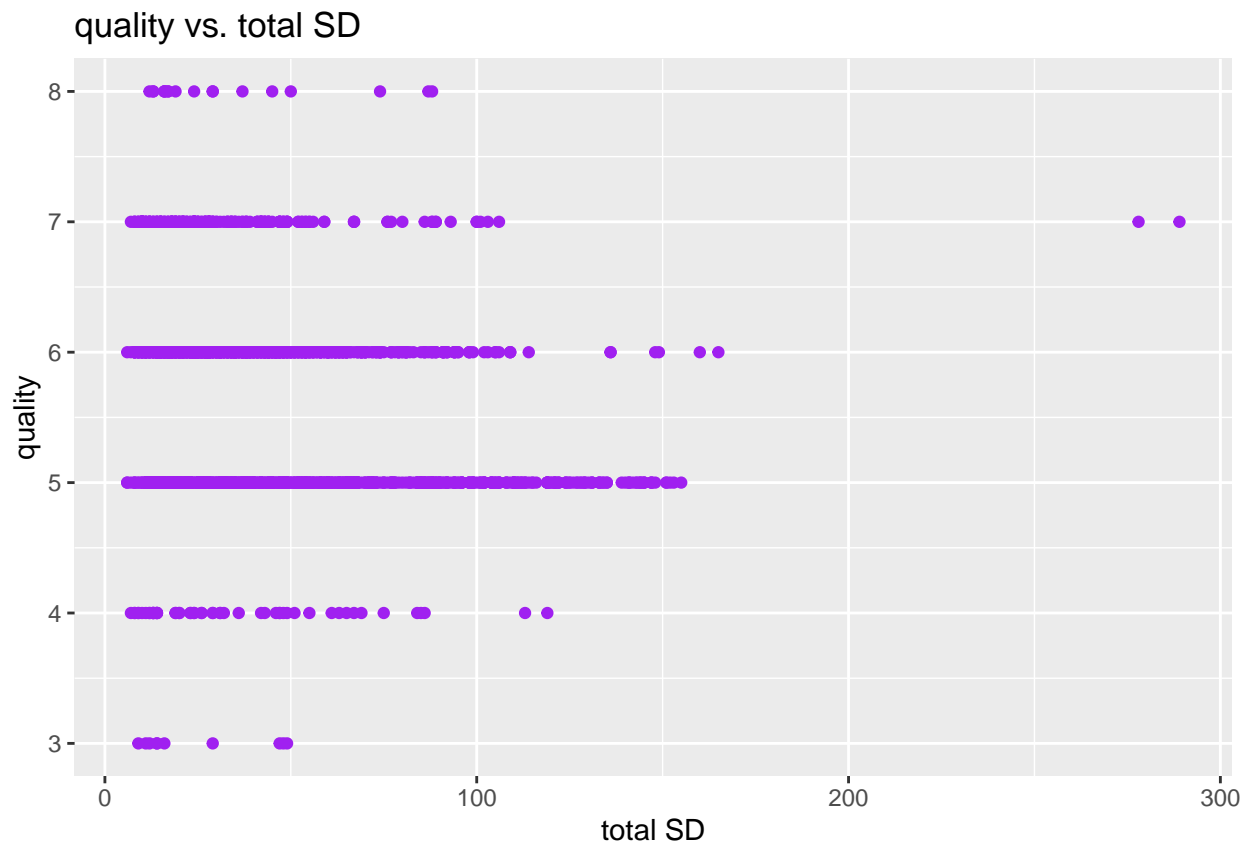
```
## volatile.acidity      1.46 0.67      1.21 0.00
## citric.acid           1.00 0.32     -0.79 0.00
## residual.sugar       14.60 4.53     28.49 0.04
## chlorides             0.60 5.67     41.53 0.00
## free.sulfur.dioxide   71.00 1.25      2.01 0.26
## total.sulfur.dioxide 283.00 1.51      3.79 0.82
## density              0.01 0.07      0.92 0.00
## pH                   1.27 0.19      0.80 0.00
## sulphates            1.67 2.42     11.66 0.00
## alcohol              6.50 0.86      0.19 0.03
## quality              5.00 0.22      0.29 0.02
```

- b. Make a scatter plot of the relationship between “quality” and “total.sulfur.dioxide”. Does it look like the relationship is best fit by a straight line or perhaps something curvilinear?

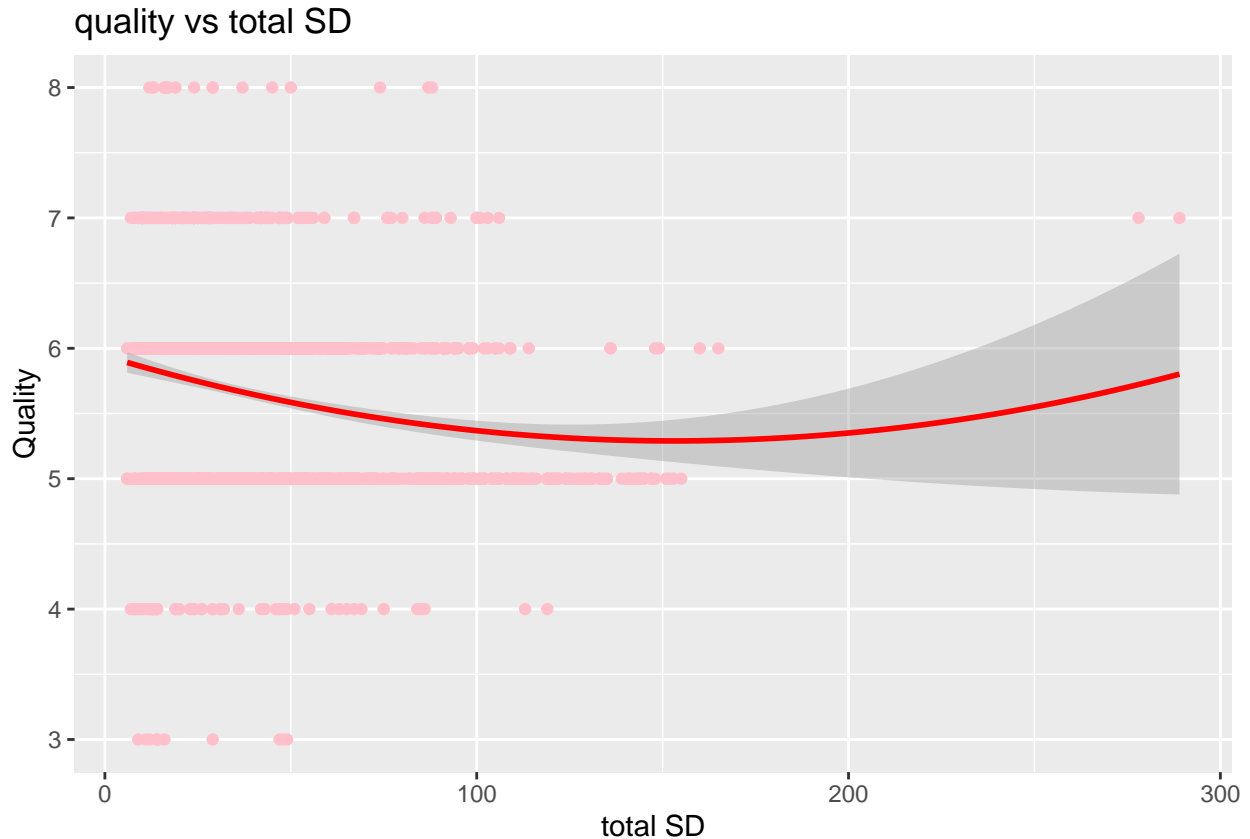
```
library(ggplot2)
```

```
##
## Attaching package: 'ggplot2'
## The following objects are masked from 'package:psych':
##
##    %+%, alpha
```

```
ggplot(data, aes(x = total.sulfur.dioxide, y = quality)) + geom_point(color = "purple") + ggtitle("qual.
```



```
ggplot(data, aes(x = total.sulfur.dioxide, y = quality)) + geom_point(color = "pink") + geom_smooth(method = "lm", color = "red")
```



##BETTER FIT BY A CURVILINEAR##

Task 3. Run a series of polynomial multiple regression models with “quality” as your outcome that includes “total.sulfur.dioxide” as a predictor. Start with a linear model, then add a quadratic term, then run another model that includes a cubic term. Compare the results of the models.

```
model <- lm(quality ~ total.sulfur.dioxide, data = data)
summary(model)
```

```
##
## Call:
## lm(formula = quality ~ total.sulfur.dioxide, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8063 -0.6336  0.2164  0.3800  2.5527
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.8471792   0.0343670  170.140 < 2e-16 ***
## total.sulfur.dioxide -0.0045442   0.0006037  -7.527 8.62e-14 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7939 on 1597 degrees of freedom
## Multiple R-squared:  0.03426,    Adjusted R-squared:  0.03366
```

```
## F-statistic: 56.66 on 1 and 1597 DF, p-value: 8.622e-14
```

```
qmodel <- lm(quality ~ total.sulfur.dioxide + I(total.sulfur.dioxide^2), data = data)
summary(qmodel)
```

```
##
## Call:
## lm(formula = quality ~ total.sulfur.dioxide + I(total.sulfur.dioxide^2),
##     data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8670 -0.6028  0.1723  0.4146  2.5923
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      5.941e+00  4.773e-02 124.480 < 2e-16 ***
## total.sulfur.dioxide -8.508e-03  1.521e-03  -5.592 2.64e-08 ***
## I(total.sulfur.dioxide^2)  2.777e-05  9.789e-06   2.837 0.00461 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7921 on 1596 degrees of freedom
## Multiple R-squared:  0.03911, Adjusted R-squared:  0.0379
## F-statistic: 32.48 on 2 and 1596 DF, p-value: 1.495e-14
```

```
cmodel <- lm(quality ~ total.sulfur.dioxide + I(total.sulfur.dioxide^2) + I(total.sulfur.dioxide^3), data = data)
summary(cmodel)
```

```
##
## Call:
## lm(formula = quality ~ total.sulfur.dioxide + I(total.sulfur.dioxide^2) +
##     I(total.sulfur.dioxide^3), data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.7637 -0.6670  0.2371  0.3459  2.5971
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      5.749e+00  6.722e-02  85.523 < 2e-16 ***
## total.sulfur.dioxide  2.454e-03  3.107e-03   0.790  0.42980
## I(total.sulfur.dioxide^2) -1.087e-04  3.515e-05  -3.092  0.00202 **
## I(total.sulfur.dioxide^3)  4.099e-07  1.014e-07   4.040 5.59e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7883 on 1595 degrees of freedom
## Multiple R-squared:  0.04884, Adjusted R-squared:  0.04705
## F-statistic: 27.3 on 3 and 1595 DF, p-value: < 2.2e-16
```

- a. Report the results here in APA format. Be sure to include the adjusted R² value, the b estimates, and the p-values. What can you conclude from your results and which model best characterizes this relationship?

The results show that the cubic model provided the best fit for the data, with an adjusted

$R^2=0.04705$. However, the model had a non-significant p-value for the linear term ($p=0.4298$), which can mean that it may not be statistically meaningful. The quadratic model also showed a significant relationship ($p=0.00461$), with an adjusted $R^2=0.0379$. The linear model explained just 3.36% of the variance, suggesting limited prediction for total sulfur dioxide. In conclusion, while the cubic model provided a better fit in terms of adjusted R^2 , the quadratic model is more reliable because it is statistically significant.###