

18YZALG — Tutorial 1 Assignments

Tutorial 1 — Mini-Projects

Choose **one** mini-project per group and present your solution in the next tutorial session.

Quick facts

Item	Description
Who	Student groups (recommended 2–3 students)
When	Next tutorial, i.e., February 24th
What	Short live demo
What we practice	Algorithm description, correctness tests, basic time/memory complexity, simple benchmarking
Grading	Extra credit to the continuous assessment component (tutorial part of the course)

What every group must include

- **Problem statement:** input format, output format, and edge cases (5–10 lines).
- **At least two approaches** to the same task (three is even better). Include a clear algorithm description (plain English or try with pseudocode).
- **Complexity:** informal Big-O time and memory discussion for each approach.
- **Benchmark:** measure runtime for multiple input sizes and interpret the trend (a table is enough; a plot is optional but welcomed).
- **Correctness checks:** a small test suite (simple assert tests are sufficient). Test your implementation on some trivial cases.
- **Conclusion:** when would you use which approach, and why?

Submission format

- You do not need to submit any files beforehand, the only deliverable here is the live demonstration.
- For the demonstration you can use a presentation format, Jupyter notebook, or whatever you are comfortable with. The only requirement is it has to contain all the required contents..

Live demonstration checklist (presentation)

Aim for a concise demo, 10–15 minutes is more than enough. You may split speaking roles inside the group, but it is optional.

Example presentation could look like:

- **1 minute:** Problem statement + what counts as a correct output.

- **2–3 minutes:** Approaches (Method 1 baseline, Method 2 improvement, Method 3 improvement). Show high-level logic, not every line.
- **1–2 minutes:** Complexity: explain Big-O in one or two sentences per method.
- **1–2 minutes:** Benchmark: show a runtime table and explain the scaling.
- **1–2 minutes:** Correctness: run tests or show representative tests.
- **1–2 minutes:** Final takeaway (which method wins when, and trade-offs).

Assessment

Maximum of 20 points for this given presentation, later translated to the overall tutorial part of the course assessment.

Criterion	Points	What we look for
Correctness & tests	0–5	Works on edge cases; tests are clear and actually run
Algorithm description & complexity	0–5	Approaches are explained; Big-O time/memory reasoning is plausible
Benchmark & interpretation	0–5	Multiple input sizes; fair timing; conclusions match results
Demo clarity	0–5	Clear structure and presentation

Mini-Projects

Pick exactly one. Each project is designed so you can compare multiple approaches, reason about complexity, and validate with tests and benchmarks.

1. Duplicate detection at scale

Goal. Given a list of IDs, decide whether any value appears at least twice.

Required content

- Define the input clearly (integers/strings are enough) and specify edge cases (empty list, all unique, all equal).
- Implement at least two methods and ensure they return identical results on the same tests.
- Benchmark across at least 5 input sizes and identify where the baseline becomes impractical.

Suggested approaches to compare

- Method 1 (baseline): pairwise comparison of all pairs ($i < j$).
- Method 2: sort a copy and scan adjacent elements.
- Method 3: scan with a set of seen elements.

Demo focus

- Show a tiny example list and walk through what each method does.
- Run your tests live (or show the command and output).
- Show the benchmark table and explain the scaling trend.

Stretch goals (optional)

- Return the first duplicate encountered in a stream (online variant).
- Return all duplicates and compare the cost to the boolean variant.

2. Membership queries: list vs sorted+binary vs set

Goal. You have a database of allowed IDs and a list of query IDs. For each query, decide membership.

Required content

- Specify input sizes using two parameters: n = database size, q = number of queries.
- Compare at least two strategies, one of which includes preprocessing.
- Benchmark for different q/n ratios (e.g., few queries vs many queries).

Suggested approaches to compare

- Baseline: for each query, linear search through a list ($O(nq)$).
- Preprocess: sort once + binary search each query (use `bisect`).
- Preprocess: build a set once + membership checks (average $O(1)$ per query).

Demo focus

- Explain why preprocessing can pay off when q is large.
- Include at least one benchmark where sorting beats linear search.

Stretch goals (optional)

- Find the break-even point: for a fixed n , vary q and find when preprocessing wins.
- Add a short memory discussion (list vs set).

3. Fibonacci: recursion, iteration, memoization

Goal. Compute $F(n)$ and study the impact of algorithm design choices.

Required content

- Define the Fibonacci sequence you use ($F(0)$, $F(1)$ base cases).
- Include at least one intentionally slow baseline method to demonstrate scaling issues.
- Benchmark for increasing n and report the largest n you can compute within a fixed time budget.

Suggested approaches to compare

- Baseline: naive recursion (exponential time).
- Improved: iterative loop (linear time).
- Improved: recursion with memoization (linear time).

Demo focus

- Show that naive recursion becomes unusable quickly (but still correct).

- Explain how memoization changes the number of repeated subproblems.

Stretch goals (optional)

- Count function calls in the naive recursion and show calls vs n.
- Compare memoization with bottom-up DP explicitly.

4. Prime numbers up to N: trial division vs sieve

Goal. Generate all primes up to N and compare algorithmic approaches.

Required content

- Define what you output (list of primes, count of primes, or boolean primality array).
- Include correctness checks for small N (e.g., N=30) where you know the exact primes.
- Benchmark for multiple N values and describe scaling.

Suggested approaches to compare

- Baseline: trial division by all integers up to n-1 (or up to n).
- Improved: trial division up to \sqrt{n} , skipping evens.
- Improved: sieve of Eratosthenes.

Demo focus

- Explain why \sqrt{n} is enough for trial division.
- Explain why the sieve trades memory for speed.

Stretch goals (optional)

- Use `bytearray` for a compact sieve representation.
- Compare returning a list of primes vs a boolean mask.

5. Top-K frequent items (practical data task)

Goal. Given a text or a list of tokens, find the top-K most frequent items.

Required content

- Specify how you tokenize input (simple split is fine) and how you handle case/punctuation (state your choice).
- Implement at least two counting approaches and return the same top-K result.
- Benchmark on scaled input sizes (e.g., repeat the text).

Suggested approaches to compare

- Baseline: repeated counting (e.g., using `list.count` in a loop) to show inefficiency.
- Improved: dictionary counting (hash map).
- Optional: `collections.Counter` and compare constant factors.

- Optional: compare sorting all counts vs using a heap for top-K.

Demo focus

- Show your top-K output for a small sample text.
- Show a benchmark table and explain why the baseline scales poorly.

Stretch goals (optional)

- Add ties handling (stable ordering) and explain your rule.
- Compare memory usage for different implementations (qualitatively).

Closing note

Keep it simple. The goal is not maximum performance at any cost — it is learning how algorithm design, data structures, and complexity reasoning translate into real runtime behavior.